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ISO/CD 18629-41

**Industrial automation system and integration -- Process specification language:
Part 41: Definitional extension : Activity extensions**

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ABSTRACT:

This document provides definitions written in the language of ISO 18629 for concepts related to activity extensions in the process specification language. The process specification language is aimed at structuring the semantic concepts intrinsic to the capture and exchange of process information related to discrete manufacturing.

KEYWORDS:

Manufacturing, manufacturing process, process information, process language, semantics, ontology.

COMMENTS TO READER:

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

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The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this part of ISO 18629 may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 18629-41 was prepared by Technical Committee ISO/TC 184, *Industrial automation systems*, Subcommittee SC 4, *Industrial data*.

A complete list of parts of ISO 18629 is available from the Internet:

http://www.tc184-sc4.org/titles/PSL_titles.rtf

Annexes A and B form a normative part of this part of ISO 18629, annex C is for information only.

Introduction

ISO 18629 is an International Standard for the computer-interpretable exchange of information related to manufacturing processes. Taken together, all the parts contained in the ISO 18629 Standard provide a generic language for describing a manufacturing process throughout the entire production process within the same industrial company or across several industrial sectors or companies, independently from any particular representation model. The nature of this language makes it suitable for sharing process specifications and properties related to manufacturing during all the stages of a production process.

This part provides a description of the definitional extensions of the language related to activity extensions defined within the International Standard.

This part of ISO 18629 and all other parts in ISO 18629 are independent of any specific process representation model used in a given application. Collectively, they provide a structural framework for improving the interoperability of these applications.

Industrial automation systems and integration — Process specification language — Part 41: Definitional extension: Activity extension

1 Scope of ISO 18629-41

Part 41 of ISO 18629 provides a specification of non-primitive concepts of the language, using a set of definitions written in the language of ISO 18629. These definitions provide an axiomatization of the semantics for terminology in ISO 18629-41.

The following is within the scope of Part 41 of ISO 18629:

- definitions of concepts specified in ISO 18629-11 and ISO 18629-12 that are independent of state and time relations.

The following is outside the scope of Part 41 of ISO 18629:

- definitions of state and time-related concepts specified in ISO 18629-11 and ISO 18629-12.

2 Normative References

The following standards contain provisions that, through reference in this text, constitute provisions for this part of ISO 18629. At the time of publication the editions indicated were valid. All standards are subject to revision, and parties to agreements based on this part of ISO 18629 are encouraged to investigate the possibility of applying the most recent editions of the standards indicated below. Members of IEC and ISO maintain registers of currently valid International Standards.

ISO/IEC 8824-1:1995, *Information technology - Open systems interconnection - Abstract syntax notation one (ASN.1) - Part 1: Specification of basic notation*.

ISO 10303-1: 1994, *Industrial automation systems and integration - Product data representation and exchange - Part 1: Overview and fundamental principles*.

ISO 15531-1: 2003, *Industrial automation systems and integration - Industrial manufacturing management data - Part 1: General overview*.

ISO 18629-1: —¹⁾ *Industrial automation systems and integration – Process specification language – Overview and basic principles*.

ISO 18629-11: —²⁾ *Industrial automation systems and integration – Process specification language – PSL-core*

¹⁾ To be published

²⁾ To be published

ISO 18629-12: —³⁾ *Industrial automation systems and integration – Process specification language – PSL Outercore*

3 Terms, definitions, and abbreviations

3.1 Terms defined in ISO 10303-1

This part of ISO 18629 makes use of the following terms defined in ISO 10303-1:

- data;
- information;
- product.

3.2 Terms defined in ISO 15331-1

This part of ISO 18629 makes use of the following terms defined in ISO 15331-1:

- continuous process;
- discrete manufacturing;
- industrial process;
- manufacturing;
- manufacturing process;
- process;
- resource.

3.3 Terms defined in ISO 18629-1

- axiom;
- axiomatization;
- defined lexicon;
- definitional extension
- extension
- grammar;

³⁾ To be published

- language;
- model;
- ontology;
- primitive concept;
- primitive lexicon;

3.4 Abbreviations

- **KIF** Knowledge Interchange Language;

4 Organization of ISO 18629-41

4.1 Introduction

This clause specifies the fundamental theories of which ISO 18629-41 is composed.

4.2 Extensions in ISO 18629-41

The fundamental theories that are part of ISO 18629-41 are:

- Deterministic Activities: Permuting Branch Structure;
- Non-deterministic Activities: Folding Branch Structure;
- Non-deterministic Activities: Branch Structure and Ordering;
- Non-deterministic Activities: Repetitive Branch Structure;
- Spectrum of Activities: Permuting Activity Trees;
- Spectrum of Activities: Compacting Branch Structure;
- Spectrum of Activities: Activity Trees and Re-ordering;
- Spectrum and Sub-tree Containment;
- Embedding Constraints for Activities;
- Skeletal Activity Trees;
- Atomic Activities: Upwards Concurrency;
- Atomic Activities: Downwards Concurrency;
- Spectrum for Atomic Activities;
- Preconditions for Activities.

Figure 1 shows the relationships between these extensions and the foundational theories of ISO 18629-12 that are useful for specifying definitional extensions in ISO 18629-41. The arrows show dependencies between extensions in ISO 18629-41 and ISO 18629-12. All theories in ISO 18629-41 are extensions of the ISO 18629-11, itself an extension of the ISO 18629-12. Only the parts of ISO 18629-12 that are useful to showing dependencies with extensions in ISO 18629-41 are shown in Figure 1.

NOTE A complete diagram of dependencies between the extensions in ISO 18629-12 is found in ISO 18629-12 clause 4.1.

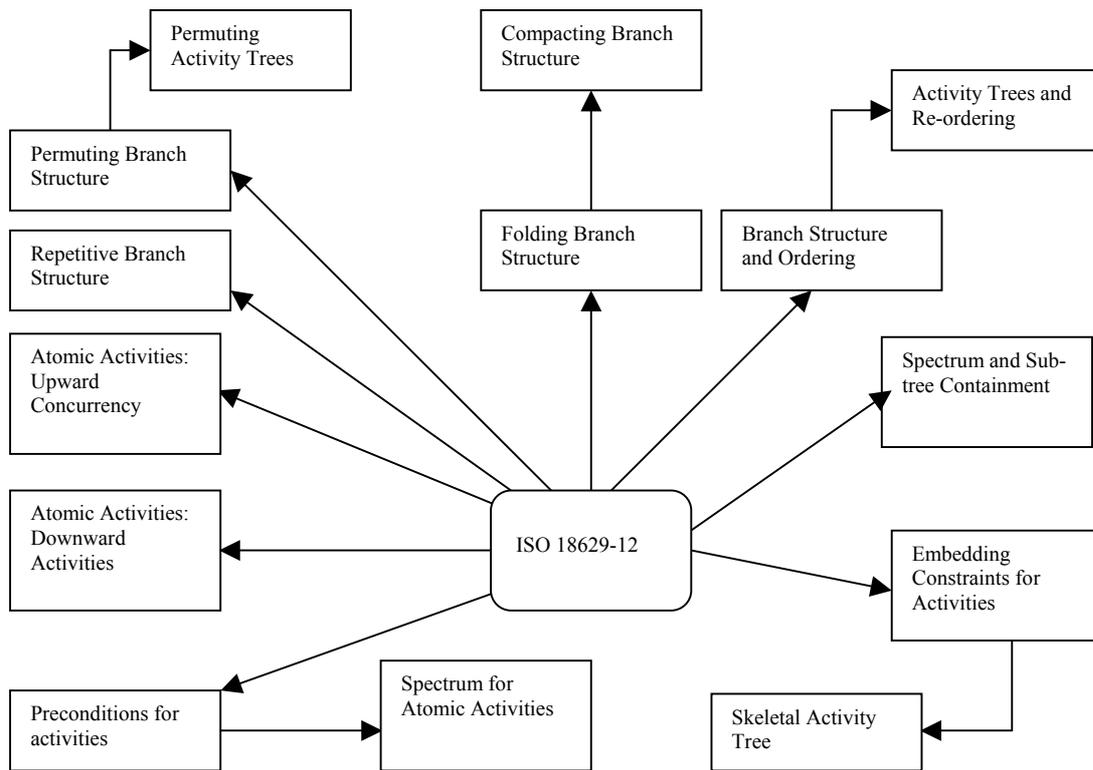


Figure 1: Definitional Extensions of ISO 18629-41

5 Deterministic activities: Permuting Branch Structure

This clause characterizes all definitions pertaining to Deterministic activities: Permuting Branch Structure.

5.1 Primitive lexicon of the Permuting Branch Structure

No primitive relations are required by the lexicon of Permuting Branch Structure.

5.2 Defined lexicon for concepts of Permuting Branch Structure

The following relations are defined in this clause:

(branch_monomorphic ?a ?occ1 ?occ2);

(branch_automorphic ?a ?occ1 ?occ2);

(permuted ?a);

(nondet_permuted ?a);

(partial_permuted ?a);

(simple ?a).

Each concept is described by informal semantics and a KIF axiom.

5.3 Core Theories required by Permuting Branch Structure

This extension requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

5.4 Definitional extensions required by Permuting Branch Structure

No definitional extensions are required by the Permuting Branch Structure.

5.5 Definitions of concepts for Permuting Branch Structure

The following concepts are defined for Permuting Branch Structure.

5.5.1 Branch_monomorphic

One branch of a minimal activity tree is branch-monomorphic to another if and only if the set of atomic activity occurrences in the one branch can be embedded into the set of atomic activity occurrences on the other branch.

(forall (?occ1 ?occ2) (iff (branch_monomorphic ?occ1 ?occ2)

(forall (?s1 ?a)

(implies (and (occurrence_of ?occ1 ?a)

```

(subactivity_occurrence ?s1 ?occ1))
(exists (?s2)
  (and(subactivity_occurrence ?s2 ?occ2)
    (mono ?s1 ?s2 ?a)))))))))

```

5.5.2 Branch_automorphic

Two branches of a minimal activity tree are branch-automorphic if and only if the set of atomic activity occurrences on one branch is a permutation of the the set of atomic activity occurrences on the other branch.

```

(forall (?occ1 ?occ2) (iff (branch_automorphic ?occ1 ?occ2)
  (and (branch_monomorphic ?occ1 ?occ2)
    (branch_monomorphic ?occ2 ?occ1))))))

```

5.5.3 Permuted

An activity occurrence is permuted if and only if the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on every other branch.

```

(forall (?occ) (iff (permuted ?occ)
  (forall (?occ1 ?occ2)
    (implies (and (same_grove ?occ1 ?occ)
      (same_grove ?occ2 ?occ))
      (branch_automorphic ?occ1 ?occ))))))

```

5.5.4 Nondet_permuted

An activity occurrence is nondeterministically permuted if and only if the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on some other branch.

```

(forall (?occ) (iff (nondet_permuted ?occ)
  (forall (?occ1)
    (implies (same_grove ?occ1 ?occ)
      (exists (?occ2)
        (and(same_grove ?occ1 ?occ2)

```

```
(not (= ?occ1 ?occ2))
(branch_automorphic ?occ1 ?occ2))))))
```

5.5.5 Partial_permuted

An activity occurrence is partially permuted if and only if there exists a branch such that the set of atomic subactivity occurrences is a permutation of the atomic subactivity occurrences on some other branch, and there exists a branch that is not a permutation of any other branch.

```
(forall (?occ) (iff (partial_permuted ?occ)
(exist (?occ1 ?occ2 ?occ3)
(and (same_grove ?occ1 ?occ)
(same_grove ?occ2 ?occ)
(not (= ?occ1 ?occ2))
(branch_automorphic ?occ1 ?occ2)
(same_grove ?occ3 ?occ)
(forall (?occ4)
(implies (and (same_grove ?occ3 ?occ4 ?a)
(branch_automorphic ?occ3 ?occ4))
(= ?occ3 ?occ4))))))))))
```

5.5.6 Simple

An activity occurrence is simple if and only if none of the branches in an activity tree are branch automorphic.

```
(forall (?occ) (iff (simple ?occ)
(forall (?occ1 ?occ2)
(implies (and (same_grove ?occ1 ?occ)
(same_grove ?occ2 ?occ)
(branch_automorphic ?occ1 ?occ2))
(= ?occ1 ?occ2))))))
```

5.6 Grammar for relations of Permuting Branch Structure

The following grammar sentences describe process descriptions and auxiliary rules specified in KIF for Permuting Branch Structure.

Note: The function and importance of grammar sentences in ISO 18629 is explained in ISO18629-1 clauses 3.3.8, 4.2.4, and 5.1.

```

< permuted_spec > ::= (forall (< variable >)
                        (implies (same_tree < variable > ?occ)
                                  < occurrence_sentence >))

< nondet_permuted_spec > ::= (forall (< variable >*)
                              (implies (same_tree < variable > ?occ)
                                        (or < occurrence_sentence >*)))

< partial_permuted_spec > ::= (or < nondet_permuted_spec >
                                  < simple_spec >)

< simple_spec > ::= (exists (< variable >*)
                    (and< occurrence_formula >
                      < branch_spec >))

< occurrence_literal > ::= (occurrence < variable > < term >)
                          (subactivity_occurrence < variable > < variable >)

< occurrence_formula > ::= < occurrence_literal > |
                          (and < occurrence_literal >*)

< occurrence_sentence > := (exists (< variable >*)
                           < occurrence_formula >)

< branch_spec > ::= (and(same_tree < variable > ?occ)+
                    (not (= < variable > ?occ))+)

```

6 Non-deterministic activities: Folding Branch Structure

This clause characterizes all definitions pertaining to Non-deterministic activities: Folding Branch Structure.

6.1 Primitive lexicon of Folding Branch Structure

No primitive relations are required by the lexicon of Folding Branch Structure.

6.2 Defined lexicon for concepts of Folding Branch Structure

The following relations are defined in this clause:

- (branch_homomorphic ?occ1 ?occ2);
- (folded ?a);
- (nondet_folded ?a);
- (partial_folded ?a);
- (rigid ?a);

Each concept is described by informal semantics and a KIF axiom.

6.3 Theories required by Folding Branch Structure

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

6.4 Definitional extensions required by Folding Branch Structure

No Definitional Extensions are required by Folding Branch Structure.

6.5 Definitions of Folding Branch Structure

The following concepts are defined for Folding Branch Structure.

6.5.1 Branch_homomorphic

One branch of a minimal activity tree is branch-homomorphic to another if and only if there exists a mapping of the set of atomic activity occurrences in the one branch into the set of atomic activity occurrences on the other branch.

```
(forall (?occ1 ?occ2) (iff branch_homomorphic ?occ1 ?occ2)
  (and (same_grove ?occ1 ?occ2)
    (forall (?s1 ?a)
      (implies (and (occurrence_of ?occ1 ?a)
                    (subactivity_occurrence ?occ3 ?occ1))
                (exists (?s2)
                  (subactivity_occurrence ?s2 ?occ2))
```

(hom ?s1 ?s2 ?a))))))

6.5.2 Folded

An activity is folded if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

(forall (?occ) (iff (folded ?occ)
 (exists (?occ1)
 (and(same_grove ?occ1 ?occ)
 (forall (?occ2)
 (implies (same_grove ?occ2 ?occ)
 (branch_homomorphic ?occ1 ?occ2))))))))))

6.5.3 Nondet_folded

An activity is nondeterministically folded if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

(forall (?occ) (iff (nondet_folded ?occ)
 (forall (?occ1)
 (implies (same_grove ?occ1 ?occ)
 (exists (?occ2)
 (and(same_grove ?occ2 ?occ)
 (not (= ?occ1 ?occ2))
 (branch_homomorphic ?occ1 ?occ2))))))))))

6.5.4 Partial_folded

An activity is partially folded if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

(forall (?occ) (iff (partial_folded ?occ)
 (exists (?occ1 ?occ2 ?occ3)
 (and(same_grove ?occ1 ?occ)
 (same_grove ?occ2 ?occ)

```

(not (= ?occ1 ?occ2))
(branch_homomorphic ?occ1 ?occ2)
(same_grove ?occ3 ?occ)
(forall (?occ4)
  (implies (and (same_grove ?occ4 ?occ)
    (not (= ?occ3 ?occ4)))
    (not (branch_homomorphic ?occ3 ?occ4))))))

```

6.5.5 Rigid

An activity is rigid if and only if none of the branches in an activity tree are branch homomorphic.

```

(forall (?occ) (iff (rigid ?occ)
  (forall (?occ1 ?occ2)
    (implies (and (same_grove ?occ1 ?occ)
      (same_grove ?occ2 ?occ)
      (not (= ?occ1 ?occ2)))
      (not (branch_homomorphic ?occ1 ?occ2))))))

```

6.6 Grammar for process descriptions of Folding Branch Structure

The following grammar sentences describe process descriptions and auxiliary rules specified in KIF for Folding Branch Structure.

```

< folded_spec > ::= (exists (< variable >
  (and(same_tree < variable > ?occ)
    < occurrence_axiom >))
< nondet_folded_spec > ::= (exists (< variable >
  (and (same_tree < variable > ?occ)
    (or < occurrence_axiom >*))
< partial_folded_spec > ::= (or < nondet_folded_spec >
  < rigid_spec >)
< rigid_spec > ::= (exists (< variable >*)

```

$$\begin{aligned}
 & (\text{and} \langle \text{occurrence_formula} \rangle \\
 & \quad \langle \text{branch_spec} \rangle)) \\
 \langle \text{occurrence_disjunct} \rangle ::= & \langle \text{occurrence_literal} \rangle | \\
 & (\text{or} \langle \text{occurrence_literal} \rangle^*) \\
 \langle \text{occurrence_axiom} \rangle ::= & (\text{exists} (\langle \text{variable} \rangle^*) \\
 & \langle \text{occurrence_disjunct} \rangle)
 \end{aligned}$$

7 Non-deterministic activities: Branch Structure and Ordering

This clause characterizes all definitions pertaining to Non-deterministic activities: Branch Structure and Ordering.

7.1 Primitive lexicon of Branch Structure and Ordering

No primitive relations are required by the lexicon of Branch Structure and Ordering.

7.2 Defined lexicon of Branch Structure and Ordering

The following relations are defined in this clause:

- (mono_tree ?s1 ?s2 ?a)
- (order_tree ?s1 ?s2 ?a)
- (root_automorphic ?occ1 ?occ2)
- (ordered ?occ)
- (nondet_ordered ?occ)
- (broken_ordered ?occ)
- (unordered ?occ)

Each concept is described by informal semantics and a KIF axiom.

7.3 Theories required by Branch Structure and Ordering

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occree.th, psl_core.th.

7.4 Definitional extensions required by Branch Structure and Ordering

No Definitional Extensions are required by Branch Structure and Ordering.

7.5 Definitions of Branch Structure and Ordering

The following concepts are defined for Branch Structure and Ordering.

7.5.1 Mono_tree

The subtree rooted in ?s1 can be monomorphically embedded into the subtree rooted in ?s2.

(forall (?s1 ?s2 ?a) (iff (mono_tree ?s1 ?s2 ?a)

(forall (?s3 ?s4 ?s5)

(implies (and (min_precedes ?s1 ?s3 ?a)

(min_precedes ?s2 ?s4 ?a)

(mono ?s3 ?s4 ?a)

(min_precedes ?s3 ?s5 ?a))

(exists (?s6)

(and(mono ?s5 ?s6 ?a)

(min_precedes ?s4 ?s6 ?a))))))

7.5.2 Order_tree

This relation holds iff there exists an order automorphism that maps the subtree rooted in ?s1 to the subtree rooted in ?s2.

(forall (?s1 ?s2 ?a) (iff (order_tree ?s1 ?s2 ?a)

(and (mono_tree ?s1 ?s2 ?a)

(forall (?s3 ?s4 ?s5 ?s6)

(implies (and (min_precedes ?s1 ?s3 ?a)

(min_precedes ?s2 ?s4 ?a)

(cousin ?s3 ?s4 ?a)

(min_precedes ?s3 ?s5 ?a)

(cousin ?s5 ?s6 ?a))

(iff(iso_occ ?s3 ?s5)

(iso_occ ?s4 ?s6))))))

7.5.3 Root_automorphic

Two activity occurrences in the same tree are root automorphic if and only if there exist atomic subactivity occurrences of each activity occurrence that are the roots of isomorphic subtrees.

```
(forall (?occ1 ?occ2) (iff (root_automorphic ?occ1 ?occ2)
  (exists (?a ?s1 ?s2)
    (and(occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (subactivity_occurrence ?s1 ?occ1)
      (subactivity_occurrence ?s2 ?occ2)
      (order_tree ?s1 ?s2 ?a)
      (order_tree ?s2 ?s1 ?a))))))
```

7.5.4 Ordered

An activity occurrence is ordered if and only if it is root automorphic with every other root subactivity occurrence of the same tree.

```
(forall (?occ1 ?occ2) (iff (root_automorphic ?occ1 ?occ2)
  (exists (?a ?s1 ?s2)
    (and(occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (subactivity_occurrence ?s1 ?occ1)
      (subactivity_occurrence ?s2 ?occ2)
      (order_tree ?s1 ?s2 ?a)
      (order_tree ?s2 ?s1 ?a))))))
```

7.5.5 Nondet_ordered

An activity occurrence is nondeterministically ordered if and only if each activity occurrence in the tree is root automorphic to some other root subactivity occurrence in the tree.

```
(forall (?occ1) (iff (nondet_ordered ?occ1)
  (forall (?occ2)
    (implies (same_grove ?occ1 ?occ2)
      (exists (?occ3)
```

```
(and(same_grove ?occ1 ?occ3)
      (not (= ?occ3 ?occ2))
      (root_automorphic ?occ2 ?occ3))))))
```

7.5.6 Broken_ordered

An activity is broken ordered if and only if there exist activity occurrences in the same tree that are root automorphic to some other root subactivity occurrences in the tree, and there also exist root subactivity occurrences that are not root automorphic to any other root subactivity occurrence.

```
(forall (?occ1) (iff (broken_ordered ?occ1)
  (exists (?occ2)
    (and(same_grove ?occ1 ?occ2)
          (not (= ?occ1 ?occ2))
          (root_automorphic ?occ1 ?occ2)
          (forall (?occ3)
            (implies (and (same_grove ?occ3 ?occ1)
                          (not (= ?occ3 ?occ2)))
                      (not (root_automorphic ?occ3 ?occ2))))))))))
```

7.5.7 Unordered

An activity occurrence is unordered if and only if none of the activity occurrences in the same tree are root automorphic.

```
(forall (?occ1) (iff (unordered ?occ1)
  (forall (?occ2)
    (implies (and (same_grove ?occ1 ?occ2)
                  (not (= ?occ1 ?occ2)))
              (not (root_automorphic ?occ1 ?occ2))))))
```

7.6 Grammar for Branch Structure and Ordering

The following grammar sentences describe process descriptions and auxiliary rules specified in KIF for Branch Structure and Ordering.

```
< ordered_spec > ::= (forall (< variable >)
  (implies (same_tree < variable > ?occ)
```

< ordered_sentence >)) |

(forall (< variable >
 (implies (same_tree < variable > ?occ)
 < ordered_formula >))

< nondet_ordered_spec > ::= (forall (< variable >
 (implies (same_tree < variable > ?occ)
 (or < ordered_sentence >*)))

< broken_ordered_spec > ::= (forall (< variable >
 (implies (same_tree < variable > ?occ)
 (or {< ordered_sentence >* |
 < ordered_list >*})))

< unordered_spec > ::= (forall (< variable >
 (implies (same_tree < variable > ?occ)
 (or < ordered_list >*)))

< ordered_literal > ::= (min_precedes < variable > < variable > <
 term >)|
 (next_subocc < variable > < variable > < term >)

< ordered_list > ::= < ordered_literal > |
 (and < ordered_literal >*)

< conditional_occurrence > ::= (implies < occurrence_formula >
 < ordered_list >)

$$\begin{aligned} \langle \text{ordered_sentence} \rangle ::= & \quad (\text{exists} (\langle \text{variable} \rangle) \\ & \quad (\text{and}(\text{root_occ} \langle \text{variable} \rangle ?\text{occ}) \\ & \quad \quad \langle \text{occurrence_disjunct} \rangle \\ & \quad \quad \langle \text{conditional_occurrence} \rangle)))) \end{aligned}$$

$$\begin{aligned} \langle \text{ordered_conjunct} \rangle ::= & \quad \langle \text{ordered_literal} \rangle | \\ & \quad (\text{and} \langle \text{ordered_formula} \rangle^*) \end{aligned}$$

$$\begin{aligned} \langle \text{ordered_formula} \rangle ::= & \quad (\text{exists} (\langle \text{variable} \rangle) \\ & \quad (\text{and} (\text{root_occ} \langle \text{variable} \rangle ?\text{occ}) \\ & \quad \quad \langle \text{occurrence_disjunct} \rangle \\ & \quad \quad \langle \text{ordered_conjunct} \rangle)) | \\ & \quad (\text{or} \langle \text{ordered_formula} \rangle^*) \end{aligned}$$

8 Non-deterministic activities: Repetitive Branch Structure

This clause characterizes all definitions pertaining to Non-deterministic activities: Repetitive Branch Structure.

8.1 Primitive lexicon of Repetitive Branch Structure

No primitive relations are required by the lexicon of Repetitive Branch Structure.

8.2 Defined relations of Repetitive Branch Structure

The following relations are defined in this clause:

- (branch_mono ?s1 ?s2 ?s3 ?s4 ?a)
- (reptree ?s ?occ)
- (repetitive ?occ)
- (nondet_repetitive ?occ)
- (partial_repetitive ?occ)
- (amorphous ?occ)

Each concept is described by informal semantics and a KIF axiom.

8.3 Theories required by Repetitive Branch Structure

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

8.4 Definitional extensions required by Repetitive Branch Structure

No Definitional Extensions are required by the Repetitive Branch Structure.

8.5 Definitions of Repetitive Branch Structure

The following concepts are defined for Repetitive Branch Structure.

8.5.1 Branch_mono

The sub-branch of a minimal activity with initial atomic subactivity occurrence ?s1 and final atomic subactivity occurrence ?s2 is occurrence-isomorphic to the sub-branch with initial atomic subactivity occurrence ?s3 and final atomic subactivity occurrence ?s4.

(forall (?s1 ?s2 ?s3 ?s4 ?a) (iff (branch_mono ?s1 ?s2 ?s3 ?s4 ?a)

(forall (?s5 ?s6)

(implies (and (min_precedes ?s1 ?s5 ?a)

(min_precedes ?s6 ?s2 ?a)

(next_subocc ?s5 ?s6 ?a))

(exists (?s7 ?s8)

(and (min_precedes ?s3 ?s7 ?a)

(min_precedes ?s8 ?s4 ?a)

(next_subocc ?s7 ?s8 ?a)

(iso_occ ?s5 ?s7)

(iso_occ ?s6 ?s8)))))))))

8.5.2 Reptree

Every atomic subactivity occurrence in ?occ can be embedded in a branch of the subtree whose root occurrence is ?s.

(forall (?s ?occ) (iff (reptree ?s ?occ)

(forall (?s1 ?a)

```
(implies (and (occurrence ?occ ?a)
              (subactivity_occurrence ?s1 ?occ))
         (exists (?s2 ?s3 ?s4 ?occ1)
              (and(same_tree ?o ?o1)
                  (leaf_occ ?s2 ?occ1)
                  (<_min ?s3 ?s1 ?a)
                  (<_min ?s1 ?s4 ?a)
                  (branch_mono ?s3 ?s4 ?s ?s2 ?a))))))
```

8.5.3 Repetitive

An activity occurrence is repetitive if and only if every branch in the same activity tree can be embedded in a unique subtree. Intuitively, this is equivalent to the existence of a unique repeating subtree.

```
(forall (?occ) (iff (repetitive ?occ)
                    (exists (?s1 ?occ2)
                          (and(same_tree ?occ ?occ2)
                              (subactivity_occurrence ?s ?occ2)
                              (forall (?occ1)
                                    (implies (same_tree ?occ ?occ1)
                                              (and (reptree ?s ?occ1)
                                                  (not (root_occ ?s ?occ1))))))))))
```

8.5.4 nondet_repetitive

An activity is nondeterministically repetitive if and only if every branch in the same activity tree can be embedded in some subtree. Intuitively, this is equivalent to the existence of multiple nonisomorphic repeating subtrees.

```
(forall (?occ) (iff (nondet_repetitive ?occ)
                    (forall (?occ1)
                          (implies (same_tree ?occ ?occ1)
                                    (exists (?s1 ?occ2)
                                          (and(same_tree ?occ ?occ2)
```

```
(subactivity_occurrence ?s ?occ2)
(reptree ?s ?occ1)
(not (root_occ ?s ?occ1)))))))))
```

8.5.5 partial_repetitive

An activity occurrence is partially repetitive if and only if there exist repeating subtrees, but there also exist branches in the same tree that cannot be mapped to any repeating subtree.

```
(forall (?occ) (iff (partial_repetitive ?occ)
  (and (exists (?occ1 ?occ2 ?s1)
    (and (same_tree ?occ ?occ1)
      (same_tree ?occ ?occ2)
      (subactivity_occurrence ?s ?occ2)
      (rep_tree ?s ?occ1)
      (not (root_occ ?s ?occ1))))))
    (exists (?occ2)
      (forall (?s2)
        (implies (reptree ?s1 ?occ1)
          (root_occ ?s1 ?occ1)))))))))
```

8.5.6 Amorphous

An activity occurrence is amorphous if and only if there are no repeating subtrees in the same activity tree.

```
(forall (?occ) (iff amorphous ?occ)
  (forall (?occ1 ?s)
    (implies (and (same_tree ?occ1 ?occ)
      (reptree ?s ?occ1))
      (root_occ ?s ?occ1))))))
```

8.6 Grammar for Repetitive Branch Structure

The following grammar sentences describe process descriptions and auxiliary rules specified in KIF for Repetitive Branch Structure.

```
< repetitive_spec > ::= (forall (< term > ?s1 ?s2)
```

(iff (do < term > ?s1 ?s2)
 < rep_formula >))

< nondet_rep_spec > ::= (forall (< term > ?s1 ?s2)
 (iff (do < term > ?s1 ?s2)
 (or < rep_formula >*))

< partial_rep_spec > ::= (forall (< term > ?s1 ?s2)
 (iff (do < term > ?s1 ?s2)
 < partial_rep_formula >

< rep_formula > ::= (exists (< term >)
 (and(subactivity < term > < term >)
 (forall (?s3)
 (implies (do < term > ?s1 ?s3)
 (or (= ?s2 ?s3)
 (do < term > ?s3 ?s2))))))

< partial_rep_formula > ::= (exists (< term > ?s3)
 (and(subactivity < term > < term >)
 (do < term > ?s1 ?s3)
 (or (= ?s2 ?s3)
 (do < term > ?s3 ?s2))))

9 Spectrum of activities: Permuting Activity Trees

This clause characterizes all definitions pertaining to Spectrum of Activities: Permuting Activity Tree.

9.1 Primitive lexicon of Permuting Activity Trees

No primitive relations are required by the lexicon of Permuting Activity Trees.

9.2 Defined relations of Permuting Activity Trees

The following relations are defined in this clause:

- (reordered ?a)
- (partial_reordered ?a)
- (nondet_reorder ?a)
- (nonorderable ?a)

Each concept is described by informal semantics and a KIF axiom.

9.3 Theories required by Permuting Activity Trees

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

9.4 Definitional extensions required by Permuting Activity Trees

This extension requires Permuting Branch Structure.

9.5 Definitions of Permuting Activity Trees

The following concepts are defined for Permuting Activity Trees.

9.5.1 Reordered

An activity is reordered if and only if the set of atomic subactivity occurrences on each branch of one minimal activity tree is a permutation of the atomic subactivity occurrences on a branch in another activity tree for ?a.

```
(forall (?a) (iff (reordered ?a)
  (forall (?occ1 ?occ2)
    (implies (and (occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a))
      (branch_automorphic ?occ1 ?occ2))))))
```

9.5.2 Nondet_reordered

An activity is nondeterministically reordered if and only if the set of atomic subactivity occurrences on each branch of one minimal activity tree for ?a is a permutation of the atomic subactivity occurrences on some branch of another minimal activity tree for ?a.

```

(forall (?a) (iff (nondet_reordered ?a)
  (forall (?occ1)
    (implies (occurrence_of ?occ1 ?a)
      (exists (?occ2)
        (and(occurrence_of ?occ2 ?a)
          (not (same_grove ?occ1 ?occ2))
          (branch_automorphic ?occ1 ?occ2))))))))))

```

9.5.3 Partial_reordered

An activity is partially reordered if and only if there exists a branch such that the set of atomic subactivity occurrences is a permutation of the atomic ubactivity occurrences on some other branch, and there exists a branch that is not a permutation of any other branch.

```

(forall (?a) (iff (partial_reordered ?a)
  (exist (?occ1 ?occ2 ?occ3)
    (and(occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (not (same_grove ?occ1 ?occ2))
      (branch_automorphic ?occ1 ?occ2)
      (occurrence_of ?occ3 ?a)
      (same_grove ?occ1 ?occ3)
      (forall (?occ4)
        (implies (and (occurrence_of ?occ4 ?a)
          (not (= ?occ2 ?occ4))
          (same_grove ?occ2 ?occ4))
          (not (branch_automorphic ?occ2 ?occ4))))))))))

```

9.5.4 Unorderable

An activity is nonorderable if and only if none of the branches in an activity tree are branch automorphic to any other branches in other activity trees in the spectrum.

```

(forall (?a) (iff (unorderable ?a)

```

```
(forall (?occ1 ?occ2)
  (implies (and (occurrence_of ?occ1 ?a)
    (occurrence_of ?occ2 ?a)
    (not (same_grove ?occ1 ?occ2)))
    (not (branch_automorphic ?occ1 ?occ2))))))
```

9.6 Grammar for process descriptions of Permuting Activity Trees

The following grammar sentences describe process descriptions specified in KIF for Permuting Activity Trees (Branchwise Permuted Activity Axioms).

```
< reordered_spec > ::= (forall (< variable >
  (implies (occurrence < variable > < term >
    < occurrence_sentence >))

< nondet_reordered_spec > ::= (forall (< variable >*)
  (implies (occurrence < variable > < term >
    (or < occurrence_sentence >*)))

< partial_reordered_spec > ::= (or < nondet_reordered_spec >
  < nonorderable_spec >)

< nonorderable_spec > ::= (exists (< variable >*)
  (and< occurrence_formula >
    < branch_spec >))
```

10 Spectrum of Activities: Compacting Branch Structure

This clause characterizes all definitions pertaining to Spectrum of Activities: Compacting Branch Structure.

10.1 Primitive lexicon of Compacting Branch Structure

No primitive relations are required by the lexicon of Compacting Branch Structure.

10.2 Defined lexicon of Compacting Branch Structure

The following relations are defined in this clause:

- (compacted ?a)
- (nondet_compacted ?a)
- (partial_compacted ?a)
- (stiff ?a)

Each concept is described by informal semantics and a KIF axiom.

10.3 Theories required by Compacting Branch Structure

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

10.4 Definitional extensions required by Compacting Branch Structure

This extension requires Permuting Branch Structure.

10.5 Definitions of Compacting Branch Structure

The following concepts are defined for Compacting Branch Structure.

10.5.1 Compacted

An activity is compacted if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

```
(forall (?a) (iff (compacted ?a)
  (exists (?occ1)
    (and(occurrence_of ?occ1 ?a)
      (forall (?occ2)
        (implies (and (occurrence_of ?occ2 ?a)
          (not (same_grove ?occ1 ?occ2)))
          (branch_homomorphic ?occ1 ?occ2))))))))))
```

10.5.2 Nondet_compacted

An activity is nondeterministically compacted if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

```

(forall (?a) (iff (nondet_compacted ?a)
  (forall (?occ1)
    (implies (occurrence_of ?occ1 ?a)
      (exists (?occ2)
        (and(occurrence_of ?occ2 ?a)
          (not (same_grove ?occ1 ?occ2))
          (branch_homomorphic ?occ1 ?occ2))))))))))

```

10.5.3 Partial_compacted

An activity is partially compacted if and only if there exists a branch such that the set of atomic subactivity occurrences on each branch of the minimal activity tree is a permutation of the atomic subactivity occurrences on the first branch.

```

(forall (?a) (iff (partial_compacted ?a)
  (exists (?occ1 ?occ2 ?occ3)
    (and(occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (not (same_grove ?occ1 ?occ2))
      (branch_homomorphic ?occ1 ?occ2)
      (occurrence_of ?occ3 ?a)
      (same_grove ?occ3 ?occ1)
      (forall (?occ4)
        (implies (and (occurrence_of ?occ4 ?a)
          (not (= ?occ2 ?occ4))
          (same_grove ?occ2 ?occ4))
          (not (branch_homomorphic ?occ2 ?occ4))))))))))

```

10.5.4 Stiff

An activity is stiff if and only if none of the branches in an activity tree for ?a are branch epimorphic to the branches of any other activity tree for ?a.

```

(forall (?a) (if (stiff ?a)
  (forall (?occ1 ?occ2)

```

```
(implies (and (occurrence_of ?occ1 ?a)
              (occurrence_of ?occ2 ?a)
              (not (same_grove ?occ1 ?occ2)))
         (not (branch_homomorphic ?occ1 ?occ2))))))
```

10.6 Grammar for of Compacting Branch Structure

The following grammar sentences describe process descriptions specified in KIF for Compacting Branch Structure.

```
< compacted_spec > ::= (forall (< variable >)
  (implies (occurrence < variable > < term >)
    (exists (< variable >)
      (and(occurrence < variable > < term >)
        < occurrence_axiom >))))))

< nondet_compacted_spec > ::= (forall (< variable >)
  (implies (occurrence < variable > < term >)
    (exists (< variable >)
      (and(occurrence < variable > < term >)
        (or < occurrence_axiom >*)))))

< partial_compacted_spec > ::= (or < nondet_compacted_spec >
  < stiff_spec >)

< stiff_spec > ::= (exists (< variable >*)
  (and< occurrence_formula >
    < branch_spec >))
```

11 Spectrum of Activities: Activity Trees and Re-ordering

This clause characterizes all definitions pertaining to Spectrum Activities: Activity Tree and Re-ordering.

11.1 Primitive lexicon of Activity Trees and Re-ordering

No primitive relations are required by the lexicon of Activity Trees and Re-ordering.

11.2 Defined lexicon of Activity Trees and Re-ordering

The following relations are defined in this clause:

- (treeordered ?a)
- (partial_treeordered ?a)
- (nondet_treeordered ?a)
- (scrambled ?a)

Each concept is described by informal semantics and a KIF axiom.

11.3 Theories required by Activity Trees and Re-ordering

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

11.4 Definitional extensions required by Activity Trees and Re-ordering

This Extension requires Branch Structure and Ordering.

11.5 Definitions of Activity Trees and Re-ordering

The following concepts are defined for Activity Trees and Re-ordering.

11.5.1 Treeordered

An activity is treeordered if and only if the root subactivity occurrence of one occurrence is root automorphic with every other root subactivity occurrence of other occurrences of the activity.

```
(forall (?a) (iff (treeordered ?a)
  (forall (?occ1 ?occ2)
    (implies (and (occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (not (same_grove ?occ1 ?occ2))
      (root_automorphic ?occ1 ?occ2))))))
```

11.5.2 Nondet_treeordered

An activity occurrence is nondeterministically treeordered if and only if each root subactivity occurrence of the minimal activity tree is root automorphic to some other root subactivity occurrence in the occurrence tree.

```
forall (?a) (iff (nondet_treeordered ?a)
  (forall (?occ1)
    (implies (occurrence_of ?occ1 ?a)
      (exists (?occ2)
        (and (occurrence_of ?occ2 ?a)
          (not (same_grove ?occ1 ?occ2))
          (root_automorphic ?occ1 ?occ2))))))))
```

11.5.3 Partial_treeordered

An activity is partially treeordered if and only if there exist root subactivity occurrences of the minimal activity tree that are root automorphic to some other root subactivity occurrences in the occurrence tree, and there also exist root subactivity occurrences that are not root automorphic to any other root subactivity occurrence.

```
(forall (?a) (iff (partial_treeordered ?a)
  (exists (?occ1 ?occ2)
    (and (occurrence_of ?occ1 ?a)
      (occurrence_of ?occ2 ?a)
      (not (same_grove ?occ1 ?occ2))
      (root_automorphic ?occ1 ?occ2)
      (forall (?occ3)
        (implies (and (occurrence_of ?occ3 ?a)
          (not (same_grove ?occ3 ?occ2)))
          (not (root_automorphic ?occ3 ?occ2))))))))
```

11.5.4 Scrambled

An activity is scrambled if and only if none of the branches in an activity tree are root automorphic to any other activity tree.

```
(forall (?a) (iff (scrambled ?a)
```

```
(forall (?occ1 ?occ2)
  (implies (and (occurrence_of ?occ1 ?a)
    (occurrence_of ?occ2 ?a)
    (not (same_grove ?occ1 ?occ2))
    (not (root_automorphic ?occ1 ?occ2))))))
```

11.6 Grammar of Activity Trees and Re-ordering

The following grammar sentences describe process descriptions specified in KIF for Activity Trees and Re-ordering.

```
< treeordered_spec > ::= (forall (< variable >
  (implies (occurrence < variable > < term >
    < ordered_sentence >)) |
  (forall (< variable >
    (implies (occurrence < variable > < term >
      < ordered_formula >))
```

```
< nondet_treeordered_spec > ::= (forall (< variable >
  (implies (occurrence < variable > < term >
    (or < ordered_sentence >*))
```

```
< partial_treeordered_spec > ::= (forall (< variable >
  (implies (occurrence < variable > < term >
    (or {< ordered_sentence >* |
      < ordered_list >*})))
```

```
< scrambled_spec > ::= (forall (< variable >
  (implies (occurrence < variable > < term >
    (or < ordered_list >*)))
```

12 Spectrum and Subtree Containment

This clause characterizes all definitions pertaining to Spectrum and Subtree Containment.

12.1 Primitive lexicon of Spectrum and Subtree Containment

No primitive relations are required by the lexicon of Spectrum and Subtree Containment.

12.2 Defined lexicon of Spectrum and Subtree Containment

The following relations are defined in this clause:

- (subtree_embed ?occ1 ?occ2 ?a)
- (multiple_outcome ?a)
- (weak_outcome ?a)
- (nondet_outcome ?a)
- (imiscible ?a)

Each concept is described by informal semantics and a KIF axiom.

12.3 Theories required by Spectrum and Subtree Containment

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

12.4 Definitional extensions required by Spectrum and Subtree Containment

No Definitional Extensions are required by Spectrum and Subtree Containment.

12.5 Definitions of Spectrum and Subtree Containment

The following concepts are defined for Spectrum and Subtree Containment.

12.5.1 Subtree_embed

One minimal activity tree for ?a can be embedded into another as a subtree if and only if any atomic subactivity occurrence in the tree rooted in ?s1 can be mapped to an atomic subactivity occurrence in the tree rooted in ?s2 in such a way that the ordering is preserved.

$$(\text{forall } (?s1 ?s2 ?a) (\text{iff } (\text{subtree_embed } ?s1 ?s2 ?a)$$

$$(\text{forall } (?s3)$$

$$(\text{implies } (\text{min_precedes } ?s1 ?s3 ?a)$$

$$(\text{exists } (?s4)$$

(and (min_precedes ?s2 ?s4 ?a)
(iso_occ ?s4 ?s3))))))

12.5.2 Multiple_outcome

An activity is multiple outcome if and only if any two activity trees can be embedded into one another.

(forall (?a) (iff (multiple_outcome ?a)
(forall (?s1 ?s2)
(implies (and (root ?s1 ?a)
(root ?s2 ?a))
(or (subtree_embed ?s1 ?s2 ?a)
(subtree_embed ?s2 ?s1 ?a)))))))

12.5.3 Weak_outcome

An activity ?a is weak outcome if and only if there exists a minimal activity tree that can be embedded into all other minimal activity trees of ?a.

(forall (?a) (iff (weak_outcome ?a)
(exists (?s1)
(and (root ?s1 ?a)
(forall (?s2)
(implies (root ?s2 ?a)
(subtree_embed ?s2 ?s1 ?a)))))))

12.5.4 Nondet_outcome

An activity ?a has a nondeterministic outcome if and only if there exists a minimal activity tree that can be embedded into other minimal activity trees of ?a, and there also exists branches that cannot be embedded.

(forall (?a) (iff (nondet_outcome ?a)
(exists (?s1 ?s2 ?s3)
(and (root ?s1 ?a)
(root ?s2 ?a)
(subtree_embed ?s2 ?s1 ?a)
(root ?s3 ?a)

```
(forall (?s4)
  (implies (root ?s4 ?a)
    (not (or(subtree_embed ?s3 ?s4 ?a)
      (subtree_embed ?s4 ?s3 ?a))))))
```

12.5.5 imiscible

An activity is imiscible if and only if no tree in the spectrum can be embedded into any other.

```
(forall (?a) (iff (imiscible ?a)
  (forall (?s1 ?s2)
    (implies (and (root ?s1 ?a)
      (root ?s2 ?a))
      (not (or(subtree_embed ?s1 ?s2 ?a)
        (subtree_embed ?s2 ?s1 ?a))))))
```

12.6 Grammar for Permuting Branch Structure

The grammar for process descriptions of Permuting Branch Structure is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

13 Embedding Constraints for Activities

This clause characterizes all definitions pertaining to Embedding Constraints for Activities.

13.1 Primitive lexicon of Embedding Constraints for Activities

No primitive relations are required by the lexicon of Embedding Constraints for Activities.

13.2 Defined lexicon of Embedding Constraints for Activities

The following relations are defined in this clause:

- (live_branch ?s1 ?s2 ?a)
- (embedded ?s1 ?s2 ?a)
- (dead_branch ?s1 ?s2 ?a)
- (dead_occurrence ?s1 ?s2 ?a)
- (embed_tree ?s1 ?s2 ?s3 ?a)

— (subocc_equiv ?s1 ?s2 ?s3 ?a)

— (unrestricted ?occ)

Each concept is described by informal semantics and a KIF axiom.

13.3 Theories required by Embedding Constraints for Activities

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

13.4 Definitional extensions required by Embedding Constraints for Activities

No Definitional Extensions are required by Embedding Constraints for Activities

13.5 Definitions of Embedding Constraints for Activities

The following concepts are defined for Embedding Constraints for Activities.

13.5.1 Live_branch

An atomic activity occurrence ?s2 is on a live branch of an embedded activity tree for ?a with root ?s1 if and only if it is a subactivity occurrence on the branch.

(forall (?s1 ?s2 ?a) (iff (live_branch ?s1 ?s2 ?a)

(exists (?occ)

(and(occurrence_of ?occ ?a)

(root_occ ?s1 ?occ)

(min_precedes ?s1 ?s2 ?a))))))

13.5.2 Embedded

An activity occurrence is an element of the positive maximal embedded subtree if and only if it is an external activity occurrence that is between two subactivity occurrences on a branch of the occurrence tree.

(forall (?s1 ?s2 ?a) (iff (embedded ?s1 ?s2 ?a)

(exists (?s3)

(and(root ?s2 ?a)

(min_precedes ?s2 ?s3 ?a)

(precedes ?s2 ?s1)

(precedes ?s1 ?s3)

(not (min_precedes ?s1 ?s3 ?a))))))

13.5.3 Dead_branch

An occurrence ?s2 is on a dead branch with respect to an activity tree for ?a with root occurrence ?s1 if and only if ?s2 is on a branch that is occurrence isomorphic to a branch of the embedded activity tree. The activity occurrence ?s2 is the earliest dead occurrence with respect to the activity tree for ?a with root occurrence ?s1 if and only if it is the successor of a non-leaf subactivity occurrence in the activity tree but there are no subactivity occurrences of the tree that are later than ?s2.

```
(forall (?s1 ?s2 ?a) (iff (dead_branch ?s1 ?s2 ?a)
  (exists (?a1 ?s3)
    (and (root ?s1 ?a)
      (min_precedes ?s1 ?s3 ?a)
      (not (leaf ?s3 ?a))
      (= ?s2 (successor ?a1 ?s3))
      (not (exists (?s4)
        (and (precedes ?s3 ?s4)
          (min_precedes ?s3 ?s4 ?a))))))))))
```

13.5.4 Dead_occurrence

An external activity occurrence ?s2 is a dead occurrence with respect to the activity tree for ?a with root occurrence ?s1 if and only if ?s2 is between two activity occurrences on a dead branch for ?a.

```
(forall (?s1 ?s2 ?a) (iff (dead_occurrence ?s1 ?s2 ?a)
  (exists (?s3)
    (and (dead_branch ?s1 ?s3 ?a)
      (precedes ?s1 ?s2)
      (precedes ?s2 ?s3))))))
```

13.5.5 Embed_tree

?s1 and ?s2 are occurrences of subactivities of ?a that are elements of the same embedded activity tree for ?a with root ?s3.

```
(forall (?s1 ?s2 ?s3 ?a) (iff (embed_tree ?s1 ?s2 ?s3 ?a)
  (exists (?a1 ?a2)
    (and (subactivity ?a1 ?a)
      (subactivity ?a2 ?a))
```

```

(occurrence_of ?s1 ?a1)
(occurrence_of ?s2 ?a2)
(or (live_branch ?s3 ?s1 ?a)
    (dead_branch ?s3 ?s1 ?a))
(or (live_branch ?s3 ?s2 ?a)
    (dead_branch ?s3 ?s2 ?a))))))

```

13.5.6 Subocc_equiv

Two activity occurrences ?s1,?s2 are subocc equivalent with respect to ?a if and only if they are elements of the same maximal embedded subtree for ?a with root occurrence ?s3, they are occurrences of subactivities, and they agree on whether or not they are subactivity occurrences of an occurrence of ?a.

```

(forall (?s1 ?s2 ?s3 ?a) (iff (subocc_equiv ?s1 ?s2 ?s3 ?a)
    (and (embed_tree ?s1 ?s2 ?s3 ?a)
        (iff (min_precedes ?s3 ?s1 ?a)
            (min_precedes ?s3 ?s2 ?a))))))

```

13.5.7 unrestricted

An activity occurrence ?occ is unrestricted if and only if every branch in the maximal embedded subtree is a live branch.

```

(forall (?occ) (iff unrestricted ?occ)
    (forall (?a ?s1 ?s2 ?s3)
        (implies (and (occurrence_of ?occ ?a)
            (root_occ ?s3 ?occ)
            (embed_tree ?s1 ?s2 ?s3 ?a)
            (subocc_equiv ?s1 ?s2 ?s3 ?a))))))

```

13.6 Grammar for Embedding Constraints for Activities.

The grammar for process descriptions of Embedding Constraints for Activities is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

14 Skeletal Activity Trees

This clause characterizes all definitions pertaining to Skeletal Activity Trees.

14.1 Primitive lexicon of Skeletal Activity Trees

No primitive relations are required by the lexicon of Skeletal Activity Trees.

14.2 Defined lexicon of Skeletal Activity Trees

The following relations are defined in this clause:

- (fused ?occ)
- (embed_occ ?occ)
- (free ?occ)
- (assisted ?occ)
- (helpless ?occ)
- (unbound ?occ)
- (bound ?occ)
- (strict ?occ)

Each concept is described by informal semantics and a KIF axiom.

14.3 Theories required by Skeletal Activity Trees

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

14.4 Definitional extensions required by Skeletal Activity Trees

This extension requires Embedding Constraints for Activities

14.5 Definitions of Skeletal Activity Trees

The following concepts are defined for Skeletal Activity Trees.

14.5.1 Fused

An activity occurrence ?occ is fused if and only if every activity occurrence between a root and a leaf occurrence is also a subactivity occurrence of ?occ.

$$(\text{forall } (?occ) (\text{iff}(\text{fused } ?occ)$$

$$(\text{forall } (?s1 ?s2 ?s3)$$

$$(\text{implies } (\text{and } (\text{root_occ } ?s1 ?occ)$$

$$(\text{subactivity_occurrence } ?s2 ?occ)$$

```
(precedes ?s1 ?s3)
(precedes ?s3 ?s2))
(subactivity_occurrence ?s3 ?occ))))))
```

14.5.2 Embedd_occ

The branch of the occurrence tree containing the activity occurrence ?occ can be embedded into a dead branch in the same maximal embedded subtree.

```
(forall (?occ) (iff (embed_occ ?occ)
(forall (?a ?s ?s1 ?s2 ?s3)
(implies (and (occurrence_of ?occ ?a)
(root_occ ?s ?occ)
(next_subocc ?s1 ?s2 ?occ)
(precedes ?s1 ?s3)
(precedes ?s3 ?s2))
(exists (?s4 ?s5 ?s6)
(and(precedes ?s4 ?s5)
(precedes ?s5 ?s6)
(iso_occ ?s4 ?s1)
(iso_occ ?s5 ?s3)
(iso_occ ?s6 ?s3)
(dead_branch ?s1 ?s4 ?a)
(dead_branch ?s1 ?s6 ?a))))))))))
```

14.5.3 Free

An activity occurrence is free if and only if there exist activity occurrences in the same tree that are fused and there exist activity occurrences that are not fused. This is equivalent to saying that there do not exist necessary external activity occurrences.

```
(forall (?occ) (iff (free ?occ)
(exists (?occ1 ?occ2)
(and(same_tree ?occ ?occ1)
(same_tree ?occ ?occ2)
```

```
(not (fused ?occ1))
(fused ?occ2))))))
```

14.5.4 Assisted

An activity occurrence is assisted if and only if every activity occurrence in the same tree are not fused. This is equivalent to saying that there exist necessary external activity occurrences.

```
(forall (?occ) (iff (assisted ?occ)
(forall (?occ1)
(implies (same_tree ?occ ?occ1)
(not (fused ?occ1)))))))
```

14.5.5 Helpless

An activity is helpless if and only if between any two subactivity occurrences, there exists an external activity occurrence. This is equivalent to saying that external activities are always necessary.

```
(forall (?occ) (iff (helpless ?occ)
(forall (?s1 ?s2)
(implies (next_subocc ?s1 ?s2 ?occ)
(exists (?s3)
(and(precedes ?s1 ?s3)
(precedes ?s3 ?s2)
(not (subactivity_occurrence ?s3 ?occ))))))))))
```

14.5.6 Unbound

An activity occurrence is unbound if and only if none of the activity occurrences in the same tree can be embedded into dead branches. This is equivalent to the nonexistence of forbidden external activities.

```
(forall (?occ) (iff (unbound ?occ)
(forall (?occ1)
(implies (same_tree ?occ1 ?occ)
(not (embed_occ ?occ1)))))))
```

14.5.7 Bound

An activity occurrence is bound if and only if there exist activity occurrences in the same tree that can be embedded into dead branches. This is equivalent to the existence of forbidden external activities.

```
(forall (?occ) (iff (bound ?occ)
  (exists (?occ1 ?occ2)
    (and(same_tree ?occ1 ?occ)
      (not (embed_occ ?occ1))
      (same_tree ?occ2 ?occ)
      (embed_occ ?occ2))))))
```

14.5.8 Strict

An activity occurrence is strict if and only if all occurrences in the same tree are fused. This is equivalent to saying that all external activity occurrences are forbidden.

```
(forall (?occ) (iff (strict ?occ)
  (forall (?occ1)
    (implies (same_tree ?occ ?occ1)
      (fused ?occ1))))))
```

14.6 Grammar for Skeletal Activity Tree

The grammar for process descriptions of Skeletal Activity Tree is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

15 Atomic Activities: Upwards Concurrency

This clause characterizes all definitions pertaining to Atomic Activities: Upwards Concurrency.

15.1 Primitive lexicon of Atomic Activities: Upwards Concurrency

No primitive relations are required by the lexicon of Atomic Activities: Upwards Concurrency.

15.2 Defined lexicon of Atomic Activities: Upwards Concurrency

The following relations are defined in this clause:

- (natural ?a ?s)
- (artificial ?a ?s)

— (performed ?a ?s)

— (up_ghost ?a ?s)

— (up_conflict ?a ?s)

— (quark ?a ?s)

Each concept is described by informal semantics and a KIF axiom.

15.3 Theories required by Atomic Activities: Upwards Concurrency

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

15.4 Definitional extensions required by Atomic Activities: Upwards Concurrency

No Definitional Extensions are required by Atomic Activities: Upwards Concurrency.

15.5 Definitions of Atomic Activities: Upwards Concurrency

The following concepts are defined for Atomic Activities: Upward Concurrency.

15.5.1 Natural

An activity is natural if and only if it is a subactivity of any activity that is possible whenever it is possible.

(forall (?a ?s) (iff (natural ?a ?s)

(forall (?a1)

(implies (and (poss ?a ?s)

(poss ?a1 ?s))

(subactivity ?a ?a1))))))

15.5.2 Artificial

An activity is an artificial activity if and only if

(forall (?a ?s) (iff (artificial ?a ?s)

(forall (?a1)

(implies (and (poss ?a ?s)

(poss ?a1 ?s)

(not (subactivity ?a1 ?a))))))

(poss (conc ?a ?a1) ?s))))))

15.5.3 Performed

An activity is a performed activity if and only if

(forall (?a ?s) (iff (performed ?a ?s)
 (exists (?a1 ?a2)
 (and(subactivity ?a1 ?a)
 (subactivity ?a2 ?a)
 (poss ?a ?s)
 (not (poss (conc ?a1 ?a2) ?s))))))))))

15.5.4 Up_ghost

An activity is an up_ghost activity if and only if

(forall (?a ?s) (iff (up_ghost ?a ?s)
 (forall (?a1)
 (implies (and (poss ?a1 ?s)
 (subactivity ?a ?a1))
 (poss ?a ?s))))))

15.5.5 Up_conflict

An activity is an up_conflict activity if and only if

(forall (?a ?s) (iff (up_conflict ?a ?s)
 (forall (?a1)
 (implies (poss (conc ?a ?a1) ?s)
 (or(poss ?a ?s)
 (poss ?a1 ?s)
 (subactivity ?a ?a1))))))))))

15.5.6 Quark

An activity is a quark activity if and only if

(forall (?a ?s) (iff (quark ?a ?s)

(exists (?a1 ?s)
 (and(atomic ?a1)
 (subactivity ?a ?a1)
 (poss ?a1 ?s)
 (not (poss ?a ?s))))))

15.6 Grammar for Atomic Activities: Upwards Concurrency

The grammar for the process descriptions of Atomic Activities: Upward Concurrency is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

16 Atomic Activities: Downwards Concurrency

This clause characterizes all definitions pertaining to Atomic Activities: Downwards Concurrency.

16.1 Primitive lexicon of Atomic Activities: Downwards Concurrency

No primitive relations are required by the lexicon of Atomic Activities: Downwards Concurrency.

16.2 Defined lexicon of Atomic Activities: Downwards Concurrency

The following relations are defined in this clause:

- (superpose ?a ?s)
- (assistance ?a ?s)
- (team ?a ?s)
- (ghost ?a ?s)
- (conflict ?a ?s)
- (dysfunction ?a ?s)

Each concept is described by informal semantics and a KIF axiom.

16.3 Theories required by Atomic Activities: Downwards Concurrency

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

16.4 Definitional extensions required by Atomic Activities: Downwards Concurrency

No definitional extension is required by this extension.

16.5 Definitions of Atomic Activities: Downwards Concurrency

The following concepts are defined for Atomic Activities: Downward Concurrency.

16.5.1 Superpose

An activity is a superposition activity if and only if every subactivity is possible whenever the activity itself is possible.

(forall (?a ?s) (iff (superpose ?a ?s)

(forall (?a1)

(implies (and (subactivity ?a1 ?a)

(poss ?a ?s))

(poss ?a1 ?s))))))

16.5.2 Assistance

An activity is an assistance activity if and only if

(forall (?a ?s) (iff (assistance ?a ?s)

(forall (?a1 ?a2)

(implies (and (subactivity ?a1 ?a)

(subactivity ?a2 ?a)

(poss ?a ?s))

(poss (conc ?a1 ?a2 ?s))))))

16.5.3 Team

(forall (?a ?s) (iff (team ?a ?s)

(exists (?a1 ?a2)

(and(subactivity ?a1 ?a)

(subactivity ?a2 ?a)

(poss ?a ?s)

(not (poss (conc ?a1 ?a2 ?s))))))

16.5.4 Ghost

(forall (?a ?s) (iff (ghost ?a ?s)

(forall (?a1)

(implies (and (subactivity ?a1 ?a)
 (poss ?a1 ?s))
 (poss ?a ?s))))))

16.5.5 Conflict

(forall (?a ?s) (iff (conflict ?a ?s)
 (forall (?a1 ?a2)
 (implies (and (subactivity ?a1 ?a)
 (subactivity ?a2 ?a)
 (not (poss ?a1 ?s))
 (poss (conc ?a1 ?a2) ?s))
 (poss ?a ?s))))))

16.5.6 Dysfunction

(forall (?a ?s) (iff (dysfunction ?a ?s)
 (exists (?a1 ?a2)
 (and(subactivity ?a1 ?a)
 (subactivity ?a2 ?a)
 (not (poss ?a1 ?s))
 (not (poss ?a ?s))
 (poss (conc ?a1 ?a2) ?s))))))

16.6 Grammar for Atomic Activities: Downwards Concurrency

The grammar for the process descriptions of Atomic Activities: Downwards Concurrency is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

17 Spectrum of Atomic Activities

This clause characterizes all definitions pertaining to Spectrum of Activities.

17.1 Primitive lexicon of Spectrum of Atomic Activities

No primitive relations are required by the lexicon of Spectrum for Atomic Activities.

17.2 Defined lexicon of Spectrum of Atomic Activities

The following relations are defined in this clause:

- (global_ideal ?a)
- (global_nonideal ?a)
- (global_filter ?a)
- (global_nonfilter ?a)

Each concept is described by informal semantics and a KIF axiom.

17.3 Theories required by Spectrum of Atomic Activities

This theory requires act_occ.th, complex.th, atomic.th, subactivity.th, occtree.th, psl_core.th.

17.4 Definitional extensions required by Spectrum of Atomic Activities

This extension requires Preconditions for Activities.

17.5 Definitions of Spectrum of Atomic Activities

The following concepts are defined for Spectrum of Atomic Activities.

17.5.1 Global_ideal

```
(forall (?a) (iff (global_ideal ?a)
  (forall (?a1 ?s1 ?s2)
    (implies (and (subactivity ?a ?a1)
      (poss ?a ?s1)
      (poss ?a ?s2))
      (poss_equiv ?a1 ?s1 ?s2))))))
```

17.5.2 global_nonideal

```
(forall (?a) (iff (global_nonideal ?a)
  (forall (?a1 ?s1 ?s2)
    (implies (and (subactivity ?a ?a1)
      (not (poss ?a ?s1))
      (not (poss ?a ?s2)))
      (poss_equiv ?a1 ?s1 ?s2))))))
```

17.5.3 global_filter

An activity is a global filter activity if and only if every subactivity has equivalent preconditions whenever the activity is possible.

```
(forall (?a) (iff (global_filter ?a)
  (forall (?a1 ?s1 ?s2)
    (implies (and (subactivity ?a1 ?a)
      (poss ?a ?s1)
      (poss ?a ?s2))
      (poss_equiv ?a1 ?s1 ?s2))))))
```

17.5.4 global_nonfilter

```
(forall (?a) (iff (global_nonfilter ?a)
  (forall (?a1 ?s1 ?s2)
    (implies (and (subactivity ?a1 ?a)
      (not (poss ?a ?s1))
      (not (poss ?a ?s2)))
      (poss_equiv ?a1 ?s1 ?s2))))))
```

17.6 Grammar for Spectrum for Atomic Activities

The grammar for the process descriptions of Spectrum for Atomic Activities is equivalent to the grammar of a general process description sentence specified in ISO 18629-11.

Annex A**Normative****ASN.1 Identifier of ISO 18629-41**

To provide for unambiguous identification of an information object in an open system, the object identifier

iso standard 18629 part 41 version 1

is assigned to this part of ISO 18629. The meaning of this value is defined in ISO/IEC 8824-1 and is described in ISO 18629-1.

Annex B

Normative

Scope of ISO 18629-4x series

The parts 4x of ISO 18629 specify definitional extensions needed to give precise definitions and the axiomatization of non-primitive concepts of ISO 18629. Definitional extensions are extensions of ISO 18629-11 and ISO 18629-12 that introduce new items for the lexicon. The items found in definitional extensions can be completely defined in terms of the ISO 18629-11- and ISO18629-12. The definitional extensions provide precise semantic definitions for elements used in the specification of individual applications or types of applications for the purpose of interoperability. Definitional extensions exist in the following categories:

- Activity Extensions;
- Temporal and State Extensions;
- Activity Ordering and Duration Extensions;
- Resource Roles;
- Resource Sets
- Processor Activity Extensions

Individual users or groups of users of ISO 18629 may need to extend ISO 18629 for specifying concepts that are currently absent in ISO 18629-4x. They shall use the elements presented in ISO 18629 for doing so. User-defined extensions and their definitions constitute definitional extensions but shall not become part of ISO 18629-4x.

Note: User-defined extensions must conform to ISO18629 as defined in clause 5.1 and 5.2, ISO 18629-1.

The following are within the scope of ISO 18629-4x:

- the semantic definitions, using concepts in ISO 18629-11 and ISO 18629-12, of elements that are specific to the six concepts outlined above;
- a set of axioms for constraining the use of elements in definitional extensions.

The following is outside the scope of ISO 18629-4x:

- definitions and axioms for concepts that are part of the ISO18629-11 and ISO 18629-12;
- elements that are not defined using the elements in ISO18629-11 and ISO 18629-12;
- user-defined extensions.

Annex C (informative)

Example of process description using ISO 18629-41

The purpose of this annex is to provide a detailed scenario in which the ISO 18629 PSL is used in a knowledge-sharing effort which involves multiple manufacturing functions.

This scenario is an "interoperability" manufacturing scenario. This means that its goal is to show how PSL can be used to facilitate the communication of process knowledge in a manufacturing environment. Specifically, this scenario is centred around the exchange of knowledge from a process planner to a job shop scheduler.

This annex extends the test case introduced in ISO 18629-11 annex C to illustrate the application of outercore concepts in the specification of the manufacturing process of a product named GT-350.

C.1 GT-350 Manufacturing Processes

This section unites the various departmental processes into a high-level collection of activities which are enacted to create a GT-350 product. As described in the GT-350 product structure (table 1), subcomponents of this product are either purchased, sub-contracted, or made internally. These process descriptions address the activities performed to manufacture the internal subcomponents. This top-down view of the manufacturing process provides an overall picture from an abstract, "make GT350" activity which is expanded down to the detailed departmental levels.

As the Figure C.1 below shows, the GT-350 manufacturing process is divided into 6 main areas of work. The first five: make interior, make drive, make trim, make engine and make chassis are all unordered with respect to each other but they must all be completed before final assembly takes place.

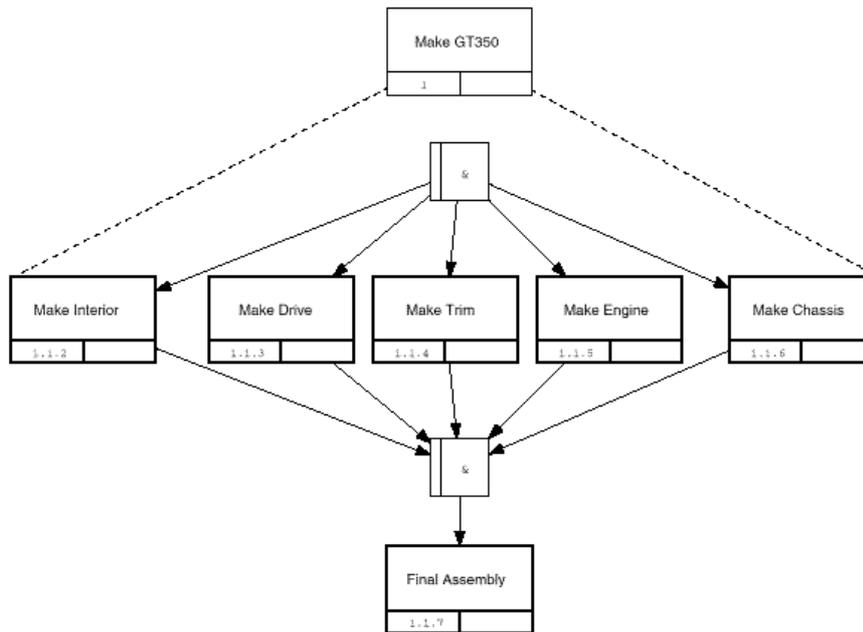


Figure C1: TOP level process for manufacturing a GT350

The PSL-Outercore-based representation of the top level process is :

(subactivity make-chassis make_gt350)

(subactivity make-interior make_gt350)

(subactivity make-drive make_gt350)

(subactivity make-trim make_gt350)

(subactivity make-engine make_gt350)

(subactivity final-assembly make_gt350)

(permuted make_gt350)

(ordered make_gt350)

(rigid make_gt350)

(amorphous make_gt350)

(uniform make_gt350)

(unrestricted make_gt350)

(not (atomic make_gt350))

(forall (?occ)

 (iff (occurrence_of ?occ make_gt350)
 (exists (?occ1 ?occ2 ?occ3 ?occ4 ?occ5 ?occ6)
 (and(occurrence_of ?occ1 make_chassis)
 (occurrence_of ?occ2 make_interior)
 (occurrence_of ?occ3 make_drive)
 (occurrence_of ?occ4 make_trim)
 (occurrence_of ?occ5 make_engine)
 (occurrence_of ?occ6 final_assembly)
 (subactivity_occurrence ?occ1 ?occ)
 (subactivity_occurrence ?occ2 ?occ)
 (subactivity_occurrence ?occ3 ?occ)
 (subactivity_occurrence ?occ4 ?occ)
 (subactivity_occurrence ?occ5 ?occ)
 (subactivity_occurrence ?occ6 ?occ)

(forall (?s1 ?s2 ?s3 ?s4 ?s5 ?s6)

 (implies (and (leaf_occ ?s1 ?occ1)
 (leaf_occ ?s2 ?occ2)
 (leaf_occ ?s3 ?occ3)
 (leaf_occ ?s4 ?occ4)
 (leaf_occ ?s5 ?occ5)
 (root_occ ?s6 ?occ6))
 (and (min_precedes ?s1 ?s6 make_gt350)
 (min_precedes ?s2 ?s6 make_gt350)
 (min_precedes ?s3 ?s6 make_gt350)
 (min_precedes ?s4 ?s6 make_gt350)

(min_precedes ?s5 ?s6 make_gt350))))))))

Each of these abstract activities can be further detailed, however for the example proposed in this annex, we will not develop all of them.

On the basis of the IDEF3 representation (in terms of process representation) of the abstract activities met during the different stages of the manufacturing process, we will extract some examples of process descriptions using the PSL-Outercore presented in this part 12 of the ISO 18629 standard.

C.2 The "make-engine" abstract activity

The 350-Engine is assembled from work performed in several CMW departments. The manufacturing process is shown in Figure C.2. The part is made up of an engine block, a harness, and wiring. The sub-processes are detailed in the sub-sections below. The 350-Engine is assembled at the A004 assembly bench and takes 5 minutes per piece.

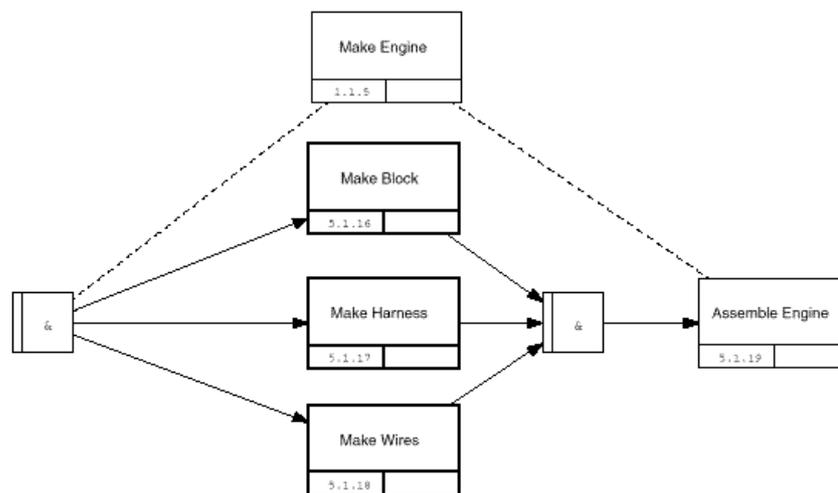


Figure C.2: PROCESS for manufacturing the 350-Engine

The PSL-Outercore-based representation of some activities and of the process related information at the make-engine stage is :

(subactivity make_block make_engine)

(subactivity make-harness make_engine)

(subactivity make-wires make_engine)

(subactivity assemble_engine make_engine)

(permuted make_engine)

(ordered make_engine)

(rigid make_engine)

(amorphous make_engine)

(uniform make_engine)

(unrestricted make_engine)

(not (atomic make_engine))

(forall (?occ)

(iff(occurrence_of ?occ make_engine)

(exists (?occ1 ?occ2 ?occ3 ?occ4)

(and(occurrence_of ?occ1 make_block)

(occurrence_of ?occ2 make_harness)

(occurrence_of ?occ3 make_wires)

(occurrence_of ?occ4 assemble_engine)

(subactivity_occurrence ?occ1 ?occ)

(subactivity_occurrence ?occ2 ?occ)

(subactivity_occurrence ?occ3 ?occ)

(subactivity_occurrence ?occ4 ?occ)

(forall (?s1 ?s2 ?s3 ?s4)

(implies (and (leaf_occ ?s1 ?occ1)

(leaf_occ ?s2 ?occ2)

(leaf_occ ?s3 ?occ3)

(root_occ ?s4 ?occ4))

(and (min_precedes ?s1 ?s4 make_engine)

(min_precedes ?s2 ?s4 make_engine)

(min_precedes ?s3 ?s4 make_engine))))))

C.3 Make Block

The 350-Block is manufactured as part of the 350-Engine sub-assembly. This involves an integration of work from the foundry and machine shop, as shown in the Figure C.3.

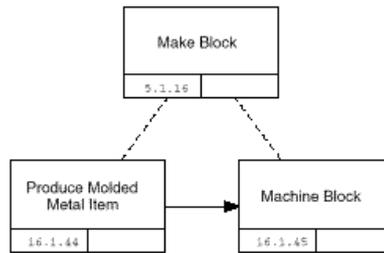


Figure C.3: PROCESS for manufacturing the 350-Block

The PSL-Outercore-based representation of some activities and of the process related information is :

(subactivity produce_molded_metal make_block)

(subactivity machine_block make_block)

(primitive machine_block)

(primitive produce_molded_metal)

(permuted make_block)

(ordered make_block)

(rigid make_block)

(amorphous make_block)

(uniform make_block)

(unrestricted make_block)

(not (atomic make_block))

(forall (?occ)

(iff (occurrence_of ?occ make_block)

(exists (?occ1 ?occ2)

(and(occurrence_of ?occ1 produce_molded_metal)

(occurrence_of ?occ2 machine_block)

(min_precedes ?occ1 ?occ2 make_block))))))

C.4 Make Harness

The 350-Harness (Figure C.4) is manufactured as part of the 350-Engine sub-assembly. This involves work performed at the wire and cable department. Figure C.5 expands the harness wire production process. The 350-Harness is assembled by a bench worker at a wire and cable bench. It takes 10 minutes per set.

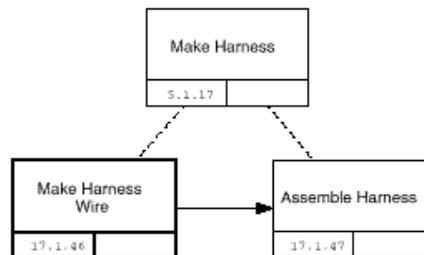


Figure C.4: PROCESS for manufacturing the 350-Harness

The PSL-Outercore-based representation of some activities and of the process related information is :

(subactivity make_harness_wire make_harness)

(subactivity assemble_harness make_harness)

(primitive assemble_harness)

(permuted make_harness)

(ordered make_harness)

(rigid make_harness)

(amorphous make_harness)

(uniform make_harness)

(unrestricted make_harness)

(not (atomic make_harness))

(forall (?occ)

(iff (occurrence_of ?occ make_harness)

(exists (?occ1 ?occ2 ?occ3)

(and(occurrence_of ?occ1 make_harness_wire)

(occurrence_of ?occ2 assemble_harness)
 (leaf_occ ?occ3 ?occ1)
 (min_precedes ?occ3 ?occ2 make_harness))))))

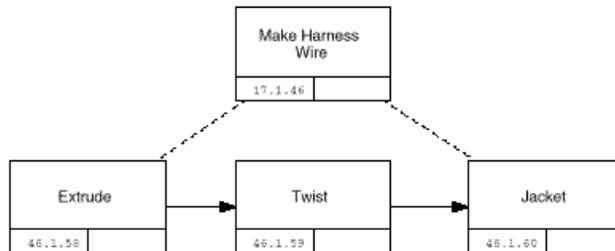


Figure C.5: PROCESS for manufacturing the harness wire

C.5 Make Harness Wires

The 350-Wire-Set is manufactured as part of the 350-Engine sub-assembly. This involves work performed at the wire and cable department.

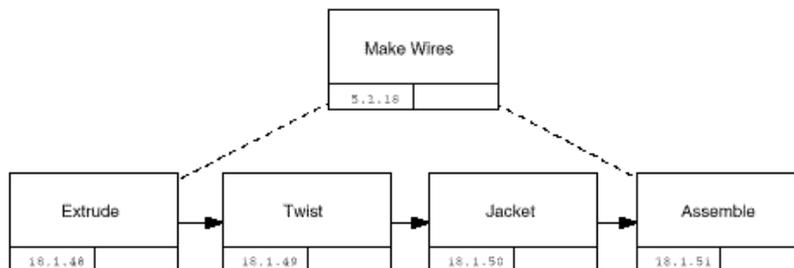


Figure C.6 : Process for manufacturing the 350-Wire

The PSL-Outercore-based representation of some activities and of the process related information is :

(subactivity extrude make_harness_wire)

(subactivity twist make_harness_wire)

(subactivity jacket make_harness_wire)

(primitive extrude)

(primitive twist)

(primitive jacket)

(permuted make_harness_wire)

(ordered make_harness_wire)

(rigid make_harness_wire)

(amorphous make_harness_wire)

(uniform make_harness_wire)

(unrestricted make_harness_wire)

(not (atomic make_harness_wire))

(forall (?occ)

 (iff (occurrence_of ?occ make_harness_wire)

 (exists (?occ1 ?occ2 ?occ3)

 (and(occurrence_of ?occ1 extrude)

 (occurrence_of ?occ2 twist)

 (occurrence_of ?occ3 jacket)

 (min_precedes ?occ1 ?occ2 make_harness_wire)

 (min_precedes ?occ2 ?occ3 make_harness_wire))))))

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