

*SCALE Users' Group Workshop*  
*27-29 August 2018*

Advanced BWR Criticality Safety with Quantified Uncertainty Using Various  
SCALE Modules

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# Contents

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- **Background**

- Advanced BWR Depletion Cases (T-Depl and T5-Depl)
- Criticality Calculations (CSAS5/KENO-V.a)
- Sensitivity and Uncertainty Analyses (TSUNAMI-3D)
- BWR Isotopic Uncertainty Quantification (Sampler)
- Summary

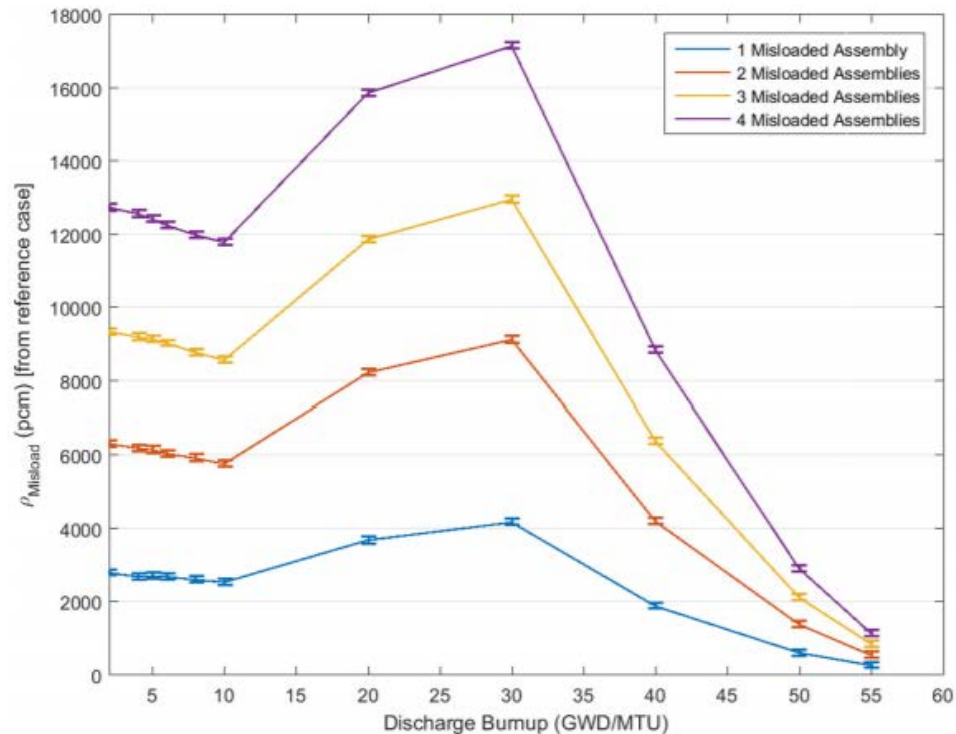
# Objectives

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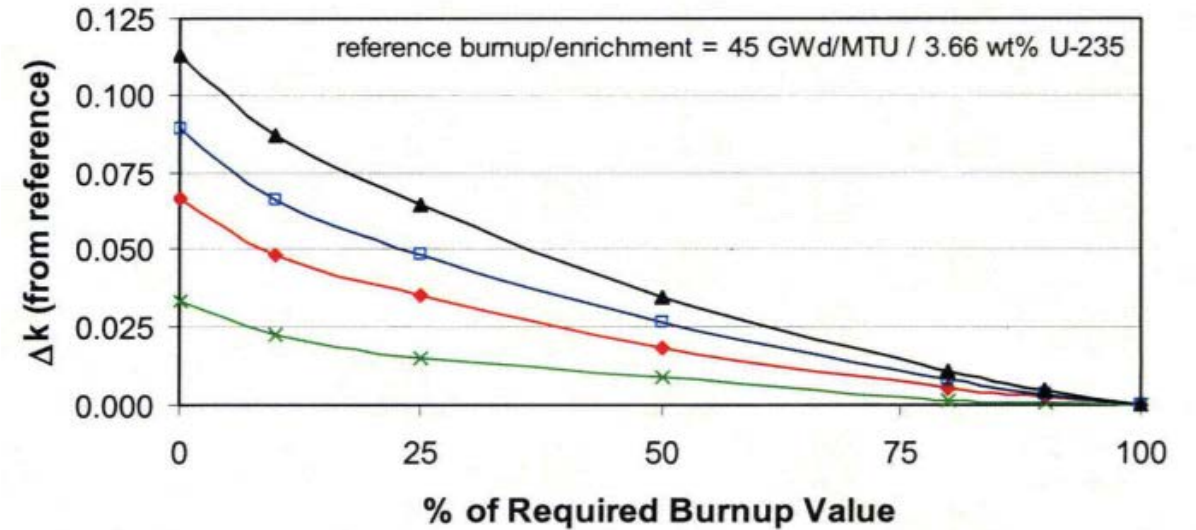
- Review our activities on BWR criticality safety based on NEUP funded project on “Cask Misload Evaluation Techniques”.
- Build a set of computational models in SCALE to capture BWR design complexities for a single lattice
  - Control rod insertion.
  - Gadolinium presence.
  - Heterogenous radial and axial enrichment.
  - Part-length rods.
  - Axial burnup and void fraction profiles.
  - Partial control rod insertion.
  - Control rod movement.
- Investigate the effect of such complexities on the burnup credit and cask  $k_{\text{eff}}$  uncertainty.
- Incorporate BWR spent fuel assay data to quantify the isotopic uncertainty in cask  $k_{\text{eff}}$ .

# Previous Cask Misloading Efforts

**BWR Misloading (Radaideh et al.)**



**PWR Misloading (Wagner)**



Radaideh, M.I., 2018. Criticality and Uncertainty Assessment of Assembly Misloading in BWR Transportation Cask, Annals of Nuclear Energy, 113, pp. 1-14.

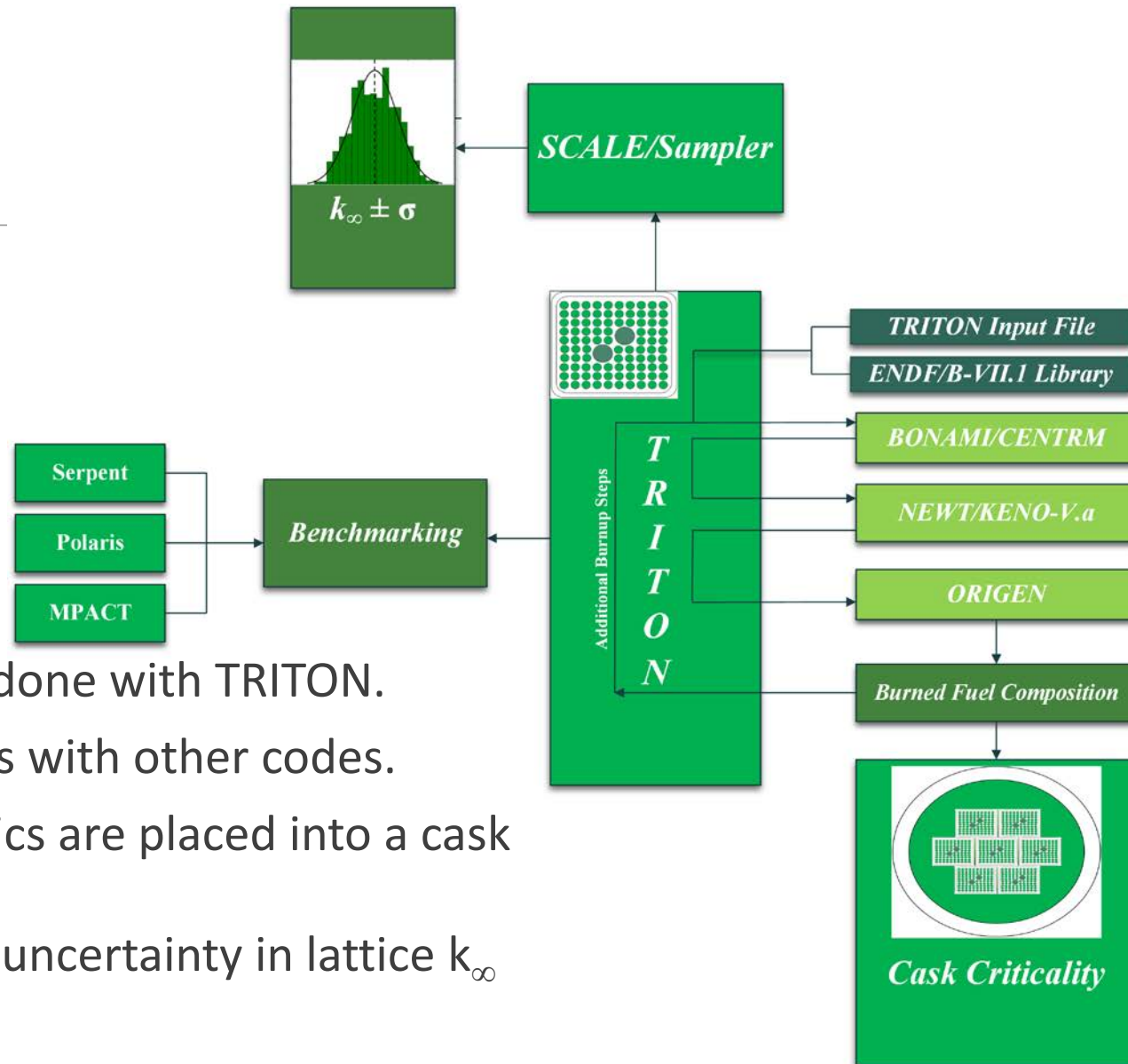
Wagner, J.C., 2008. Criticality Analysis of Assembly Misload in a PWR Burnup Credit Cask NUREG/CR-6955 ORNL/TM-2004/52. Oak Ridge National Laboratory, Oak Ridge, TN, USA.

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# Methodology



- Depletion on verified models is done with TRITON.
- Benchmarking the lattice models with other codes.
- The calculated spent fuel isotopics are placed into a cask modelled in KENO-V.a.
- Sampler is used to calculate the uncertainty in lattice  $k_{\infty}$

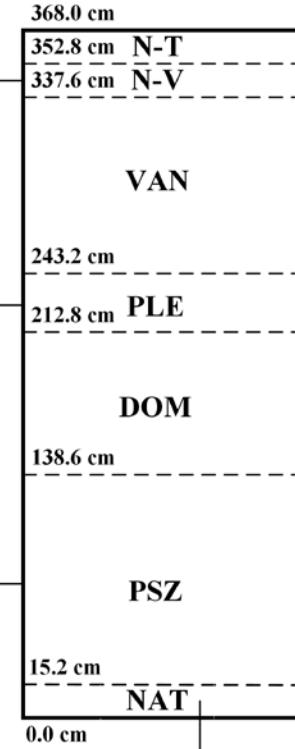
# BWR Data and Resources (Fensin)

- Model is based on GE 10x10 design
  - 74 UO<sub>2</sub> rods
  - 18 UO<sub>2</sub> + Gd<sub>2</sub>O<sub>3</sub> rods
  - 2 Large Water rods
- Axial enrichment heterogeneity
  - 7 axial layers with heterogenous enrichment and part length rods.
- Natural uranium is used at lattice lower and upper axial layers.

0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	V	0.71	V	0.71	0.71	V	0.71	V	0.71
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0.71	0.71	0.71	0.71	V			0.71	0.71	0.71
0.71	0.71	0.71			V	0.71	0.71	0.71	0.71
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0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	V	0.71	V	0.71	0.71	V	0.71	V	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71

1.60	2.80	3.20	3.95	3.95	3.95	3.95	3.95	3.95	2.80
2.80	E	3.20	E	3.60	3.95	E	4.40	E	3.95
3.20	3.20	4.40	4.40	4.90	4.40	4.40	4.40	4.40	4.90
3.95	E	4.40	4.90	6.00	3.95		4.90	E	4.90
3.95	3.60	4.90	6.00	3.95	E		4.90	4.90	4.90
3.95	3.95	4.40				E	4.90	4.90	4.90
3.95	E	4.40	6.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	E	4.40	6.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	E	4.40	6.00			4.90	4.90	4.90	4.90
2.80	3.95	4.90	4.90	4.90	4.90	4.90	4.90	4.90	3.20

1.60	2.80	3.20	3.95	3.95	3.95	3.95	3.95	3.95	2.80
2.80	2.80	3.20	3.95	3.60	3.95	3.95	4.40	3.95	3.95
3.20	3.20	4.40	4.40	4.90	4.40	4.40	4.40	4.40	4.90
3.95	3.95	4.40	4.90	8.00	3.95		4.90	4.90	4.90
3.95	3.60	4.90	8.00	3.95	4.90		4.90	4.90	4.90
3.95	3.95	4.40				4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
2.80	3.95	4.90	4.90	4.90	4.90	4.90	4.90	4.90	3.20



0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	V	0.71	V	0.71	E	V	E	V	0.71
0.71	0.71	E	0.71	E	0.71	E	0.71	E	0.71
0.71	V	0.71	E	0.71			0.71	V	0.71
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0.71	V	E			E	0.71	E	V	0.71
0.71	E	0.71	0.71	0.71	0.71	E	0.71	E	0.71
0.71	V	E	V	0.71	E	V	E	V	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71

1.60	2.80	3.20	3.95	3.95	3.95	3.95	3.95	3.95	2.80
2.80	V	3.20	V	3.60	3.95	V	4.40	V	3.95
3.20	3.20	4.40	4.40	4.90	4.40	4.40	4.40	4.40	4.90
3.95	V	4.40	4.90	6.00	3.95		4.90	V	4.90
3.95	3.60	4.90	6.00	3.95	V		4.90	4.90	4.90
3.95	3.95	4.40				V	4.90	4.90	4.90
3.95	V	4.40	6.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	V	4.40	6.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	V	4.40	6.00			4.90	4.90	4.90	4.90
2.80	3.95	4.90	4.90	4.90	4.90	4.90	4.90	4.90	3.20

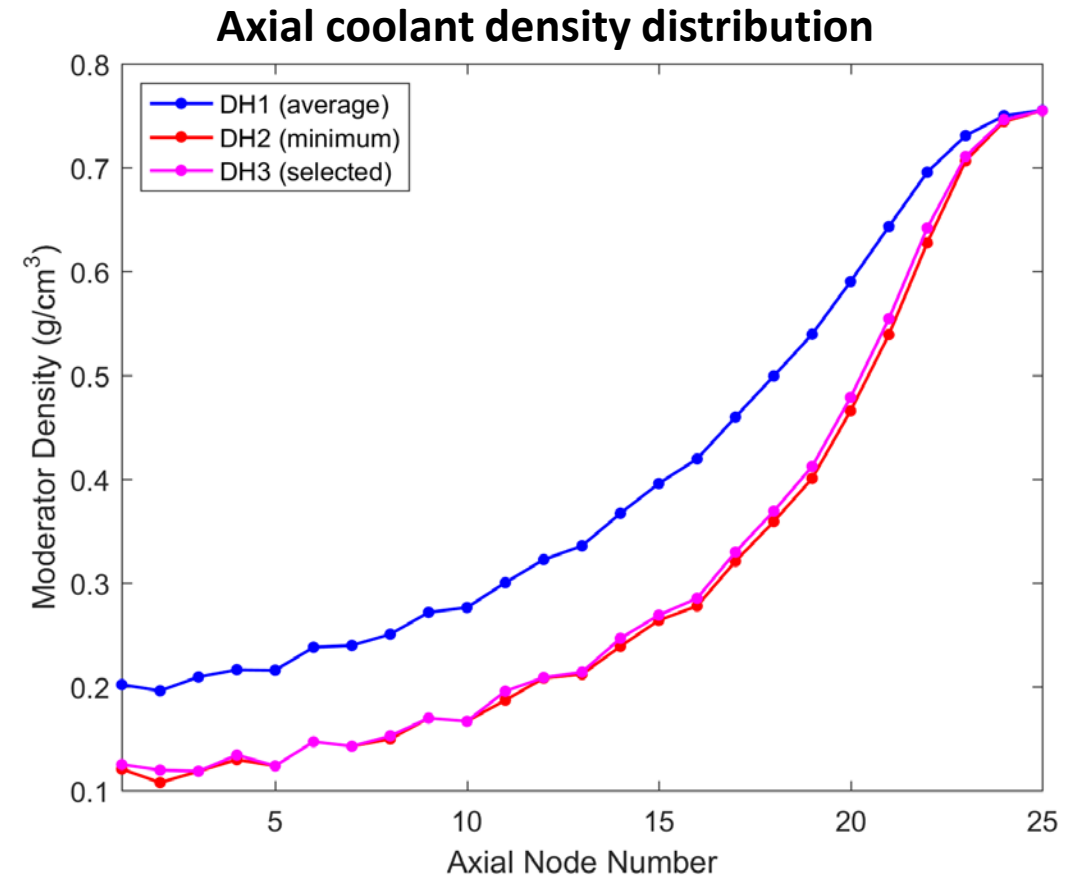
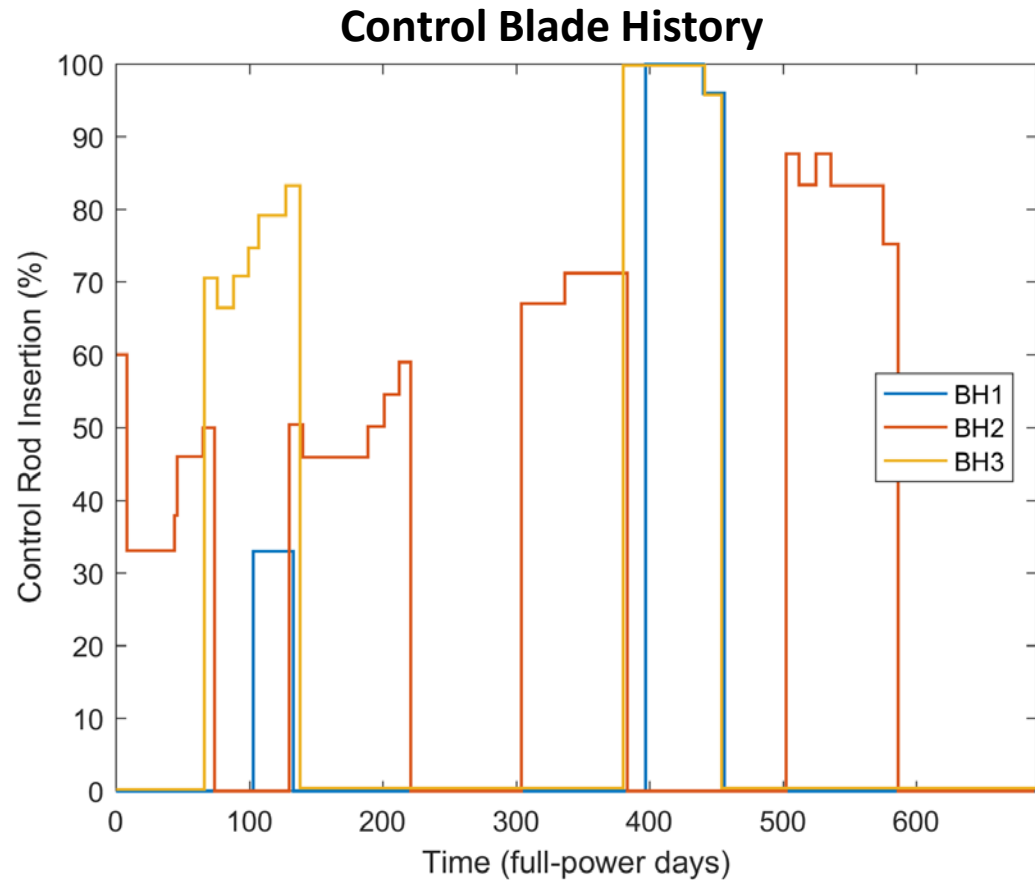
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2.80	2.80	3.20	3.95	3.60	3.95	3.95	4.40	3.95	3.95
3.20	3.20	4.40	4.40	4.90	4.40	4.40	4.40	4.40	4.90
3.95	3.95	4.40	4.90	8.00	3.95		4.90	4.90	4.90
3.95	3.60	4.90	6.00	3.95	4.90		4.90	4.90	4.90
3.95	3.95	4.40				4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
3.95	4.40	4.40	4.90	4.90	4.90	4.90	4.90	4.90	4.90
3.95	3.95	4.40	8.00			4.90	4.90	4.90	4.90
2.80	3.95	4.90	4.90	4.90	4.90	4.90	4.90	4.90	3.20

0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71			0.71	0.71	0.71
0.71	0.71	0.71					0.71	0.71	0.71
0.71	0.71	0.71			0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71			0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71
0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71	0.71

4.24	UO <sub>2</sub> Rod
4.40 8.00	UO <sub>2</sub> + Gd <sub>2</sub> O <sub>3</sub> Rod
V	Vanished location
E	Plenum tip
	Water Rod

Fensin, M.L., 2004. Optimum Boiling Water Reactor Fuel Design Strategies to Enhance Reactor Shutdown by the Standby Liquid Control System, Master Thesis. University of Florida, USA.

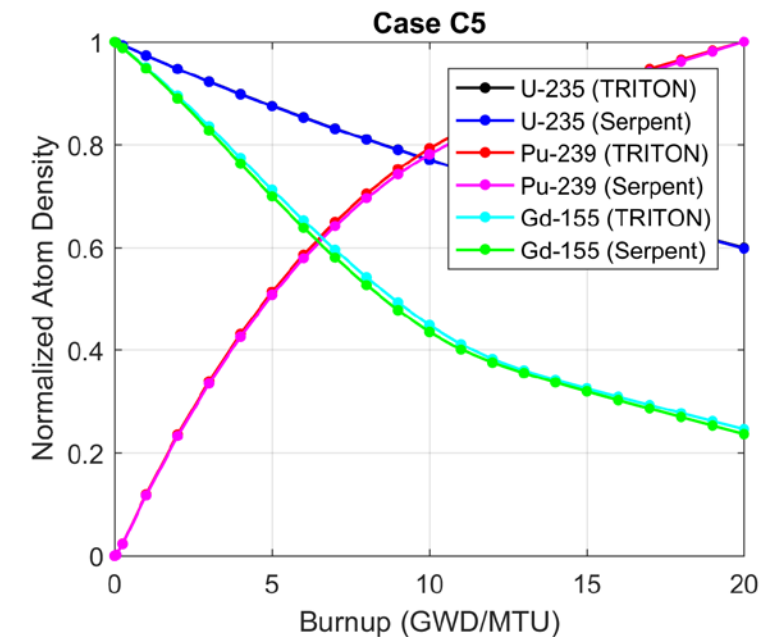
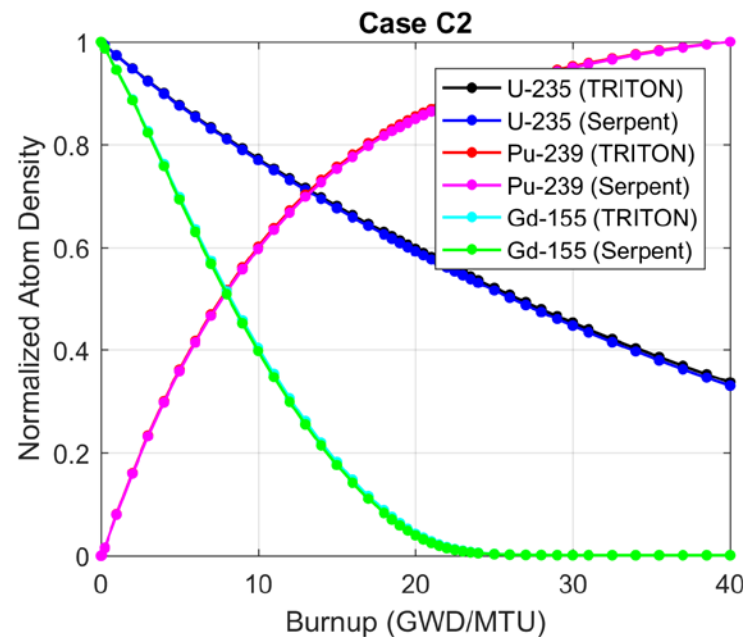
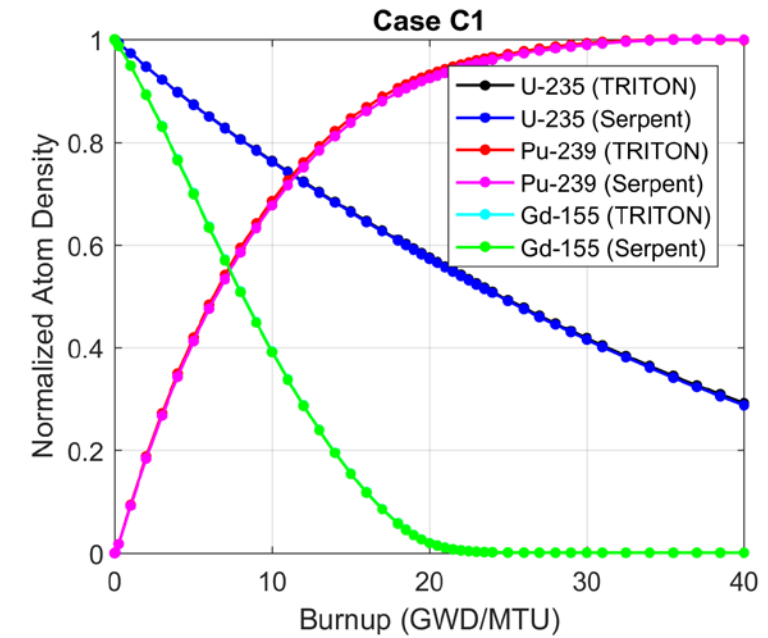
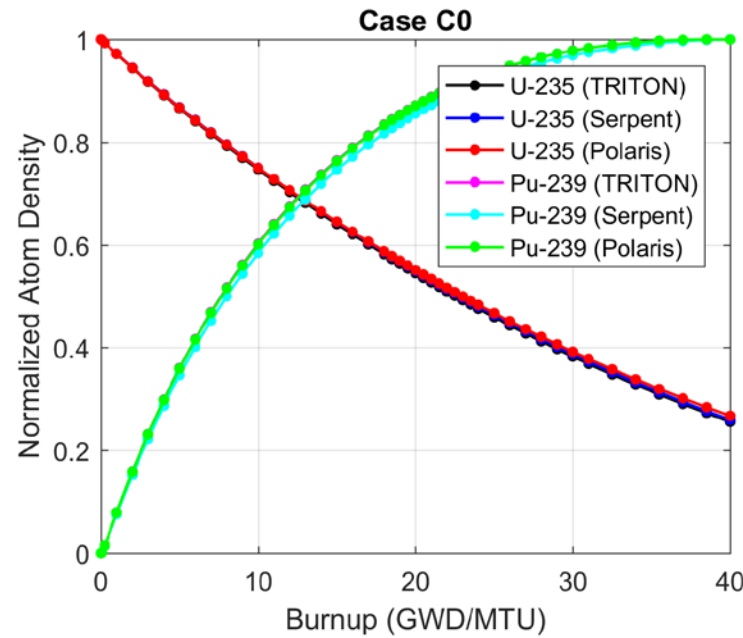
# BWR Data and Resources (Marshall, ORNL)





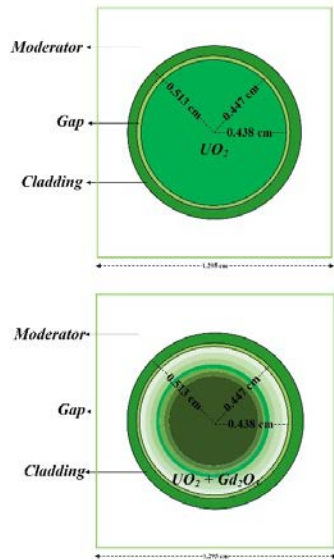
# Model Benchmarking

- Relevant isotopic concentration is benchmarked using different codes
- Different 2D and 3D cases are considered.
- Good agreement is observed

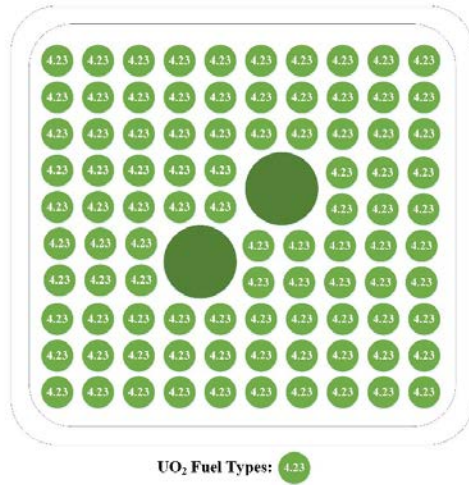


# BWR 2D Cases (T-DEPL)

CS0: UO<sub>2</sub> and Gadolinium pin-cell

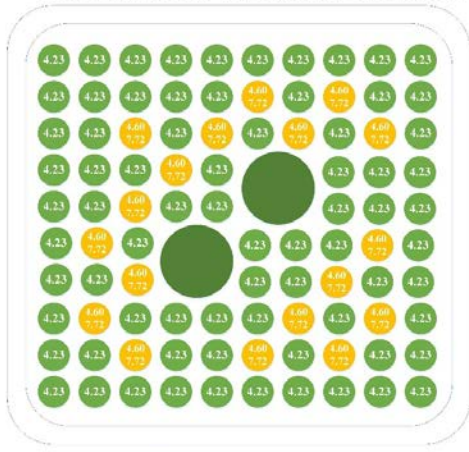


C0: UO<sub>2</sub>-only lattice



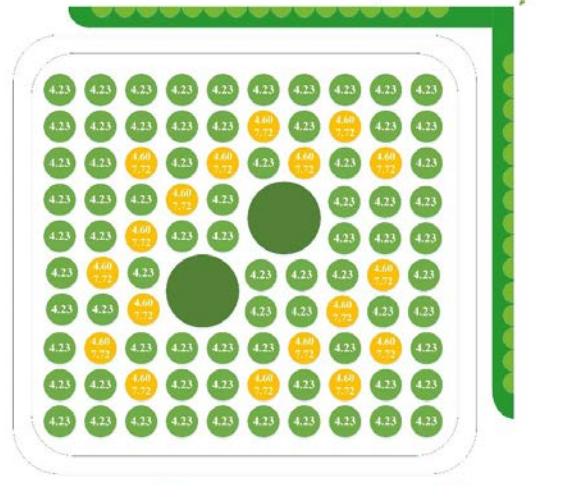
UO<sub>2</sub> Fuel Types: 4.23

C1: UO<sub>2</sub> and Gad with uniform enrichment



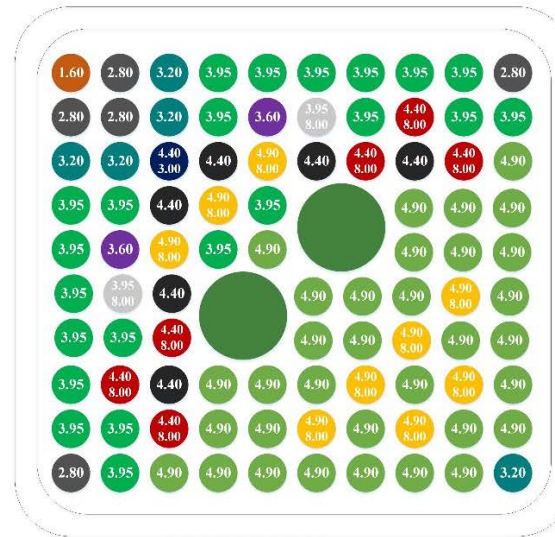
UO<sub>2</sub> Fuel Types: 4.23 UO<sub>2</sub> + Gd<sub>2</sub>O<sub>3</sub> Fuel Types: 4.60

C2: C1 with Control blade fully inserted



UO<sub>2</sub> Fuel Types: 4.23 UO<sub>2</sub> + Gd<sub>2</sub>O<sub>3</sub> Fuel Types: 4.60

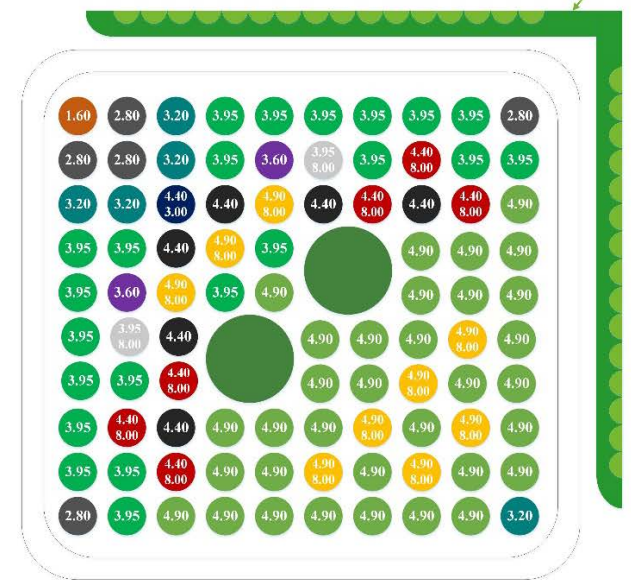
C3: UO<sub>2</sub> and Gad with variable radial enrichment



UO<sub>2</sub> Fuel Types: 1.60 2.80 3.20 3.60 3.95 4.40 4.90

UO<sub>2</sub> + Gd<sub>2</sub>O<sub>3</sub> Fuel Types: 3.95 4.40 4.40 4.90 8.00 3.00 8.00

C4: C3 with control rod fully inserted

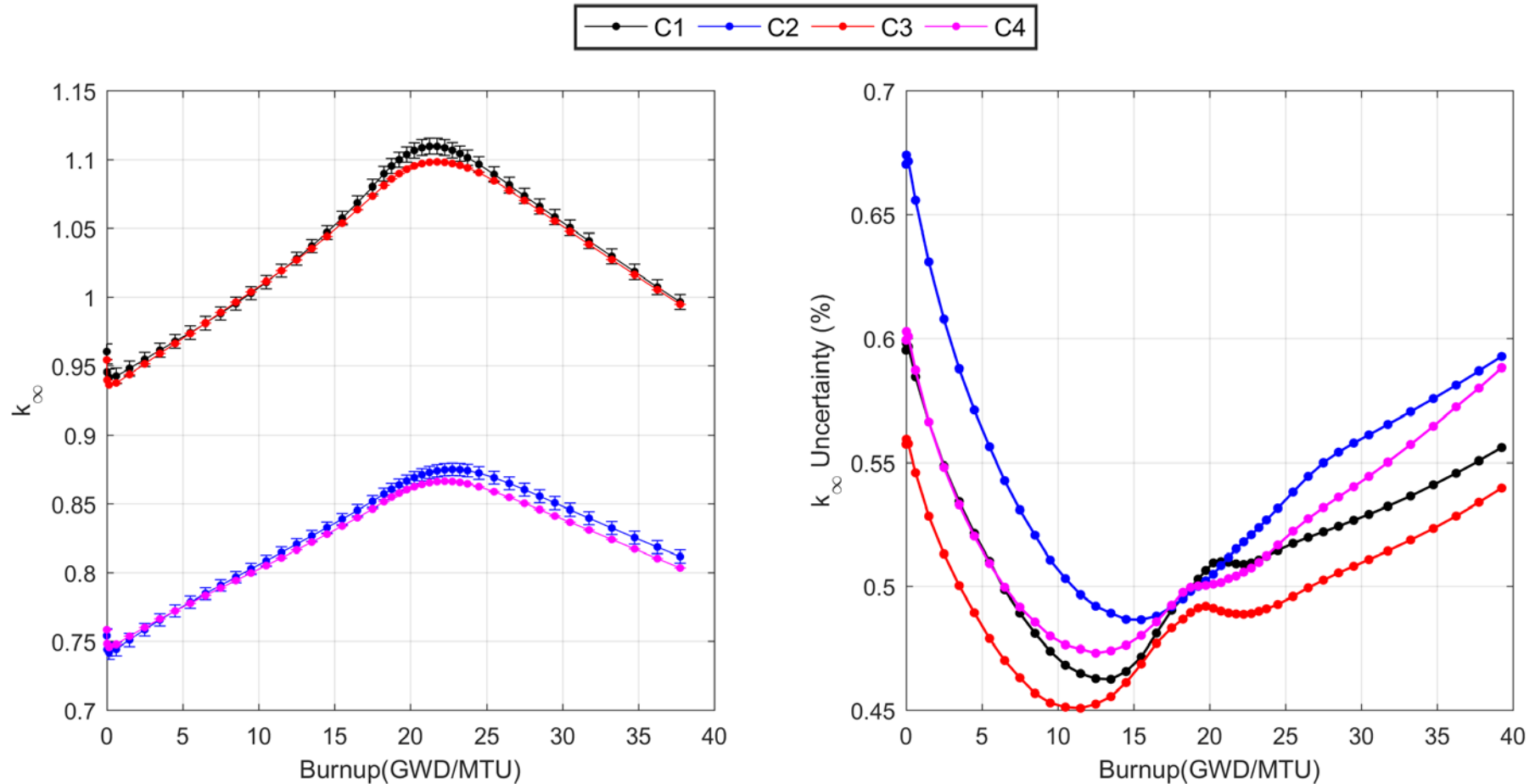


UO<sub>2</sub> Fuel Types: 1.60 2.80 3.20 3.60 3.95 4.40 4.90

UO<sub>2</sub> + Gd<sub>2</sub>O<sub>3</sub> Fuel Types: 3.95 4.40 4.40 4.90 8.00 3.00 8.00

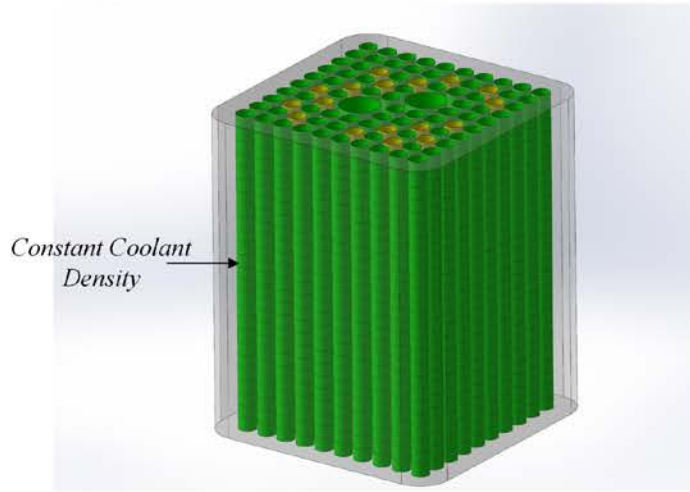
M. I. Radaideh, D. Price, T. Kozlowski, "Uncertainty quantification of BWR criticality safety simulations," Proceedings of Physics of Reactors (PHYSOR-2018), Cancun, Mexico, April 22-26, pp. 2866-2877 (2018).

# 2D Results ( $k_{\infty}$ vs Burnup)



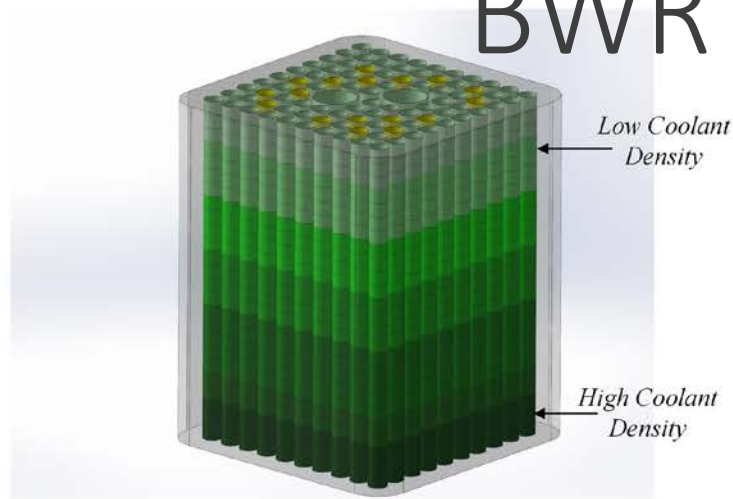
# BWR 3D Cases (T5-DEPL)

**C5:** 3D model with core-averaged axial coolant density.



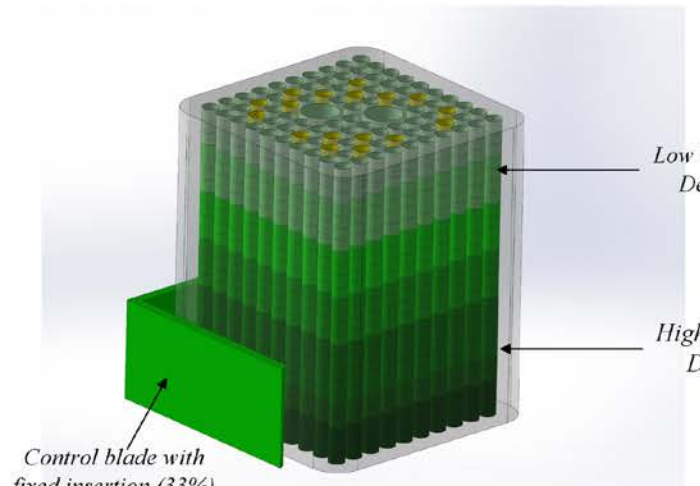
(a)

**C6:** C5 model with non-uniform axial coolant density.



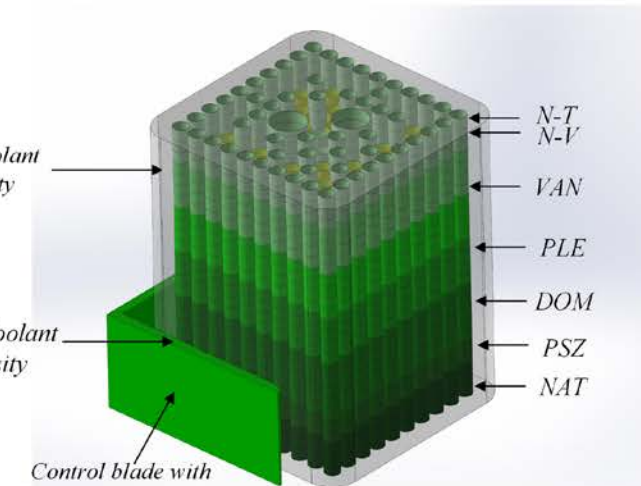
(b)

**C7:** C6 model with partial control rod insertion (i.e. 33%)



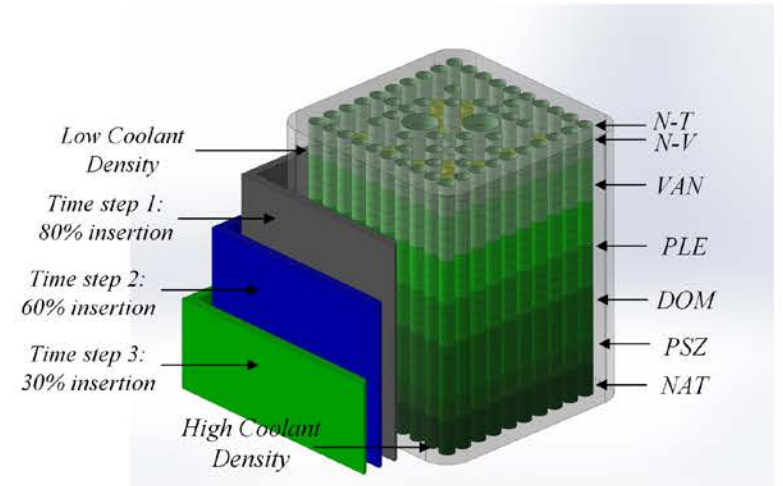
(c)

**C8:** C7 model with variable axial enrichment and part-length rods (See Fig. 1)



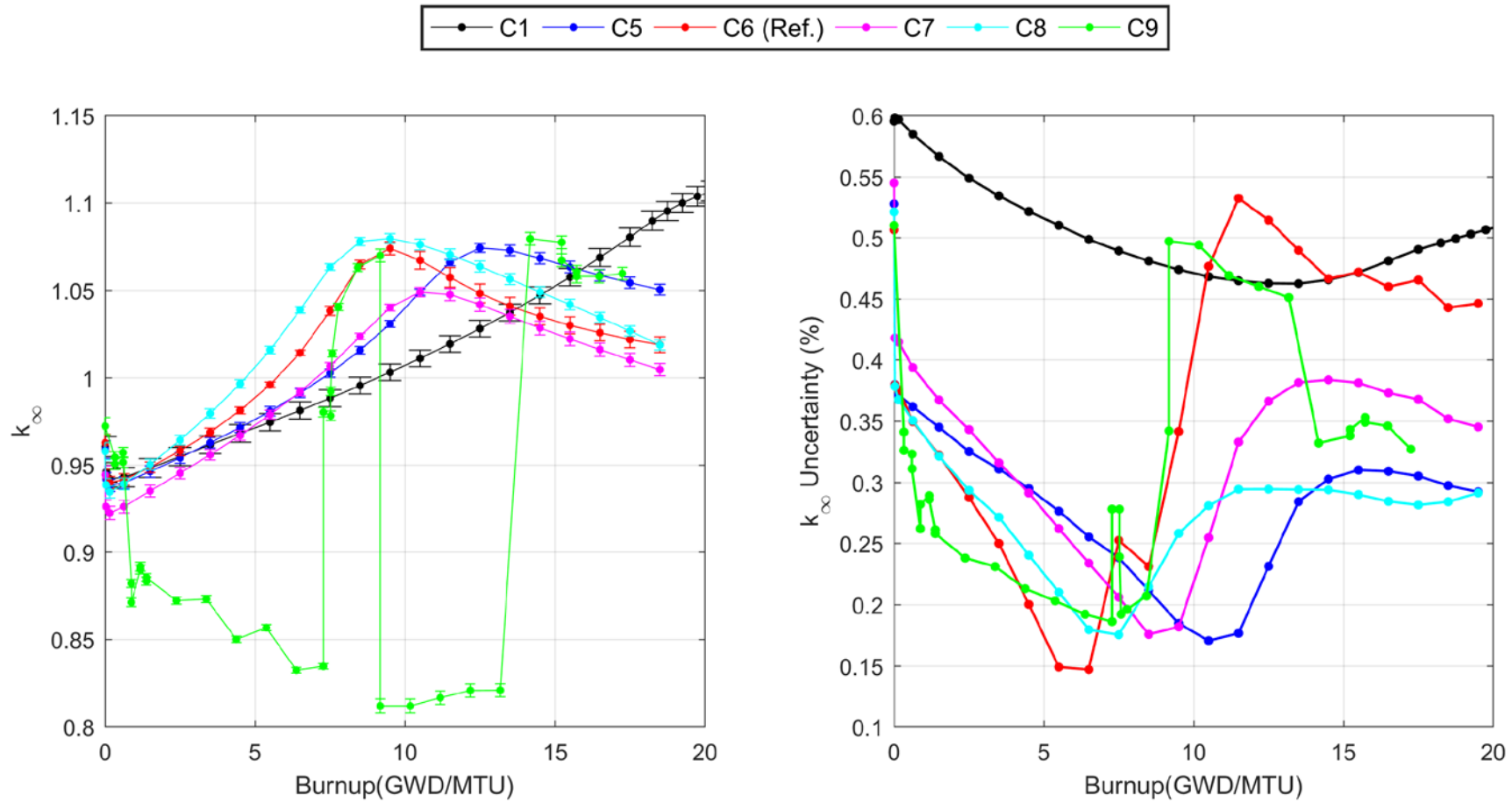
(d)

**C9:** C8 model with control rod movement during depletion



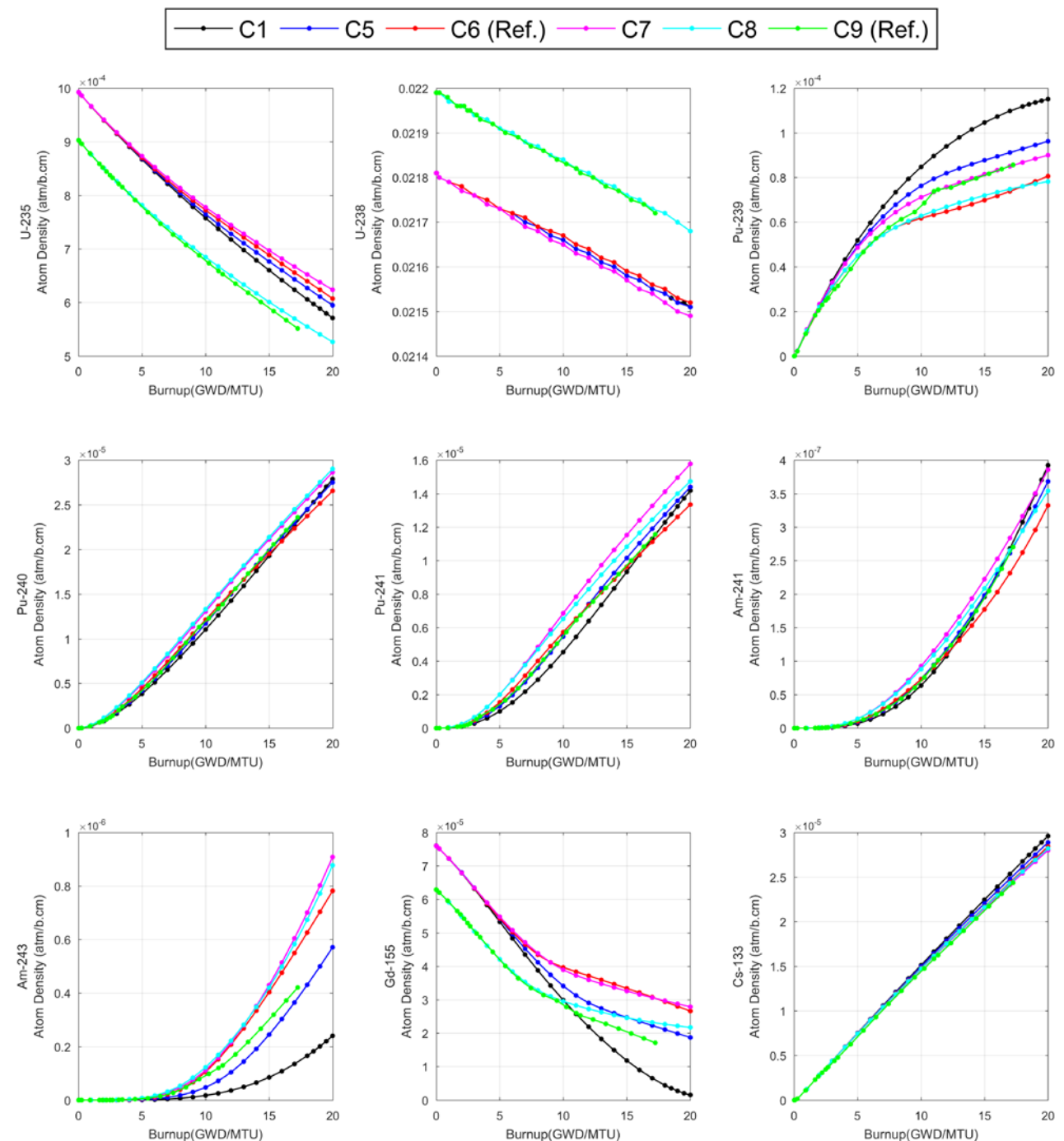
(e)

# 3D Results ( $k_{\infty}$ vs Burnup)



# 3D Results: Isotopic Inventory

- The 2D case **C1** is considered the reference case to which other cases are compared.
- Initial **U-235** and **U-238** amounts differ for **C8** and **C9** compared to other cases due to the vanished locations and axial heterogeneity.
- **3D cases deplete Gd-155 slowly** due to the axial burnup profile at the boundaries.
- **Control rod movement (C9)** enhances Pu-239 breeding due to the spectrum hardening.
- The 2D case reaches the reactivity peak **faster** due to the uniform depletion.



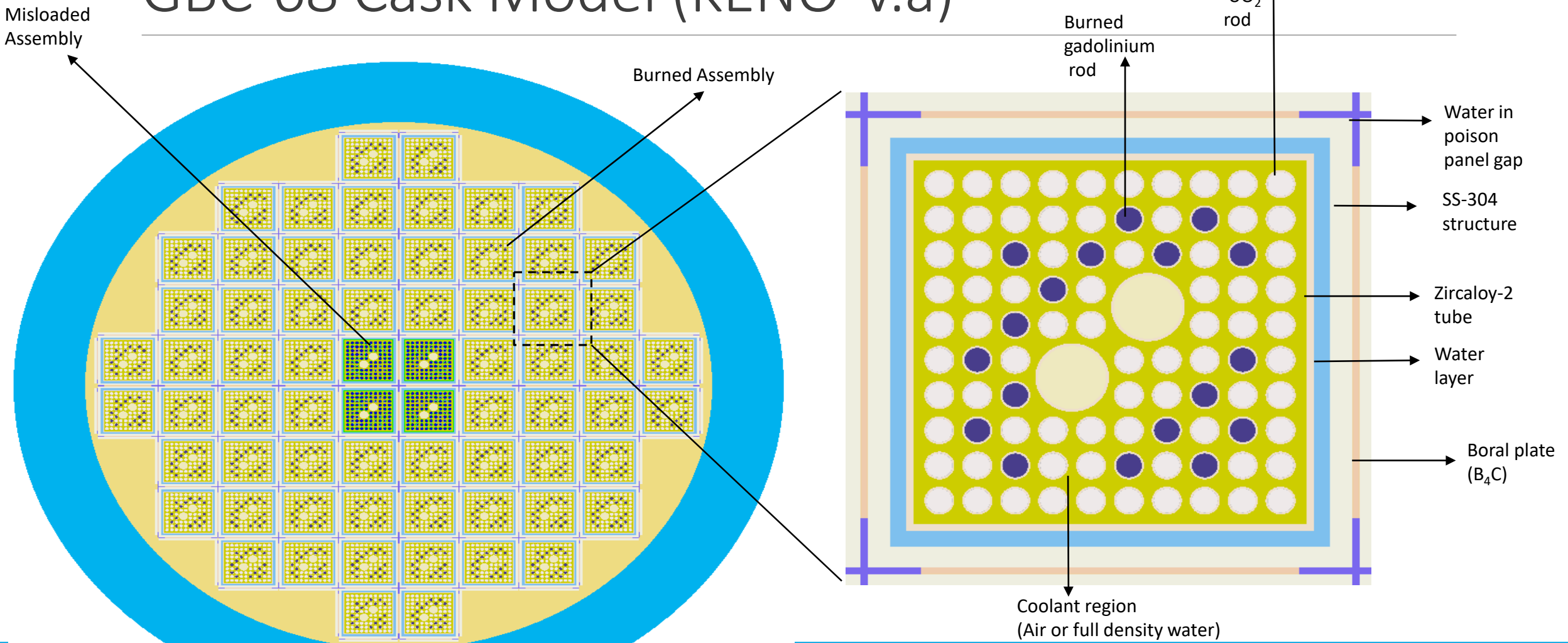
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Note: the cask was assumed flooded by full density water to simulate accident scenarios

# GBC-68 Cask Model (KENO-V.a)





# Cask Criticality

- Results from fuel discharged at 40GWD/MTU
- Rodded cases yield more critical cask
- Heterogeneous enrichment has little effect on cask criticality
- Cask criticality results for C7-C9 are in progress

Case Number	Description	$k_{\text{eff}}$
C0	Pure UO <sub>2</sub>	0.65864
C1	Homo	0.67702
C2	Homo, CR	0.72709
C3	Hetero	0.67792
C4	Hetero, CR	0.72966
C5	Constant void	0.71671
C6	Void distribution*	0.65610

All statistical uncertainty is within 10 pcm

\*based on DH1, the void distribution based on the average throughout the core

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# Nuclear Data Sensitivity (Cask $k_{eff}$ ) via TSUNAMI-3D

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Case C0

Nuclide	Reaction1; Reaction 2	$\Delta k/k$
U-238	n, gamma; n, gamma	0.220
Pu-239	fission; fission	0.207
U-235	nubar; nubar	0.151
Pu-239	fission; n, gamma	0.131
Pu-239	n, gamma; n, gamma	0.095

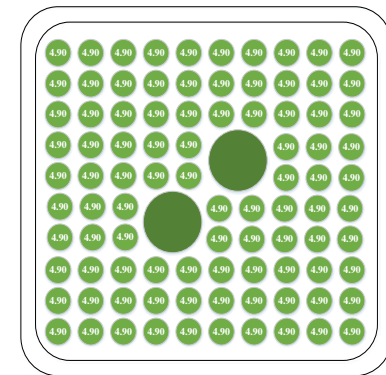
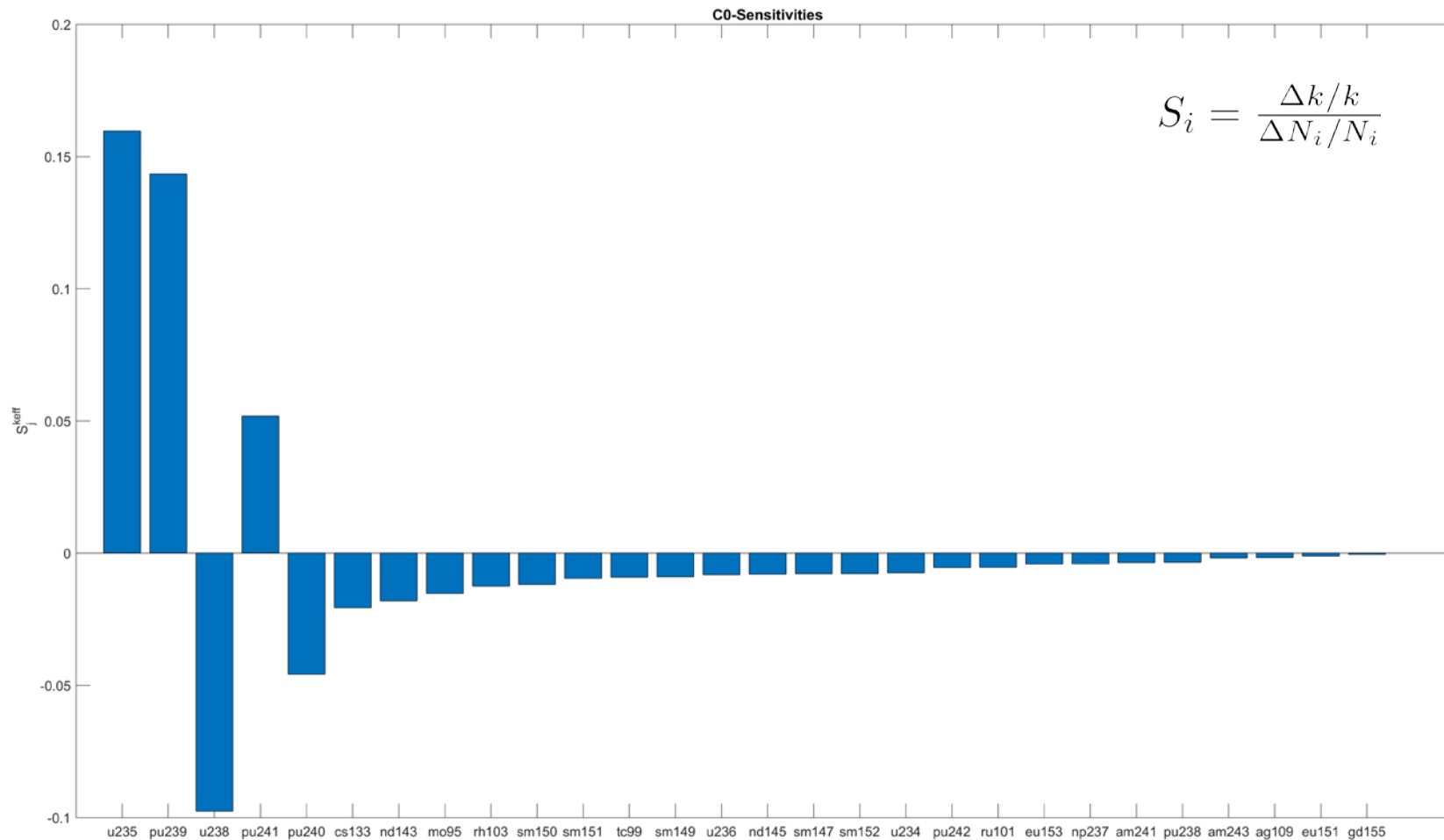
Case C1

Nuclide	Reaction1; Reaction 2	$\Delta k/k$
U-238	n, gamma; n, gamma	0.209
Pu-239	fission; fission	0.193
U-235	nubar; nubar	0.159
Pu-239	fission; n, gamma	0.128
Pu-239	n, gamma; n, gamma	0.096

Case C2

Nuclide	Reaction1; Reaction 2	$\Delta k/k$
Pu-239	fission; fission	0.201
U-238	n, gamma; n, gamma	0.190
U-235	nubar; nubar	0.142
Pu-239	fission; n, gamma	0.142
Pu-239	n, gamma; n, gamma	0.114

# Cask $k_{\text{eff}}$ Isotopic Sensitivities based on C0 depletion (EOL)

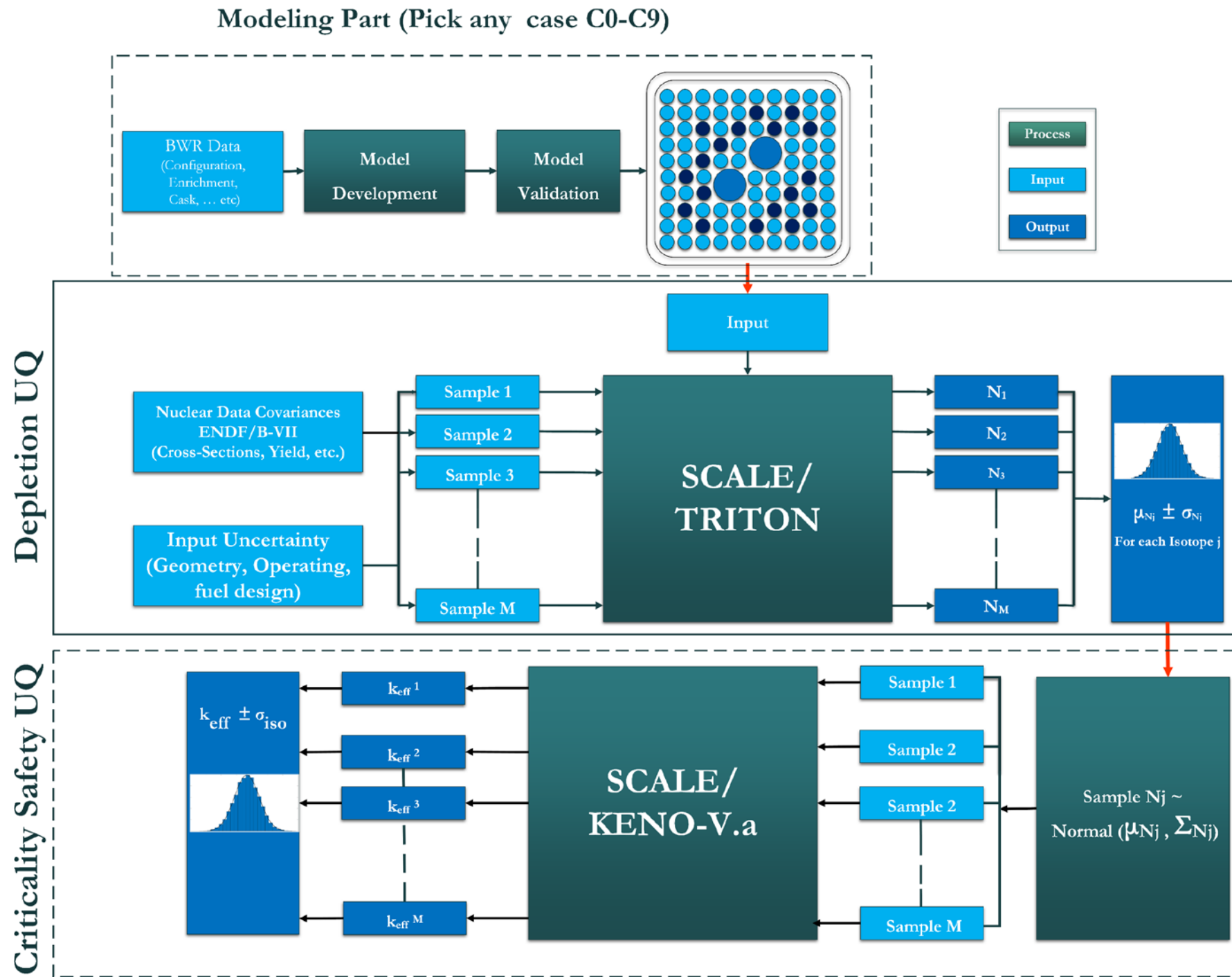


# Contents

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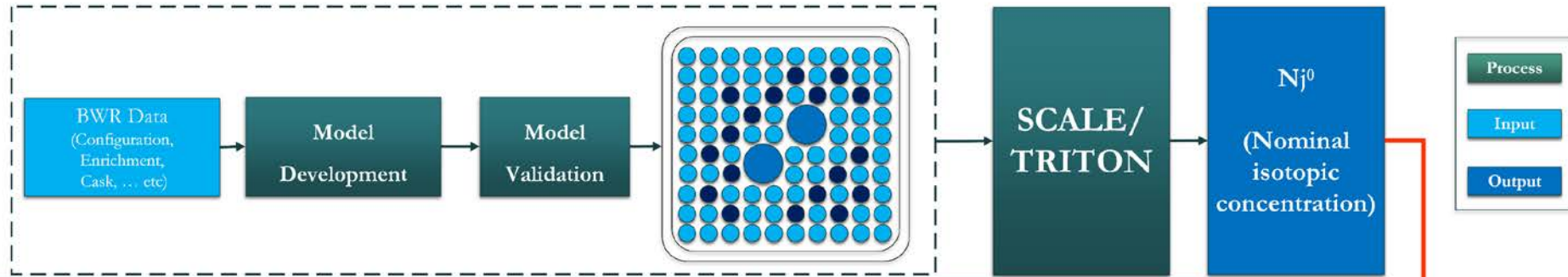
- Background
- Advanced BWR Depletion Cases (T-Depl and T5-Depl)
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- Sensitivity Analysis (TSUNAMI-3D)
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# Computational VS Data-driven (Computational method)

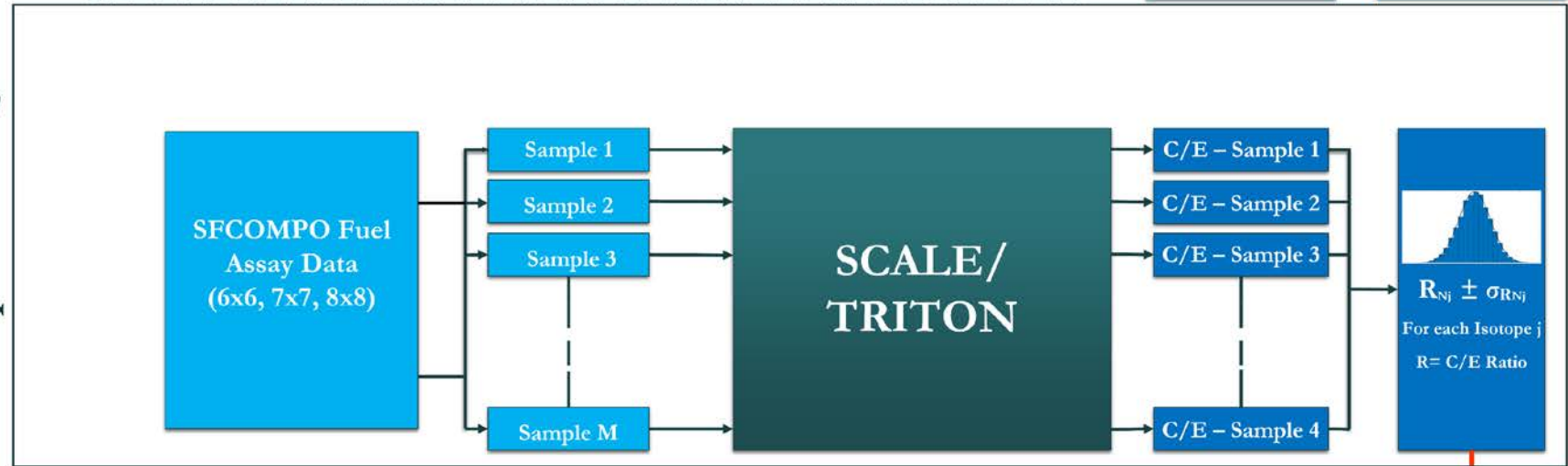


# Computational VS Data-driven (Data method)

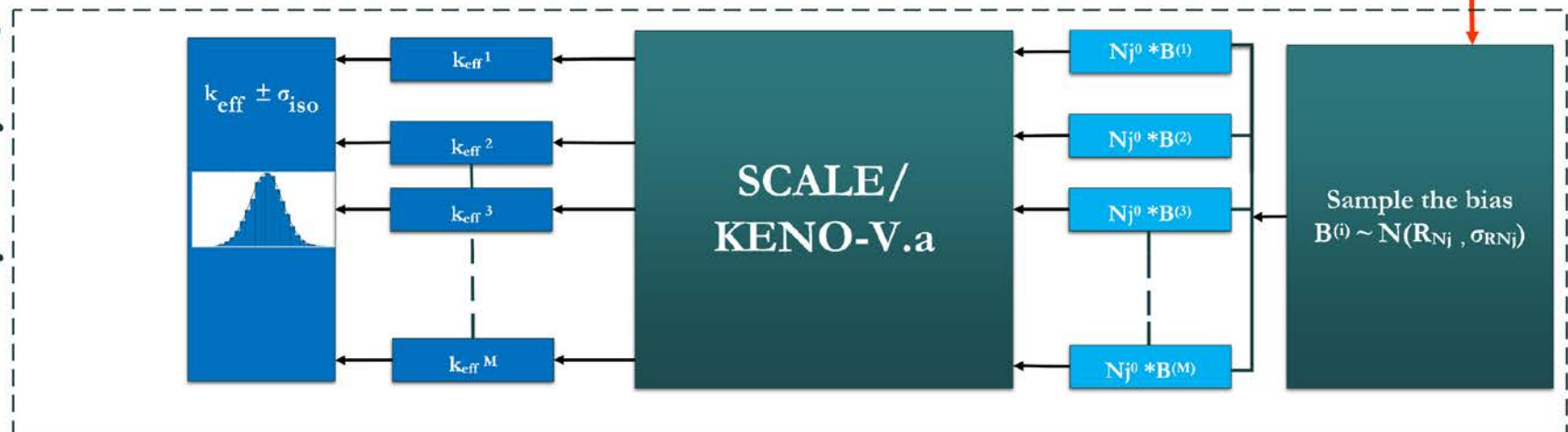
## Modeling Part (Pick any case C0-C9)



## Depletion UQ



## Criticality Safety UQ



I. C. Gauld, "Strategies for application of isotopic uncertainties in burnup credit," ORNL/TM-2001/257, Oak Ridge National Laboratory, Oak Ridge, Tennessee (2003).

[3] S. M. Bowman, "SCALE 6: comprehensive nuclear safety analysis code system," Nuclear Technology, 174(2), pp. 126-148 (2011)

[8] G. Ias, H. Liljenfeldt, "Decay heat uncertainty for BWR used fuel due to modeling and nuclear data uncertainties," Nuclear Engineering and Design, 319, 176-184 (2017).

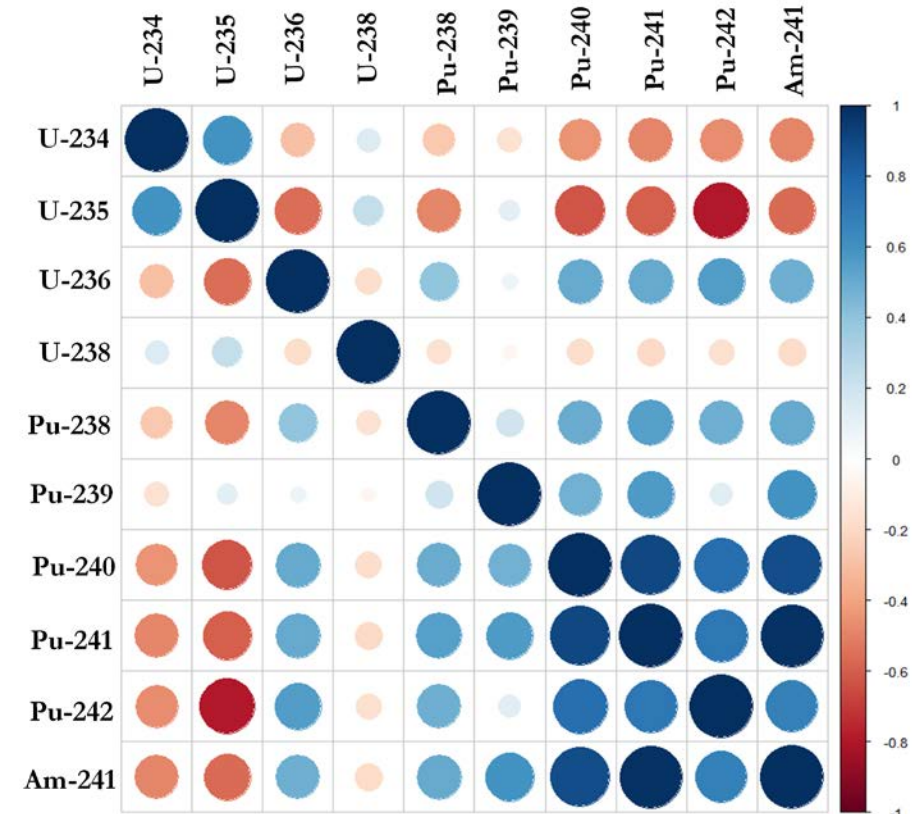
[9] A. Hofer, T. Ivanova, B. Rearden, D. Mennerdahl, O. Buss, "Proposal for Benchmark Phase IV Role of Integral Experiment Covariance Data for Criticality Safety Validation," Working Party on Nuclear Criticality Safety, EG UACSA, OECD/NEA (2014).

# Computational-driven Approach

## Input parameters' uncertainty for criticality safety applications

Parameter	1- $\sigma$ (%)	Source
<i>Geometry</i>		
Pellet radius	0.14%	[9, 10]
Clad Inner Diameter	0.43%	[9, 10]
Clad Outer Diameter	0.46%	[9, 10]
<i>Material</i>		
U-235 wt%	0.60%	[8]
Gd <sub>2</sub> O <sub>3</sub> wt%	1.67%	[8]
UO <sub>2</sub> Density	0.13%	[9, 10]
<i>Operating</i>		
Specific Power	1.67%	[8, 11, 12]
Coolant Density	3.33%	[8, 11, 12]
Fuel Temperature	3.33%	[8, 11, 12]
<i>Nuclear Data</i>		
Neutron Cross-sections	56group-COV	[3]
Fission Yield	56group-COV	[3]
Decay Data	56group-COV	[3]

## Correlation matrix between actinides based on case C1



[10] NEA Nuclear Science Committee, "International Handbook of Evaluated Criticality Safety Benchmarks Experiments," OECD Nuclear Energy Agency (1999).

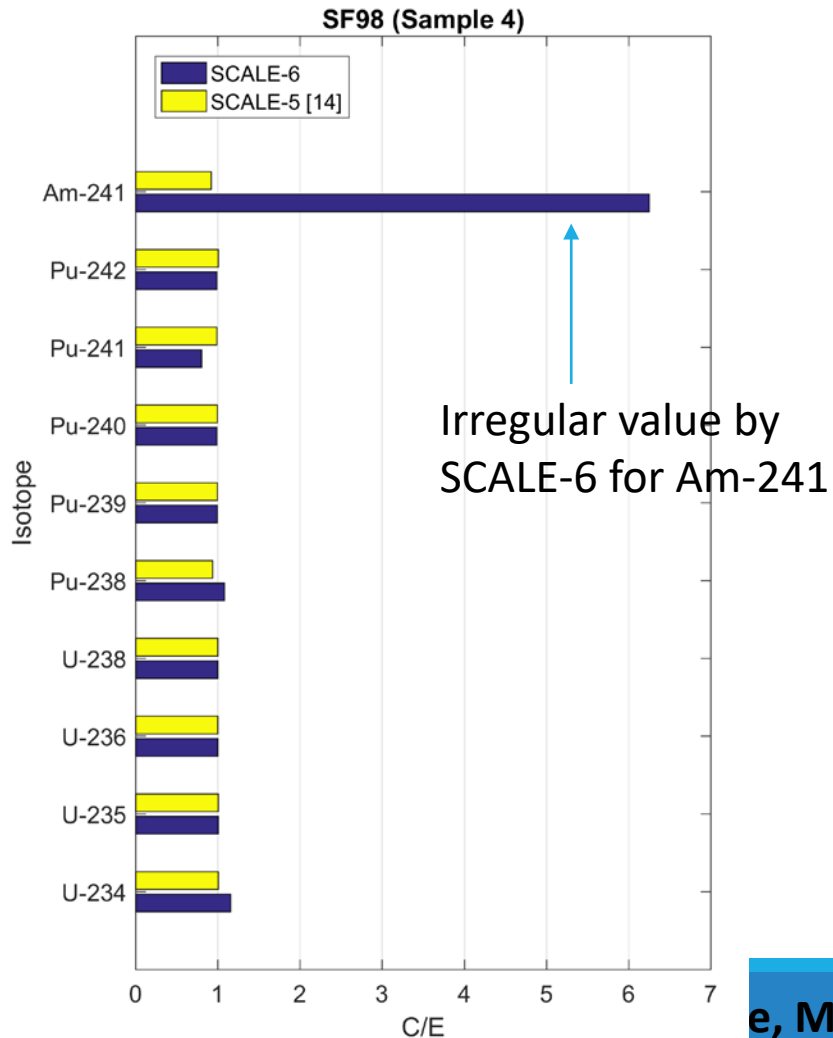
[11] G. M. Grandi, J. A. Borkowski, "Benchmark of SIMULATE-3K against the Frigg loop stability experiments," In: CD Proceedings of Advances in Nuclear Fuel Management III, Hilton Head Island, USA (2003).

[12] M. Kruners, G. Grandi, M. Carlsson, "PWR transient xenon modeling and analysis using Studsvik CMS," In: Proceeding of LWR Fuel Performance/TopFuel/WRFPM, Orlando, USA (2010).



# Data-driven Approach

$\bar{R}_n$ : mean of the bias (C/E)  
 $\sigma_{R_n}$ : standard deviation of the bias  
 $N_s^n$ : number of experimental samples used

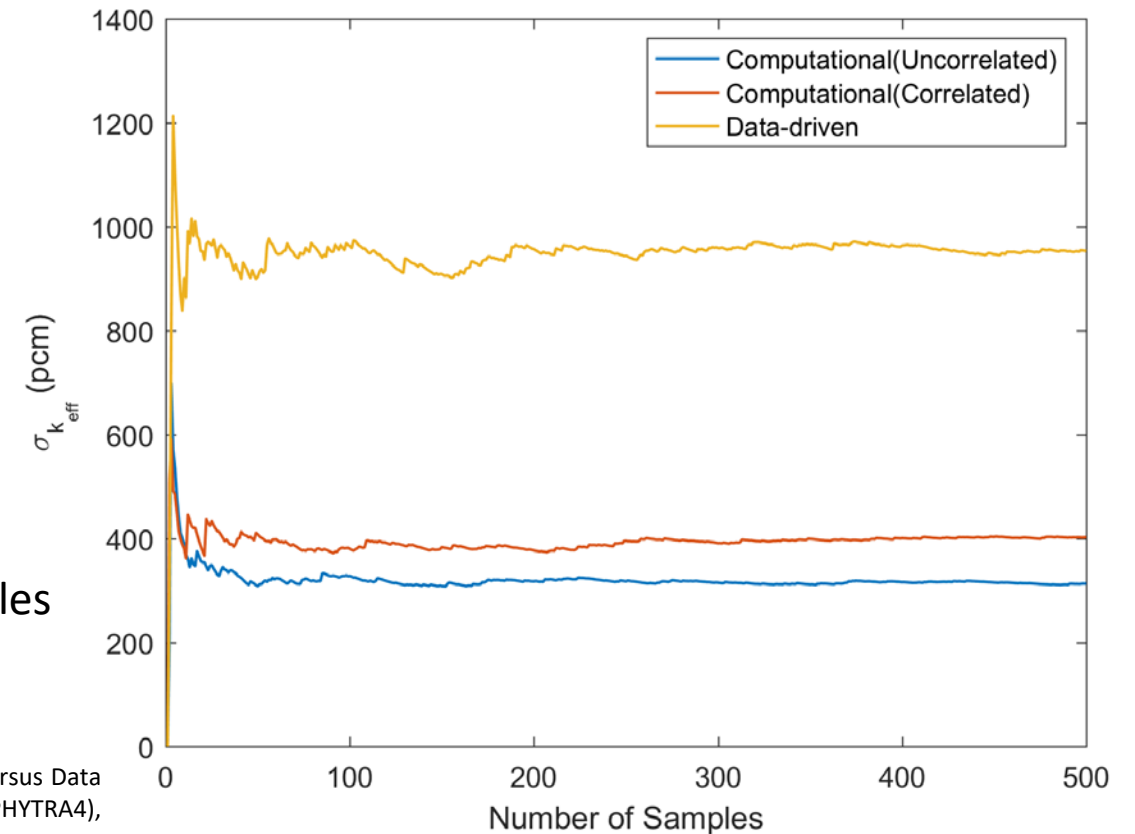


Nuclide	Geometry	$\bar{R}_n$	$\sigma_{R_n}$	$N_s^n$
U-234	8x8, 7x7	1.077	0.079	20
U-235	8x8, 7x7, 6x6	0.992	0.055	32
U-236	8x8, 7x7, 6x6	0.979	0.020	32
U-237	8x8, 7x7, 6x6	0.999	0.005	32
Pu-238	8x8, 7x7, 6x6	0.968	0.101	32
Pu-239	8x8, 7x7, 6x6	1.006	0.052	32
Pu-240	8x8, 7x7, 6x6	0.997	0.037	32
Pu-241	8x8, 7x7, 6x6	0.949	0.102	32
Pu-242	8x8, 7x7, 6x6	1.008	0.062	32
Am-241	8x8, 7x7	1.087	0.121	20

# Final cask $k_{eff}$ Uncertainty due to isotopic Uncertainty

Method	Nominal $k_{eff}$	$\overline{k_{eff}}$	1- $\sigma$ (%)	$\sigma_{k_{eff}}$ (pcm)
Computational (Uncorrelated)	0.79747	0.79762	0.39	314
Computational (Correlated)	0.79747	0.79812	0.50	403
Data-driven	0.79747	0.79601	1.20	953

The calculations were done using KENO-V.a + Sampler for 500 samples



M. I. Radaideh, D. Price, T. Kozlowski, " On Uncertainty Quantification of Isotopic Uncertainties Using Computational Versus Data Driven Approaches ," The 4th International Conference on Physics and Technology of Reactors and Applications (PHYTRA4), Marrakesh, Morocco, September 17-19 (2018).

# Contents

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- Background
- Advanced BWR Depletion Cases (T-Depl and T5-Depl)
- Cask Criticality Calculations (KENO-V.a)
- Sensitivity Analysis (TSUNAMI-3D)
- BWR Isotopic Uncertainty Quantification (Sampler)
- Summary**

# Summary

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- Advanced BWR modelling is necessary to capture the complexities associated with the BWR design, which in turn yield an accurate criticality safety calculations.
- 2D modelling shows minimal effects of radial enrichment averaging.
- 3D models show different behaviour for U-235 and Gd-155 depletion, and Pu-239 breeding.
- In general, the uncertainty due to cross-section covariances decreases during the cycle
- The data driven method for performing UQ on the cask yields a higher uncertainty (**additional enchantment of the database will be done in future**).
- Correlation between isotopes tends to increase the  $k_{\text{eff}}$  uncertainty due to isotopic uncertainty.
- **Our future work will focus on combining the computational and data-driven approaches into one hybrid approach through quantifying the code bias.**
- Even when flooded, the BWR cask remains subcritical in all cases analysed.

# Thank you!

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- **Our publications for more info**

- M. I. Radaideh, D. Price, T. Kozlowski, "Criticality and uncertainty assessment of assembly misloading in BWR transportation cask," *Annals of Nuclear Energy*, 113, pp. 1-14 (2018).
- M. I. Radaideh, D. Price, T. Kozlowski, "Uncertainty quantification of BWR criticality safety simulations ," *Proceedings of Physics of Reactors (PHYSOR-2018)*, Cancun, Mexico, April 22-26, pp. 2866-2877 (2018).
- M. I. Radaideh, D. Price, T. Kozlowski, " On Uncertainty Quantification of Isotopic Uncertainties Using Computational Versus Data Driven Approaches ," *The 4th International Conference on Physics and Technology of Reactors and Applications (PHYTRA4)*, Marrakesh, Morocco, September 17-19 (2018).

- **To come soon**

- M. I. Radaideh, D. Price, D. O'Grady, T. Kozlowski, "Advanced BWR Criticality Safety, Part I: Model Development, Model Benchmarking, , and Depletion with Uncertainty analysis," to be submitted to *Nuclear Engineering and Design* (2019).
- D. Price, M. I. Radaideh, D. O'Grady, T. Kozlowski, "Advanced BWR Criticality Safety, Part II: Cask Criticality, Burnup Credit, Sensitivity, and Uncertainty Analyses," to be submitted to *Nuclear Engineering and Design* (2019).