



Cuprate Superconductors: Towards materials specific calculations

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Acknowledgements

Collaborators:

Mark Jarrell, Alexandru Macridin / UC

Thomas Maier, Thomas Schulthess / ORNL

Ole K. Andersen, Tanusri Dasgupta, Ove
Jepsen / MPI Stuttgart

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DOE / CMSN

Computer time:

Cray XI / ORNL

Figures:

superconductors.org

DOE

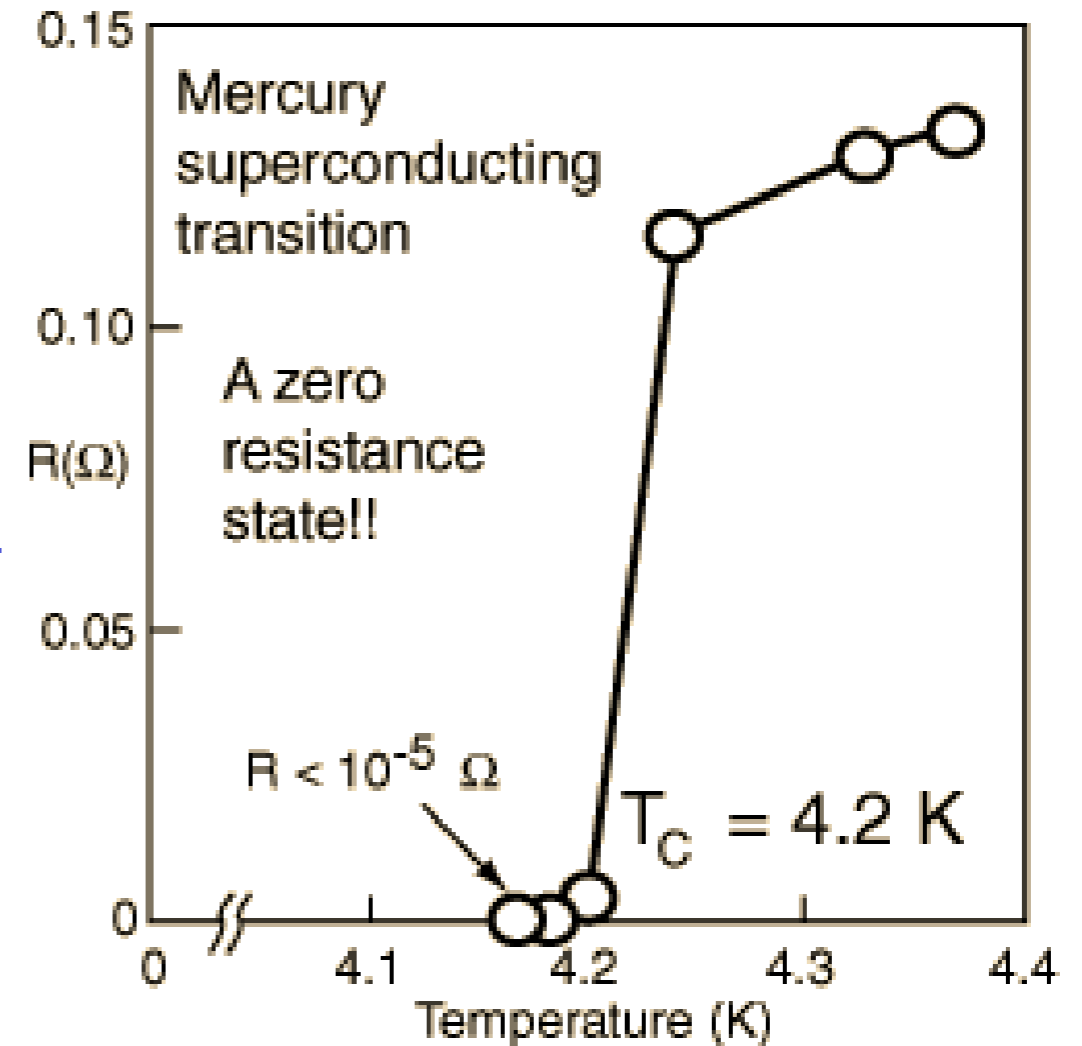
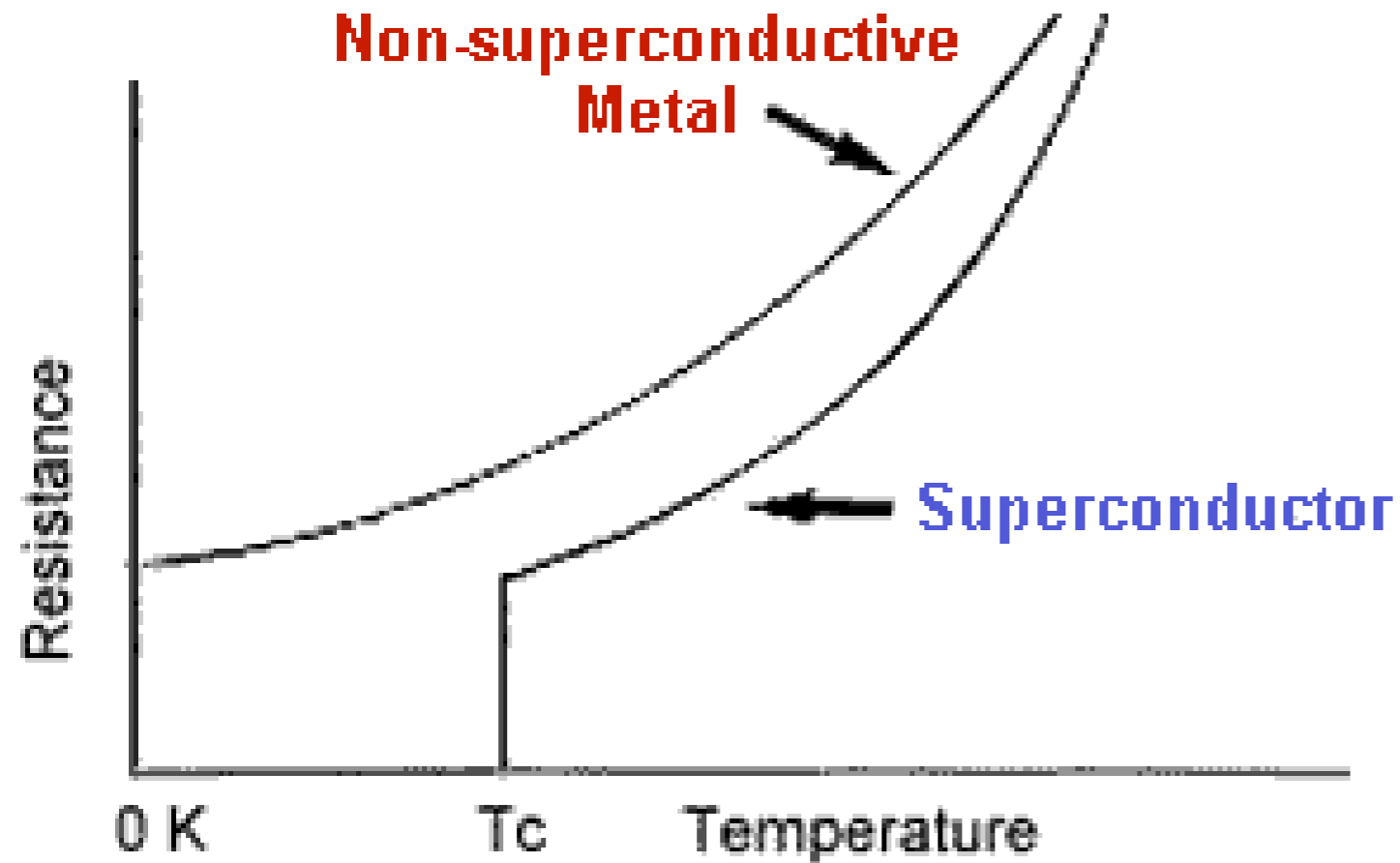
APS

Outline

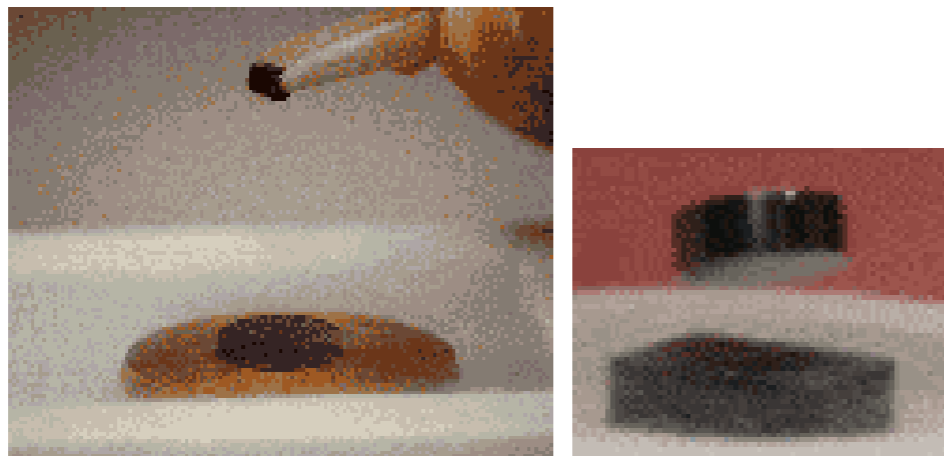
1. Superconductivity Background
2. Model theories (?)
3. Materials specific simulation (?)
4. Next Steps and Summary

Superconductivity

Superconductivity in Mercury



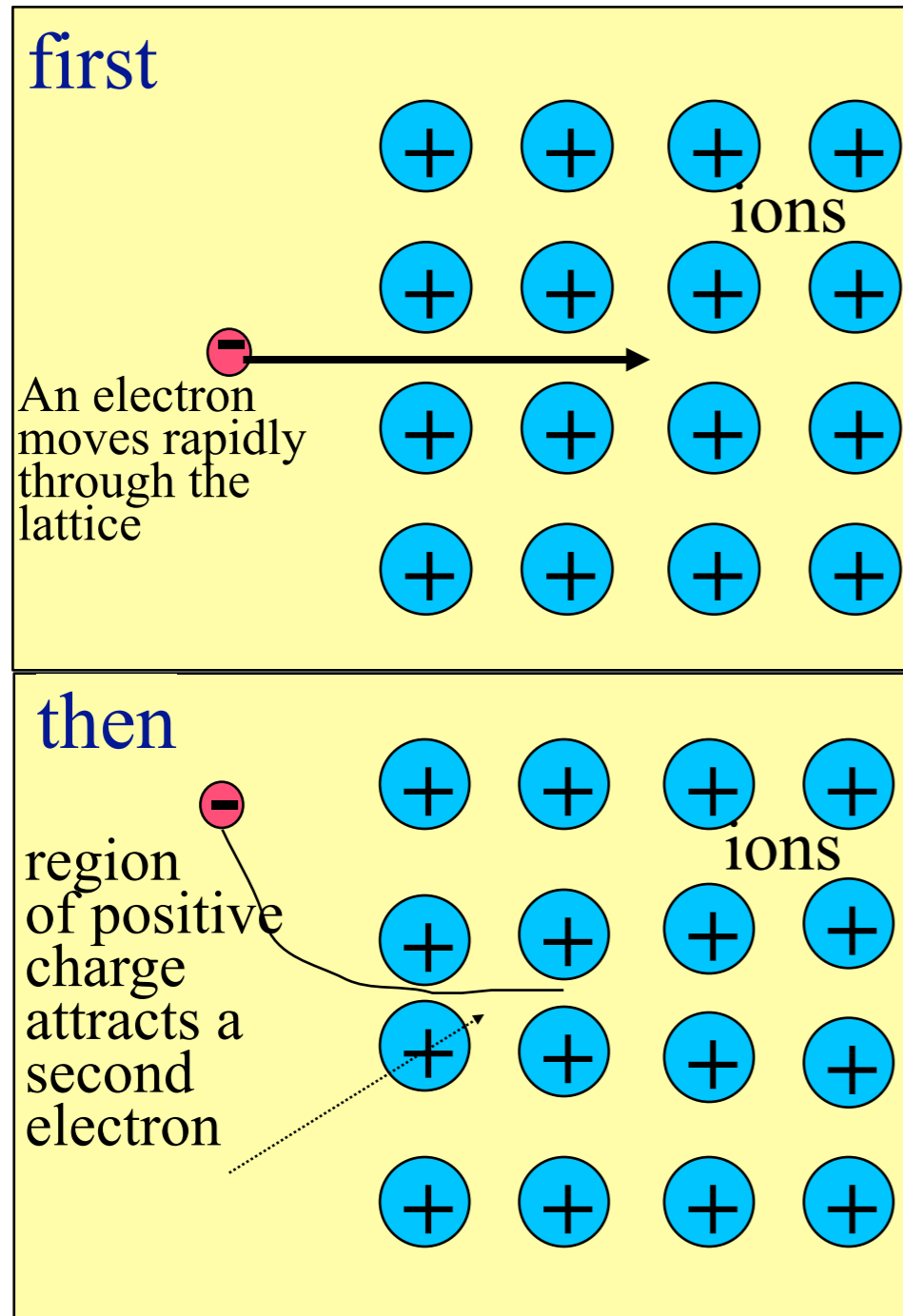
H.K. Onnes, Commun. Phys. Lab. **12** 120 (1911).



H. K. Onnes
1913 Nobel Prize (He)

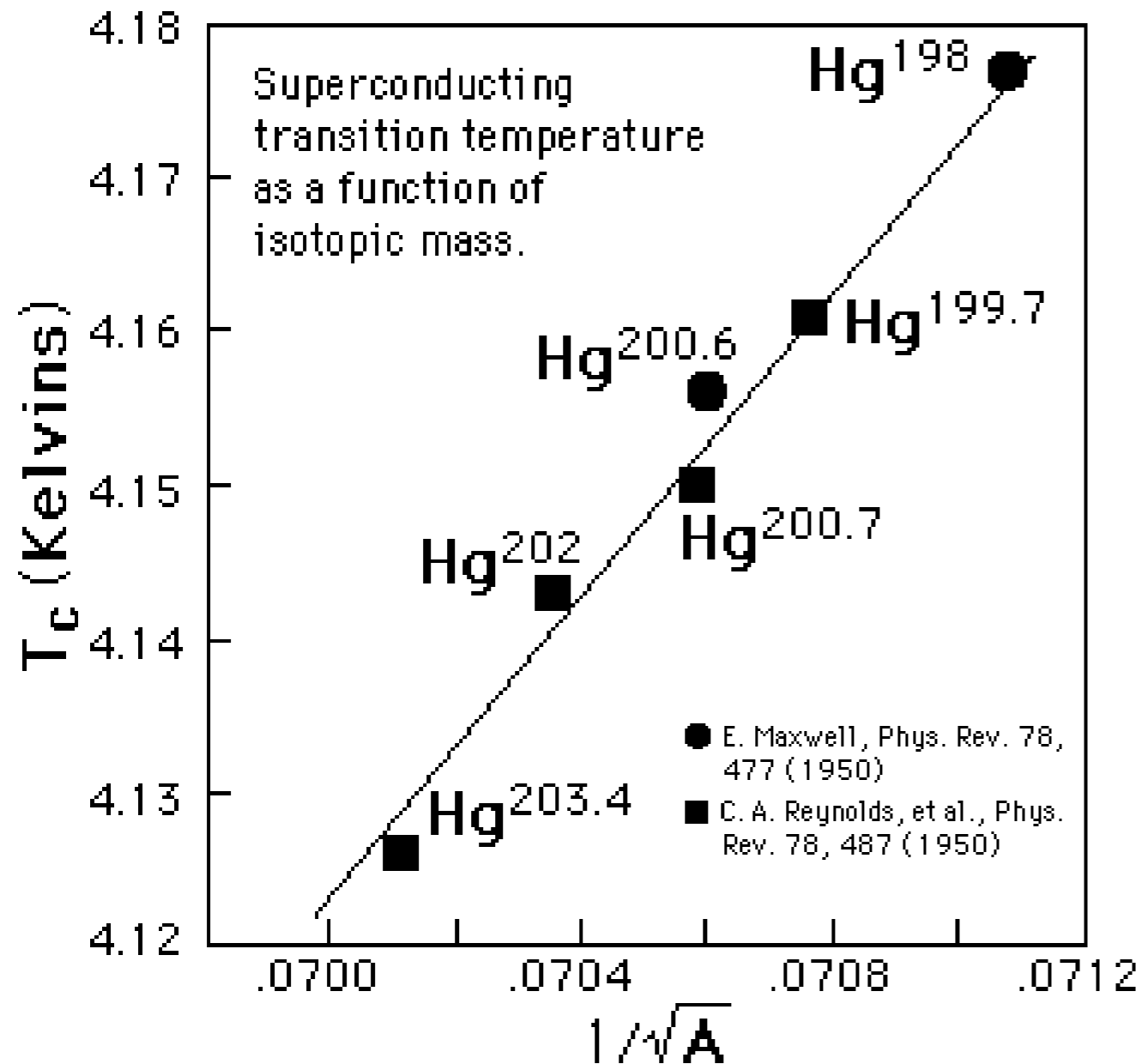


Conventional Superconductors



- Pairing due to phonon-mediated pairing potential
- Fermi-liquid Normal State
- Moderately Correlated Systems
- s-wave

The Isotope Effect (the smoking gun)



BCS

$$T_c = \omega_D e^{-1/N(0)V}$$

Migdal-Eliashberg

$$\approx \frac{\omega_D}{E_F}$$

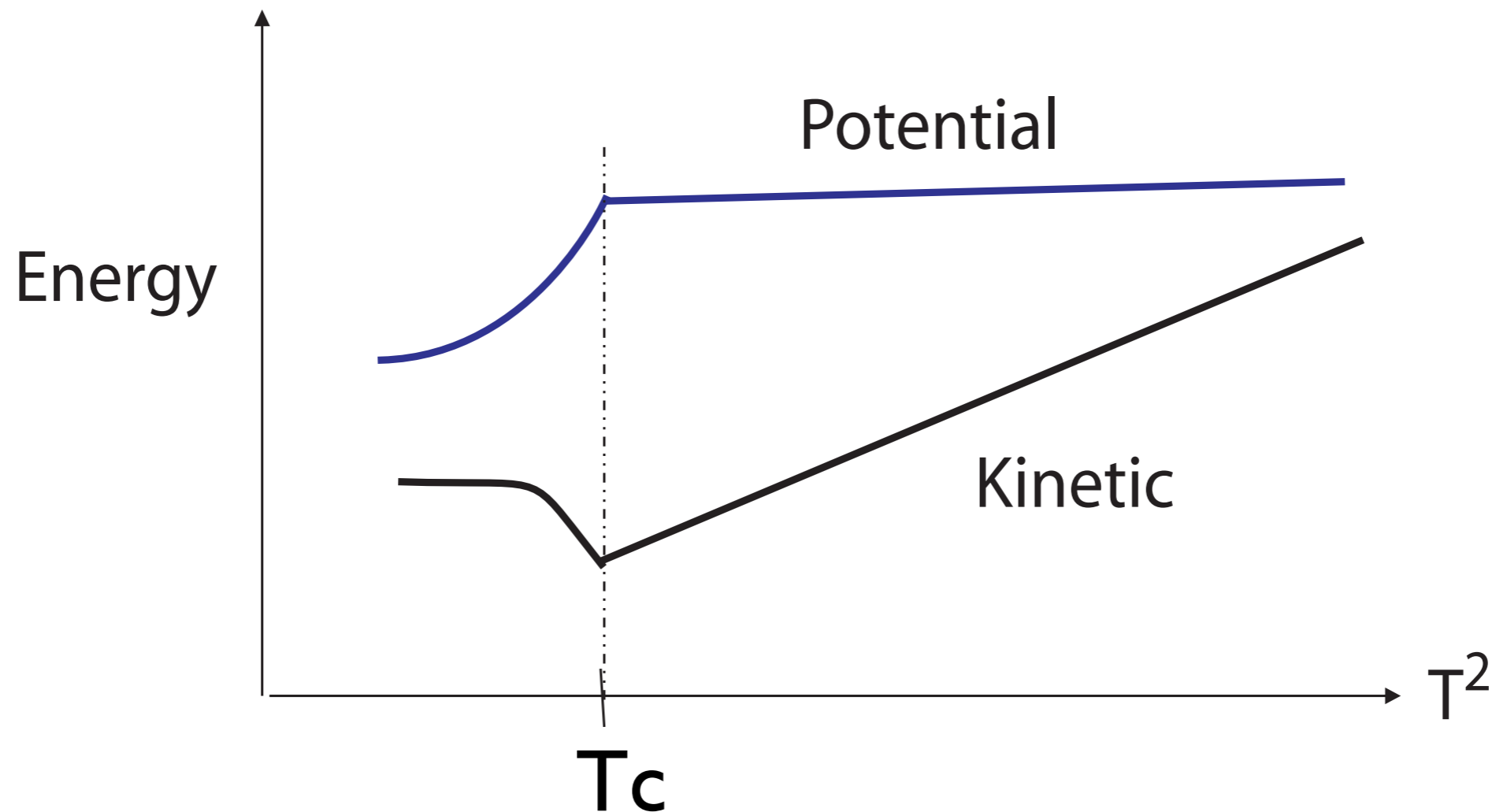
local approximation

$$\Sigma(\mathbf{k}, \omega) \approx \Sigma(\omega)$$

BCS



Pairing is due to potential energy recovery

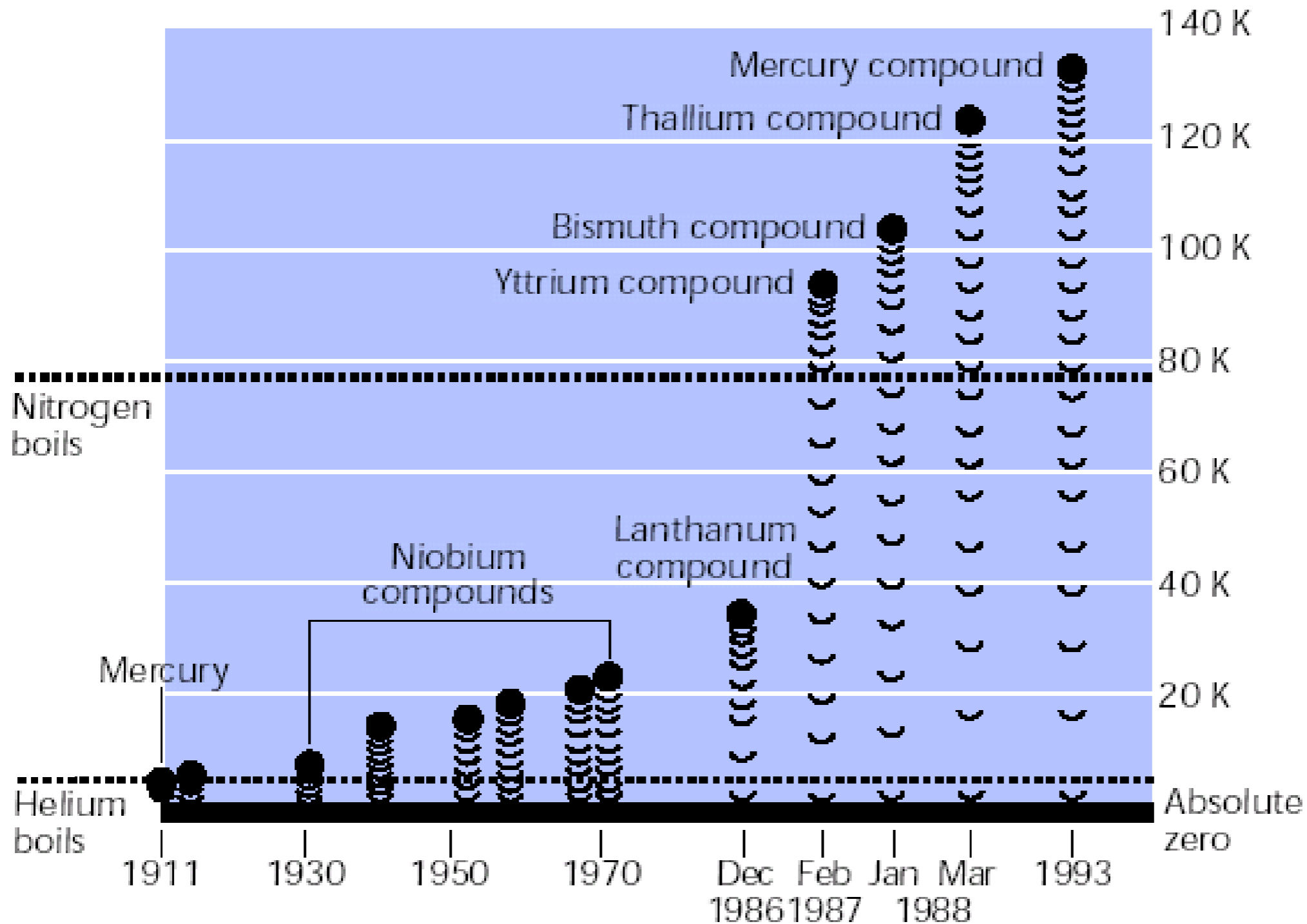
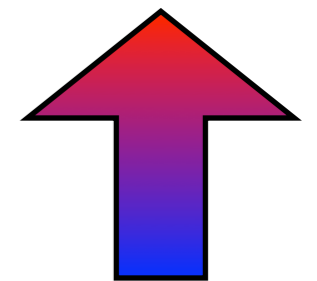


System recovers substantial potential energy by forming pairs. However, paired electrons must occupy states outside the Fermi sea, i.e. states with an increased kinetic energy.

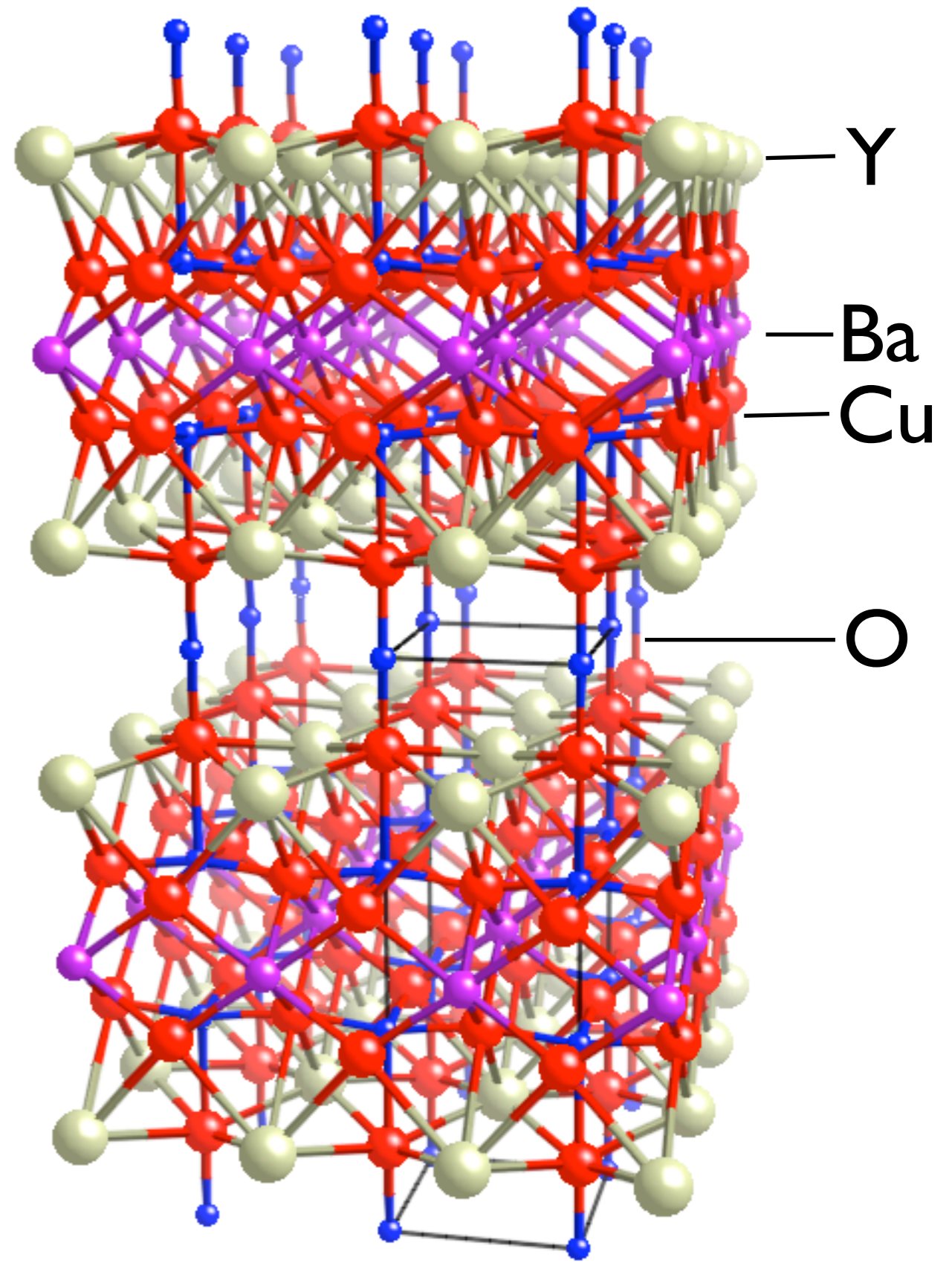
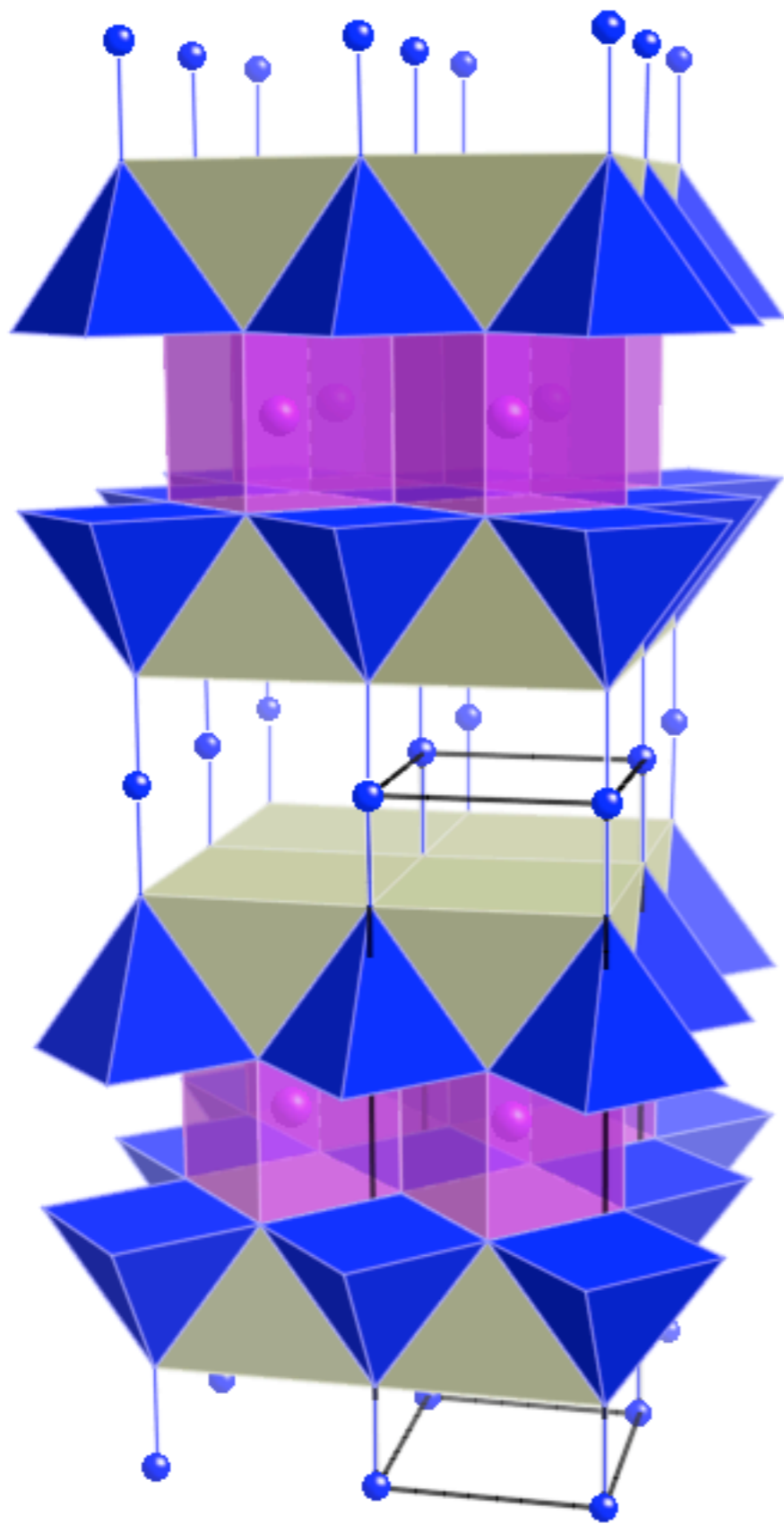
New superconductors ('86)

Pressure

168K

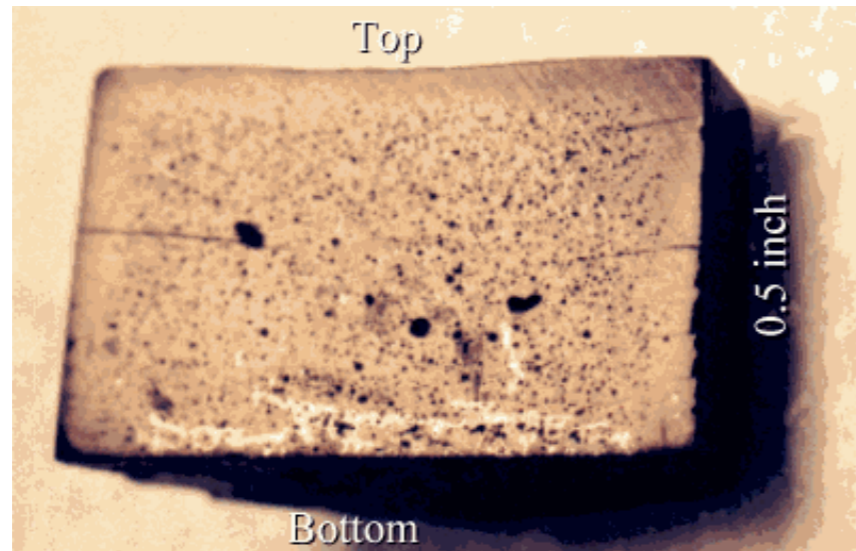


DOE figure

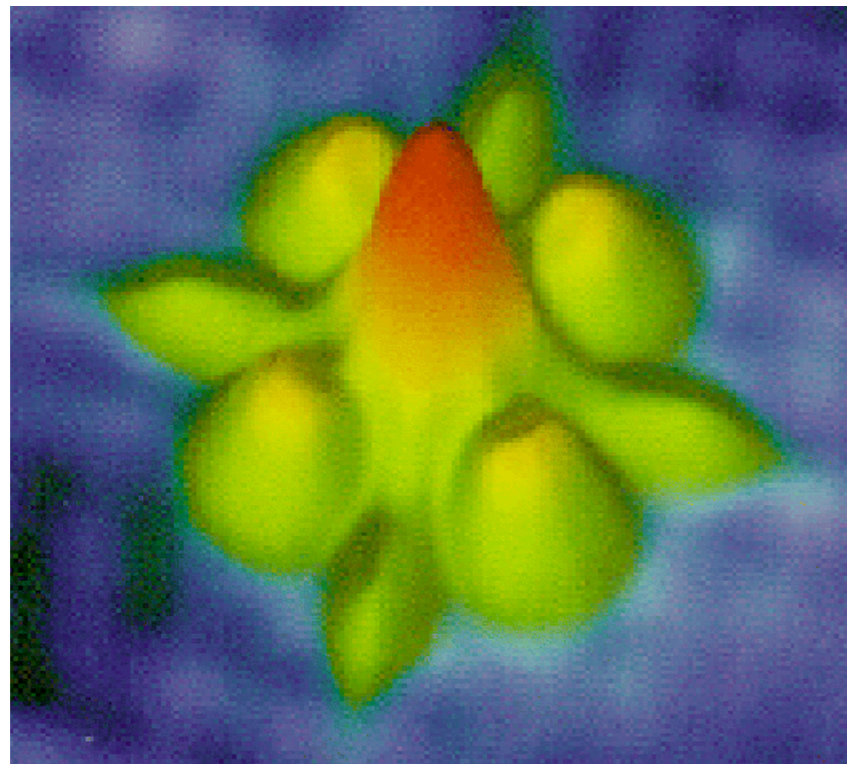


YBa₂Cu₃O₆

Cuprates: Unusual Superconductors



Ceramic material



S. Pan, dI/dV at resonance

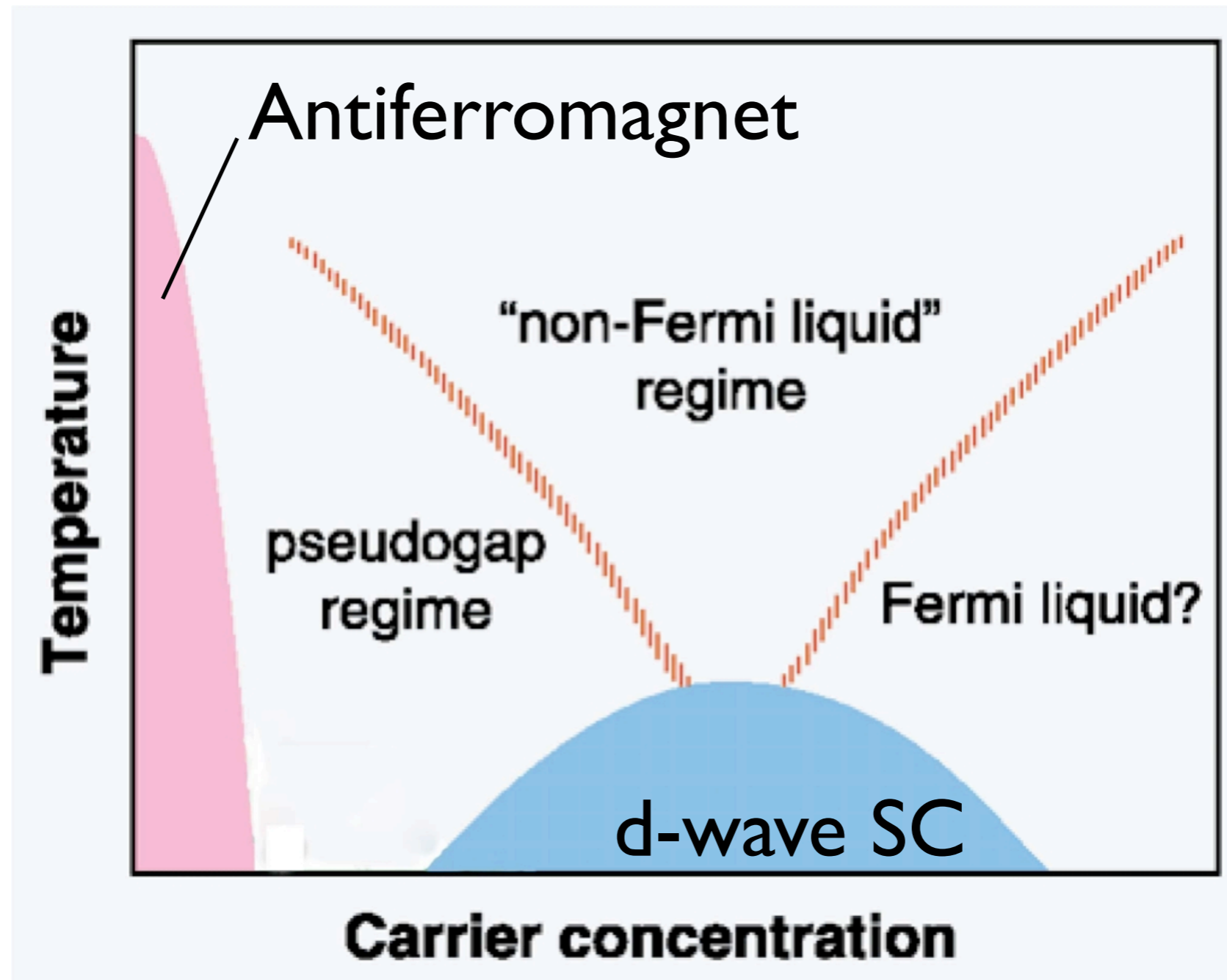
- No BCS-like phonon/isotope “smoking gun”
- Mechanism?
- Non-Fermi liquid underdoped normal state (pseudogap)
- Doped Mott insulator
- d-wave
- Kinetically Driven Pairing



Alex Müller and Georg Bednorz
1987 Nobel Prize

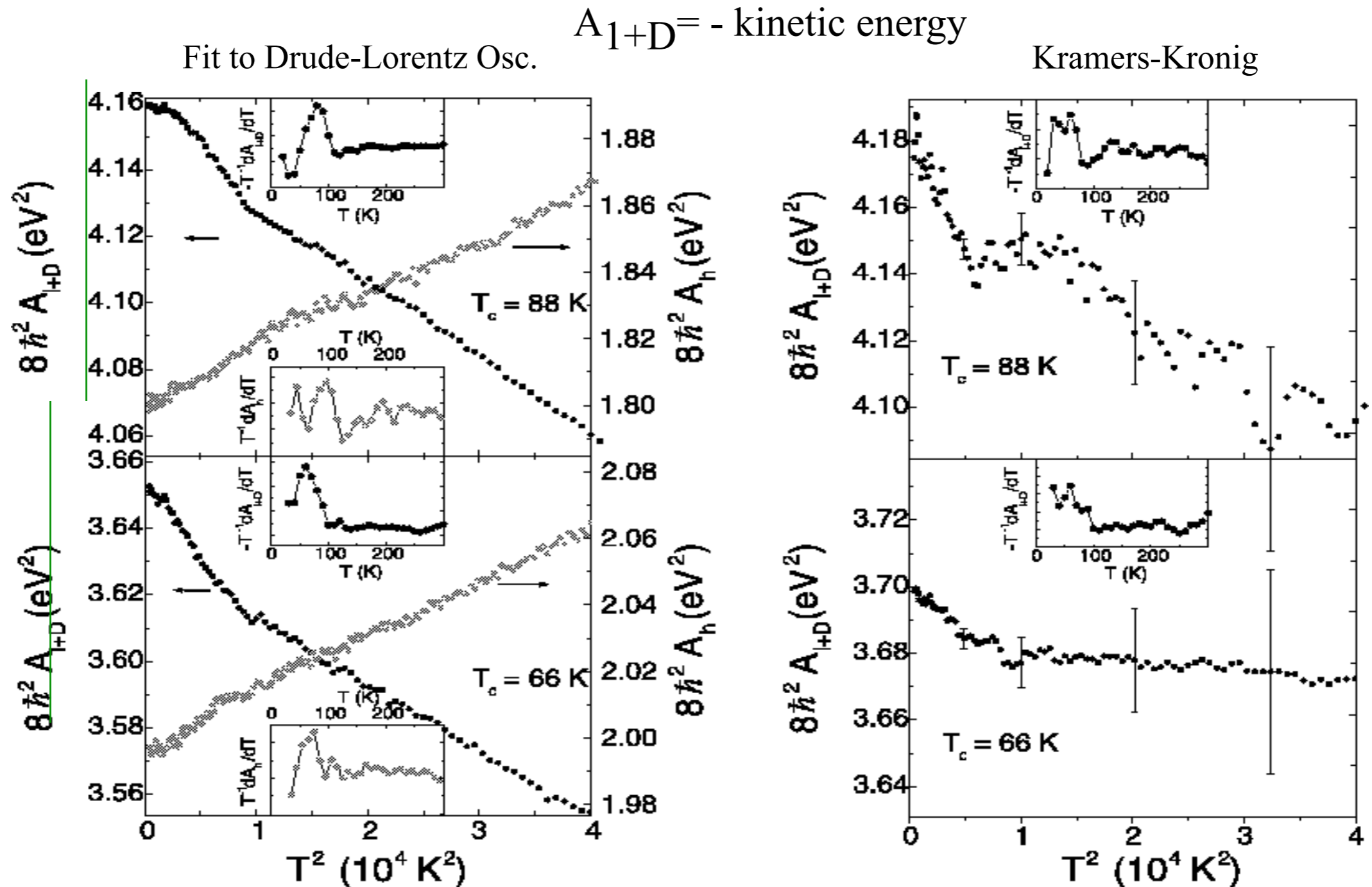
Complex phase diagram

Unlike BCS, must dope to $\sim 15\%$ holes for highest T_c



Kinetic Energy Reduction (opposite of BCS)

From spectroscopic ellipsometry. Bi2Sr2CaCu2O8 samples. Molegraaf Science **295** 2239 (2002)



Kinetic Energy **reduction** is roughly **1meV** > condensation energy!

Meanwhile...

(Back in the real world)



ADVANCED ELECTRICITY SOLUTIONS

American Superconductor Corporation (Nasdaq: AMSC) is a world-leading supplier of dynamic reactive power grid stabilization products and the world's principal vendor of high temperature superconductor (HTS) wire and large rotating superconductor machinery.

WHICH PRODUCT IS RIGHT FOR YOU?

- ▶ HTS Wire
- ▶ Motors, Generators & Synchronous Condensers
- ▶ Industrial Power Quality Solutions
- ▶ Power Conversion

American Superconductor Announces Continued Rapid Advancement in 2G Technology



Industrial manufacture of
 HTSC wires, power machinery
 (motors, generators)
 exploiting high current
 densities achievable

Outstanding questions

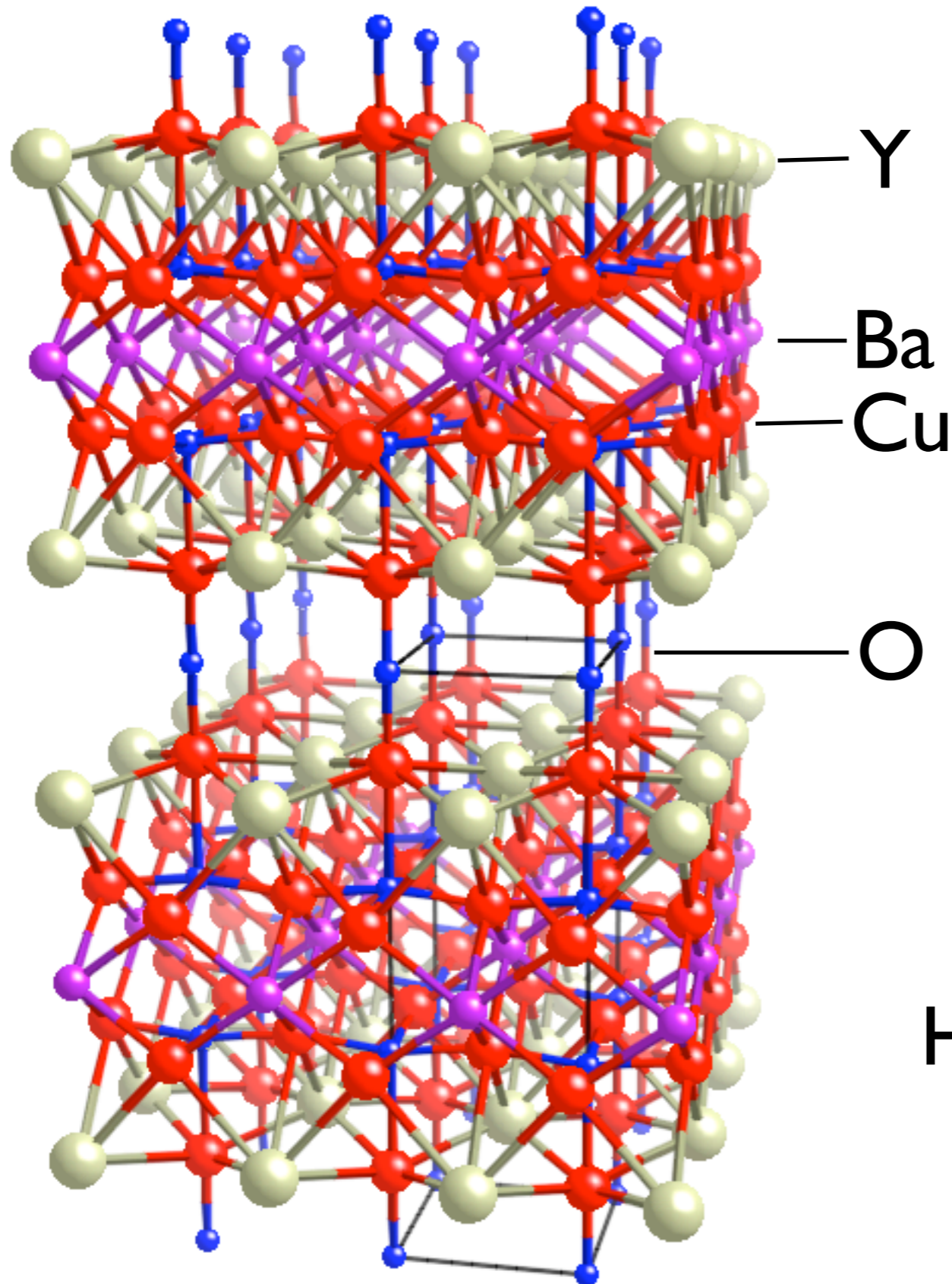
(19 years later)

- What is the principal mechanism?
 - Electrons? Phonons? Both? Other?
- Does material A,B, or C have higher T_c ?
- Influence of pressure, magnetic fields?
- Other materials with same mechanism?
c.f. new BCS-like MgB₂ in 2001, 39K
- ...many others

Outline

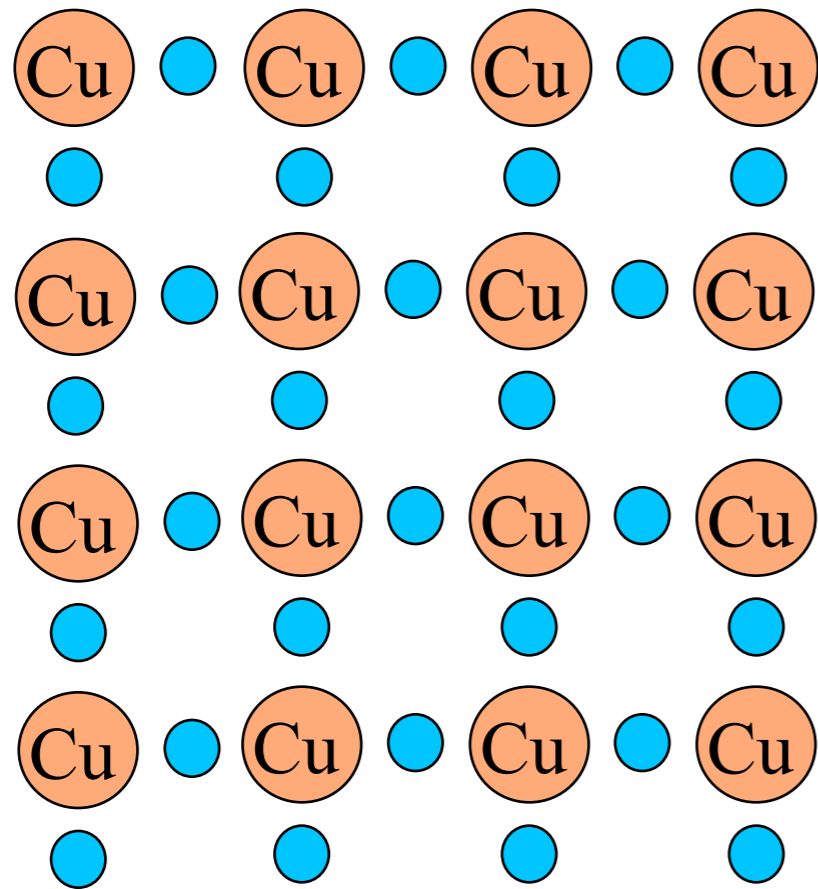
1. Superconductivity Background
2. Model theories
 - a. Hubbard model
 - b. DCA simulations
3. Materials specific simulation
4. Next Steps and Summary

Focus on Cu-O layers

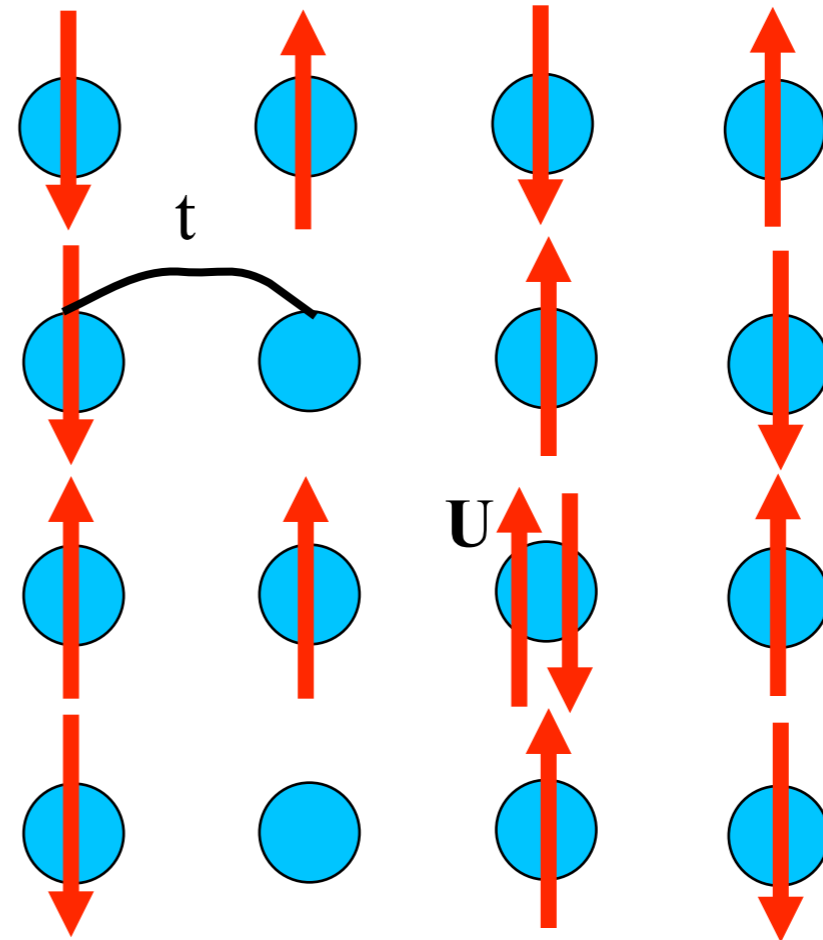


Quasi 2D system
SC is in plane
Half-filled when undoped
Antiferromagnet

The Hubbard Model of the Cuprates



CuO₂ Planes

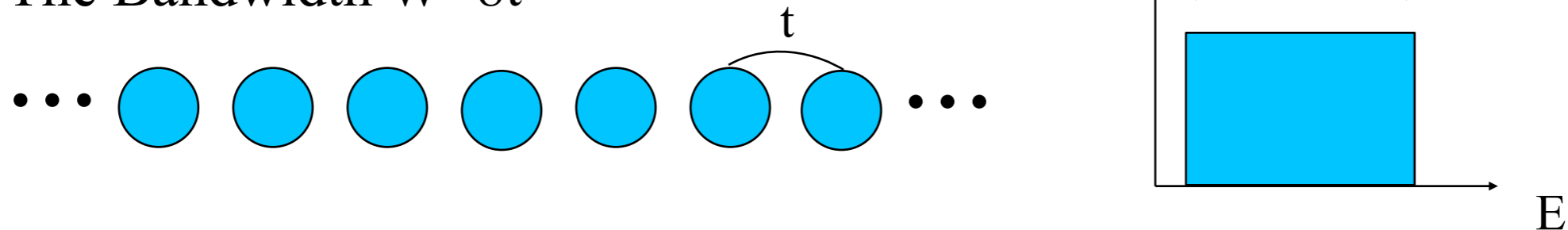


Hubbard Model with $8t = W \approx U$
Anderson 87, Zhang-Rice 88

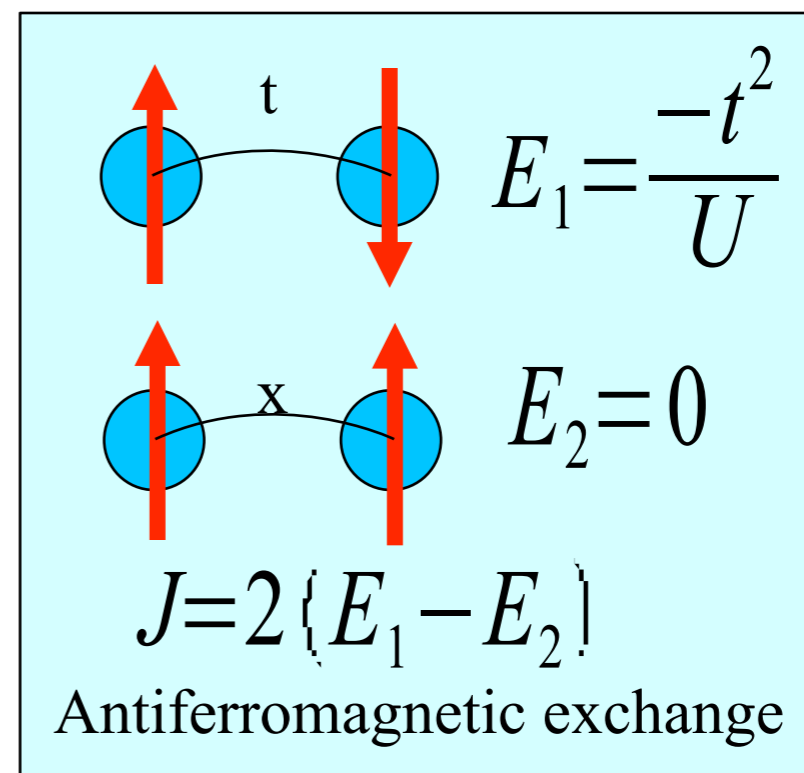
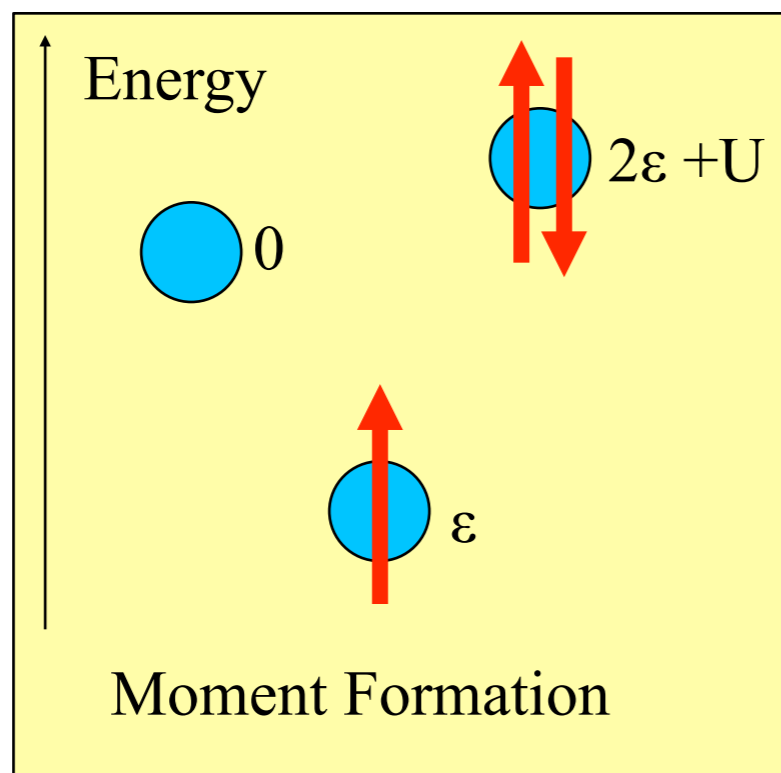
Note: A few model parameters (t, U) fit to experiment

The Energy Scales in the Hubbard Model

The Bandwidth $W=8t$



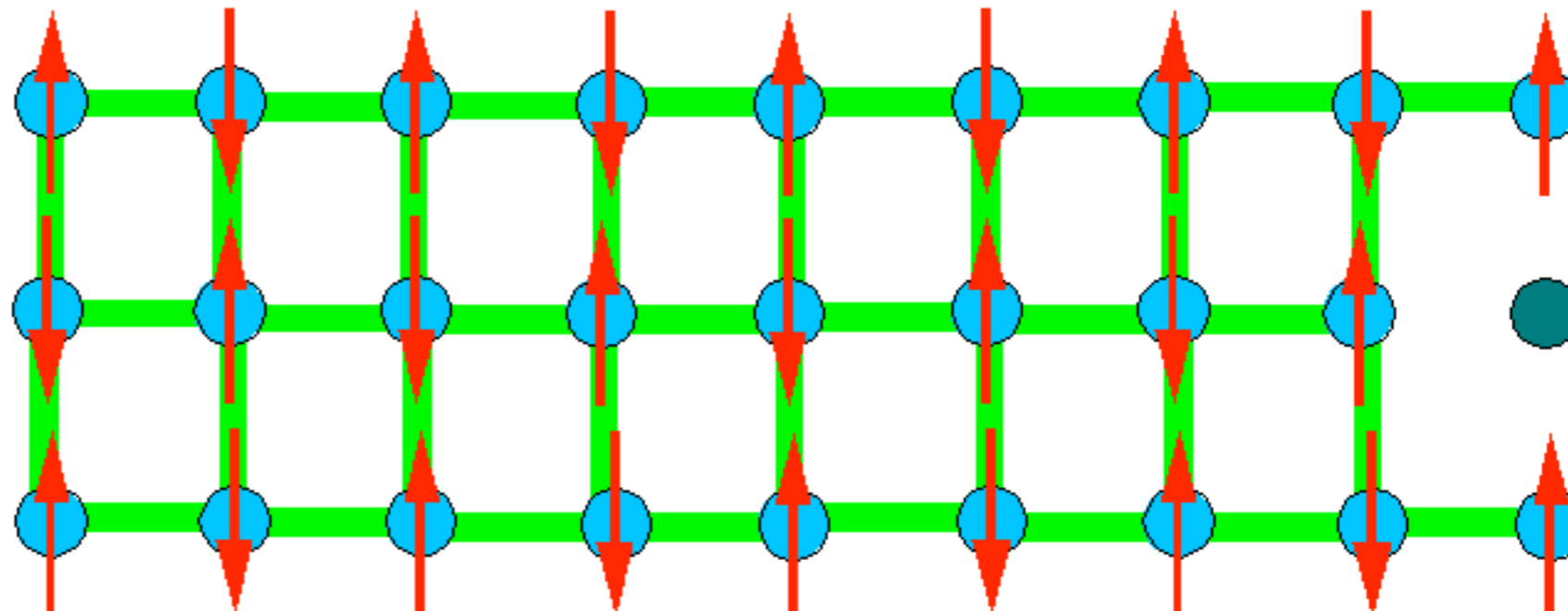
The local Coulomb repulsion U



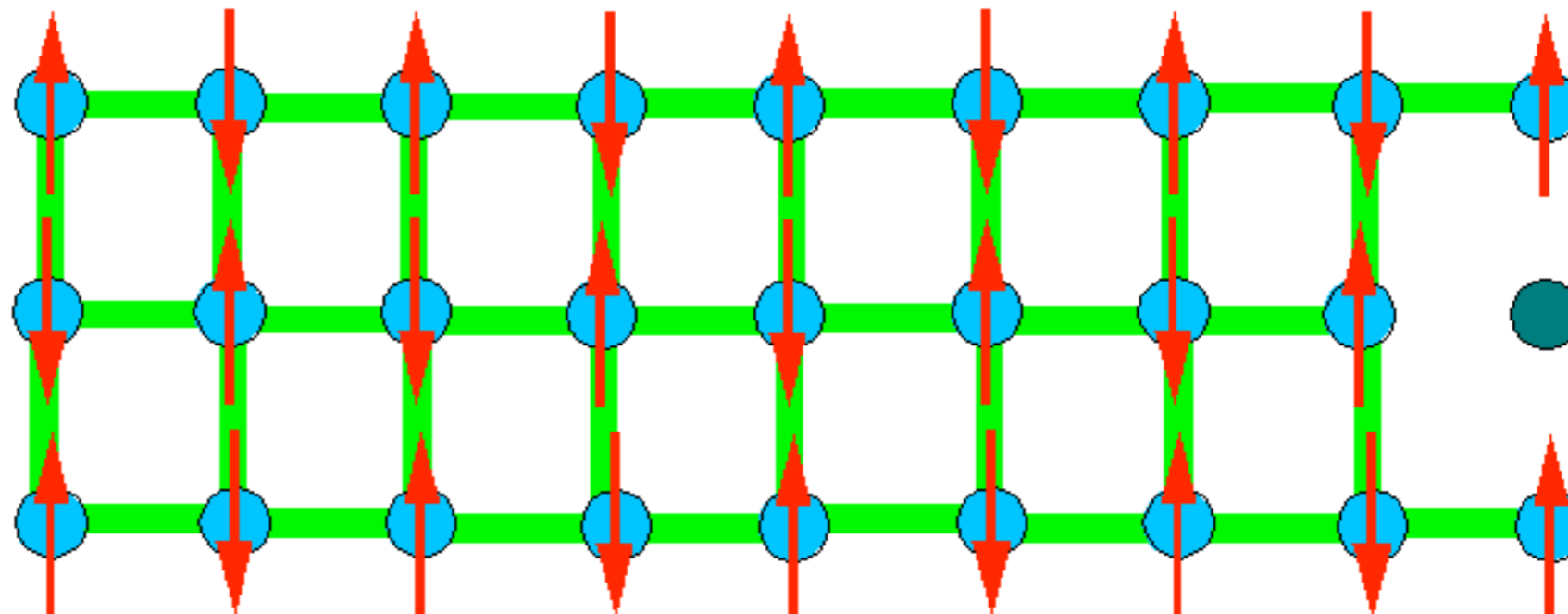
Note: A few model parameters (t, U) fit to experiment

Pairing Mechanism: Holes in AF background

One hole motion
breaks AF bonds



A bound second
hole restores the
AF bonds



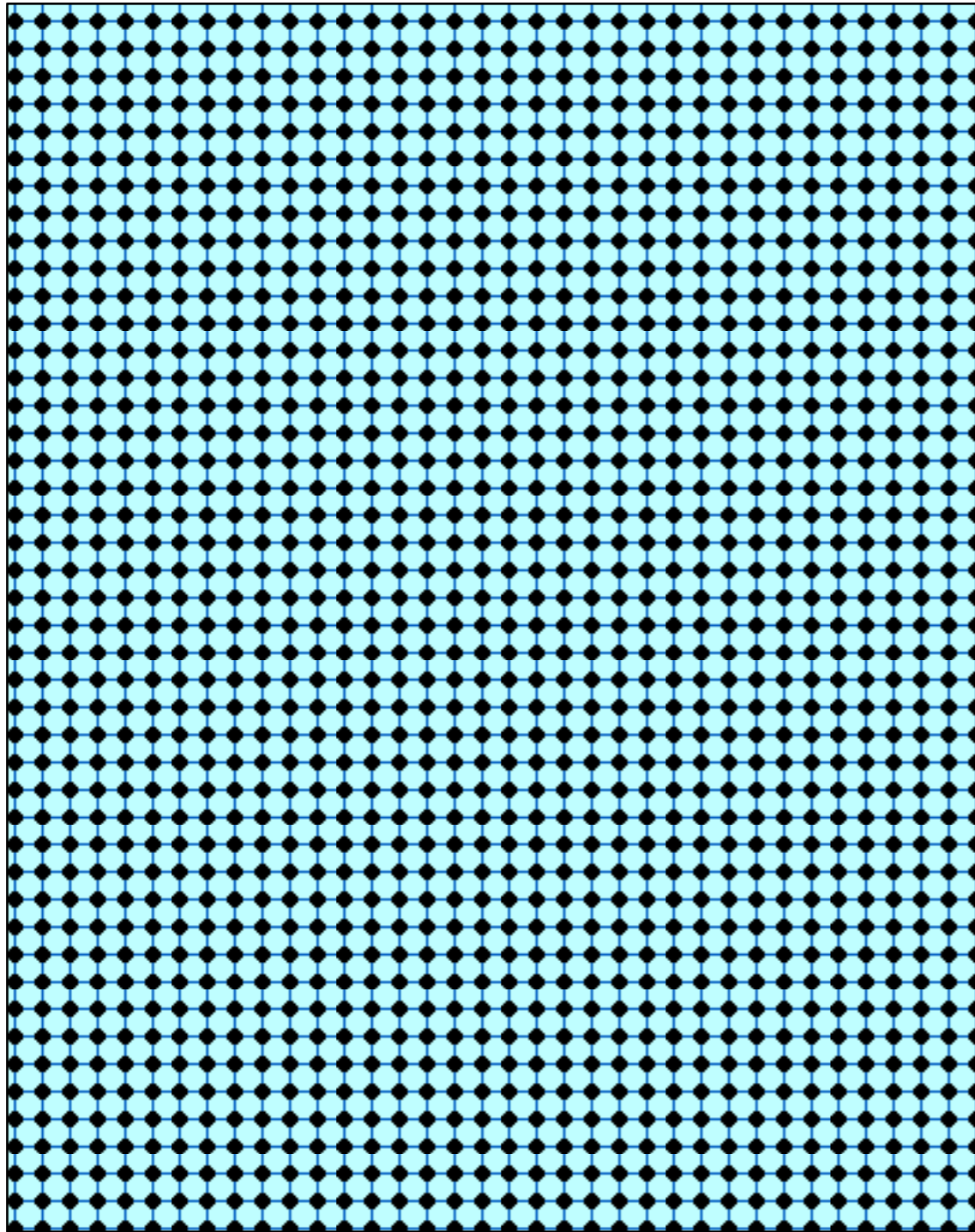
Brinkman 1970, Bonca 1989, Hirsch Science 2002

Pseudogap due to SRO or pre-formed pairs, Pairing due to kinetic energy gain

Outline

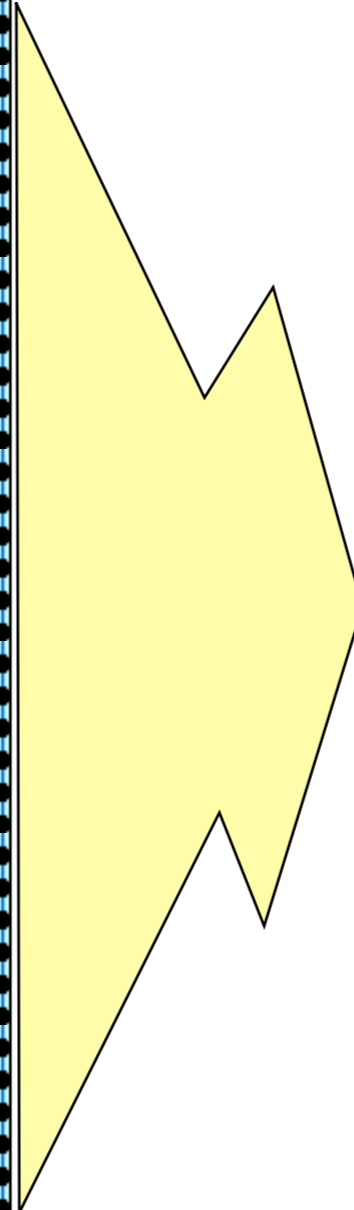
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Periodic Lattice



Difficult to solve accurately directly

Dynamical Cluster Approximation

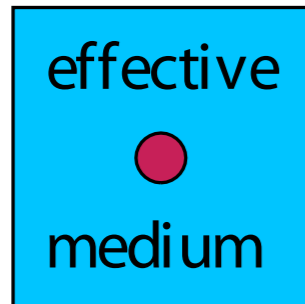


Solve self-consistently

Cluster Approximations

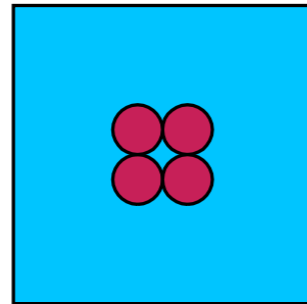
Dynamical Cluster Approximation: Expansion around the DMF/CPA Solutions

$N_c = 1$

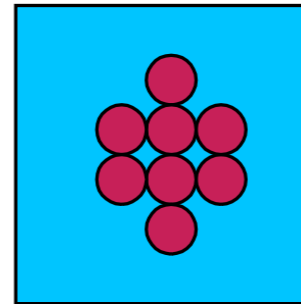


DMFA

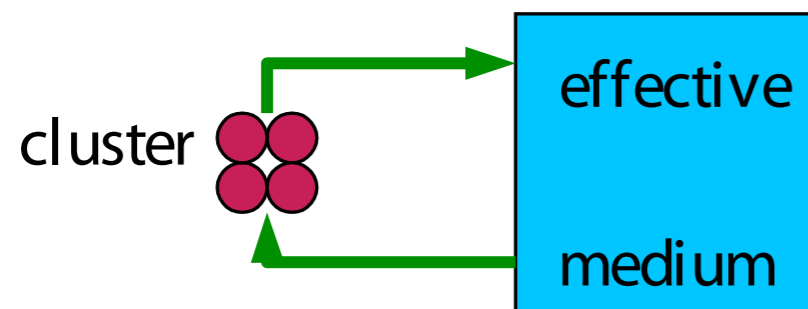
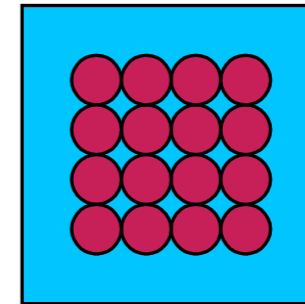
$N_c = 4$



$N_c = 8$



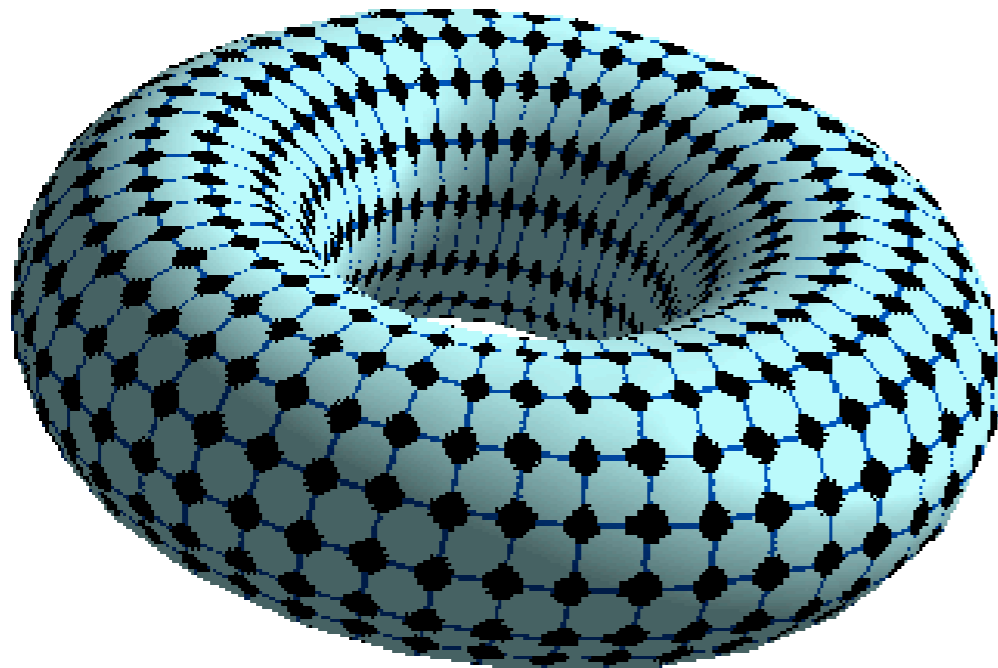
$N_c = 16$



$$\sum_{\text{lattice}} \approx \sum_{\text{cluster}}$$

DCA papers <http://www.physics.uc.edu/~jarrell>

We Solve The Cluster Problem with Quantum Monte Carlo (QMC)



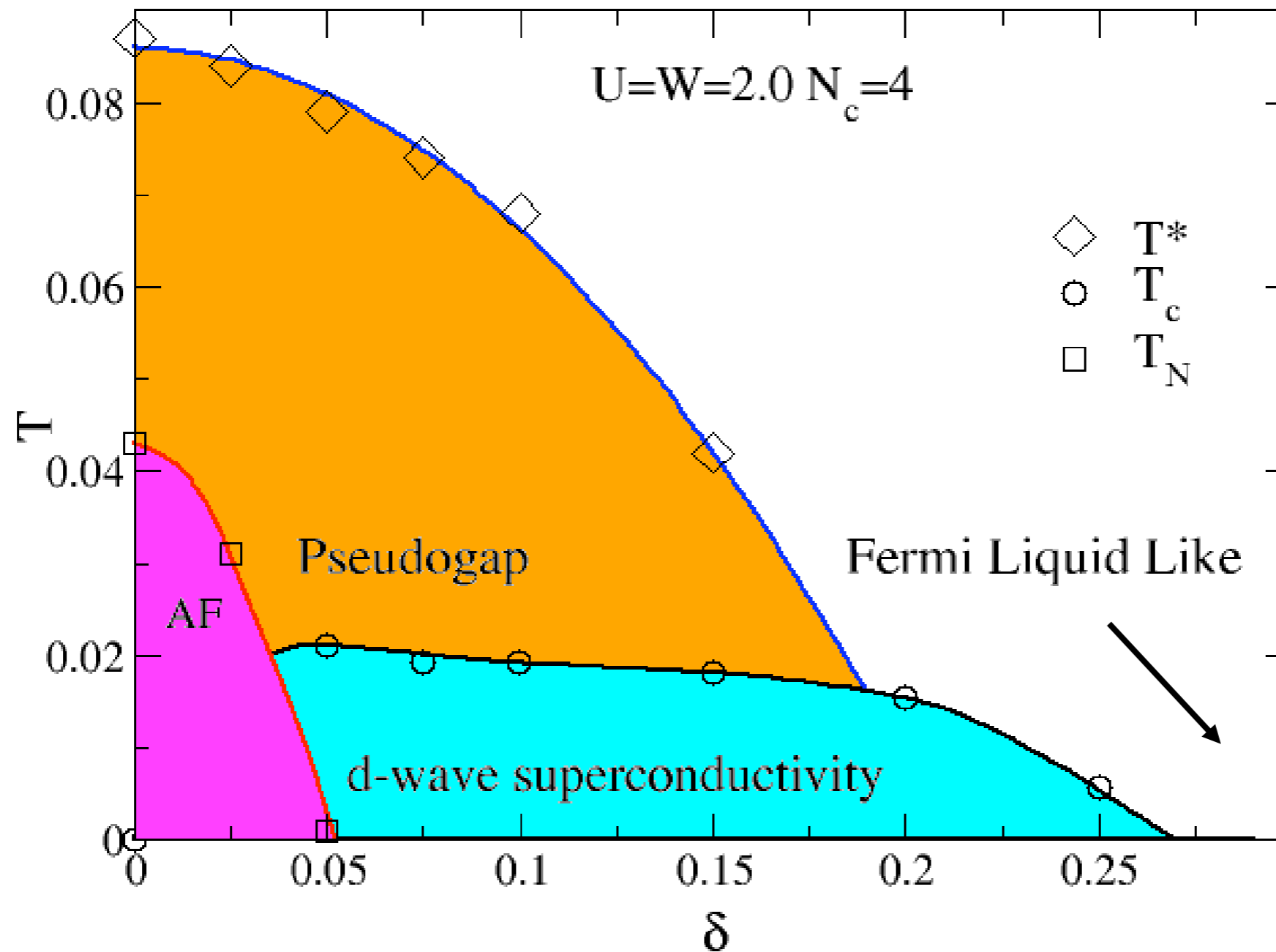
ORNL/CCS and
OSC CRAY X1



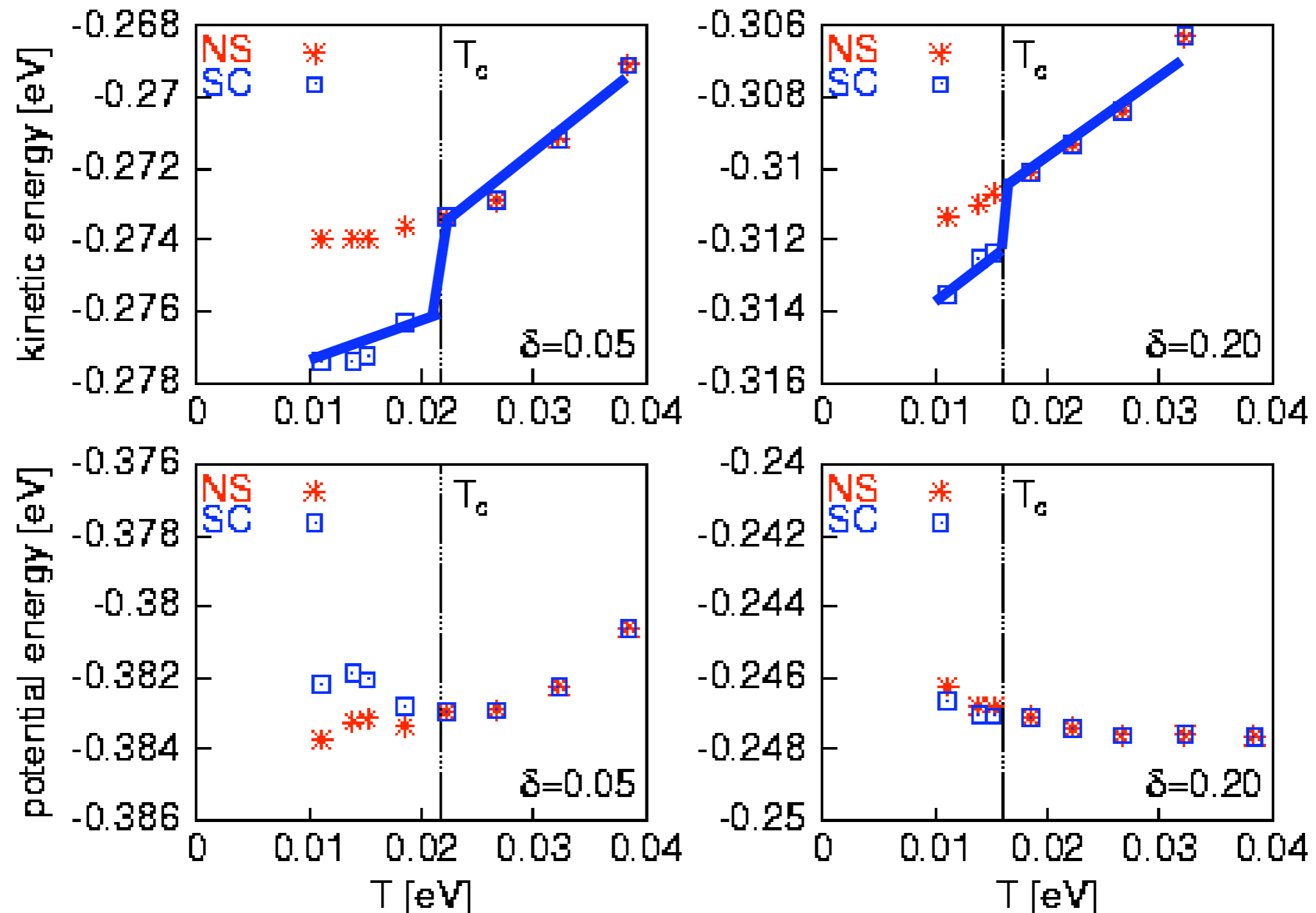
Expensive! 1-1000+ cpu hours per temperature and doping
Many temperatures and dopings per phase diagram

Small cluster results

Phase Diagram $N_c=4$



Energies for $T < T_c$



Kinetic energy reduction entering SC phase

Small cluster DCA Hubbard calculations display key features of cuprate phase diagram

Outline

1. Superconductivity Background
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Outstanding questions

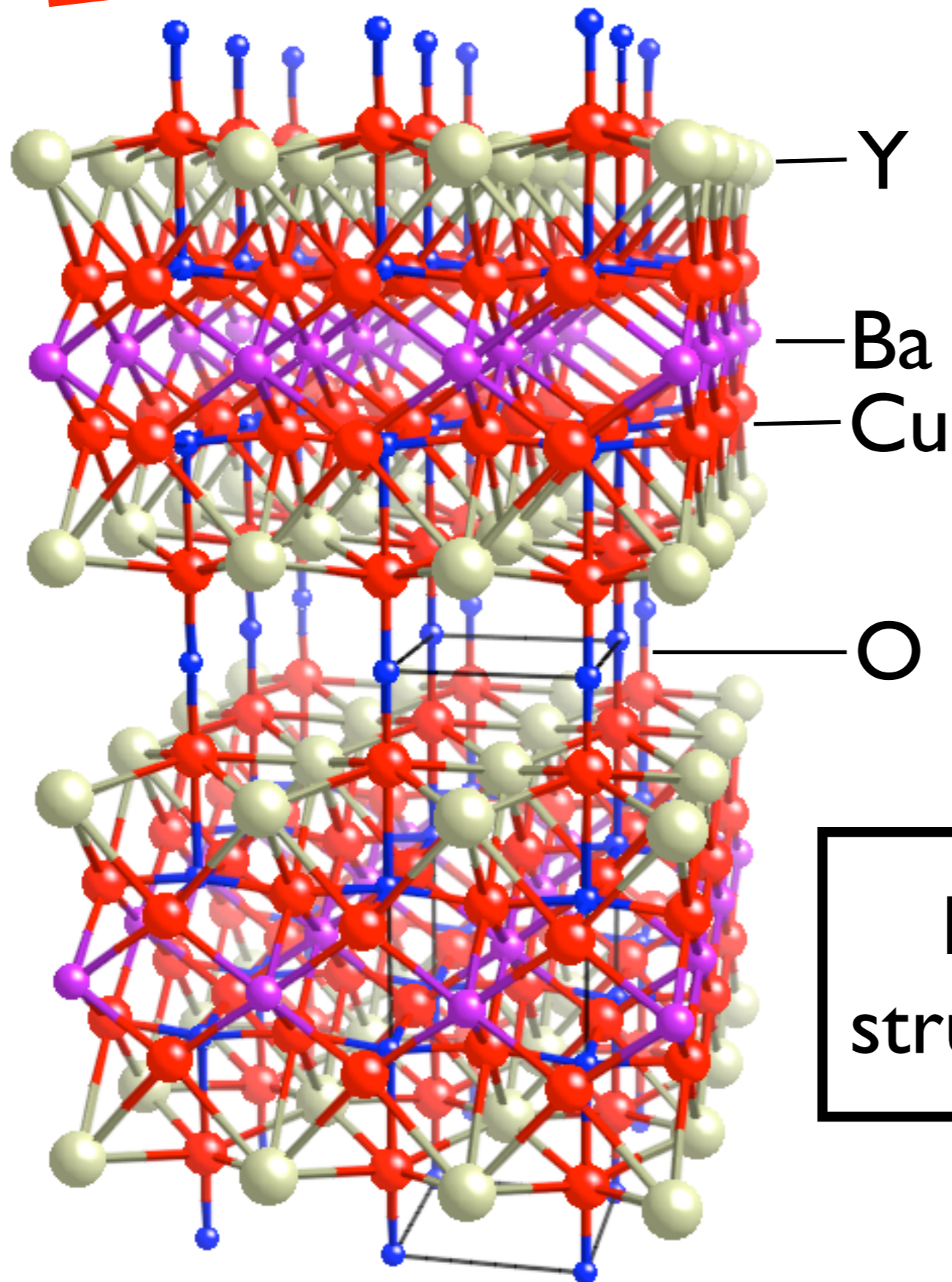
(19 years later)

- What is the principal mechanism?
 - Electrons? Phonons? Both? Other?

Mostly electronic

- Does material A,B, or C have higher T_c ?
- Influence of pressure, magnetic fields?
- Other materials with same mechanism?
 - c.f. new BCS-like MgB₂ in 2001, 39K

~~Focus on Cu-O layers~~

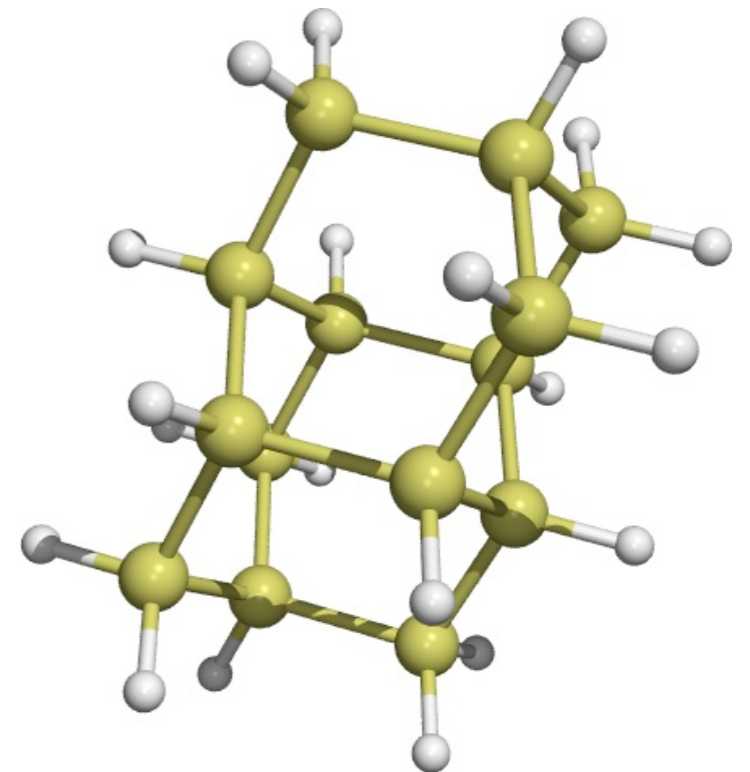
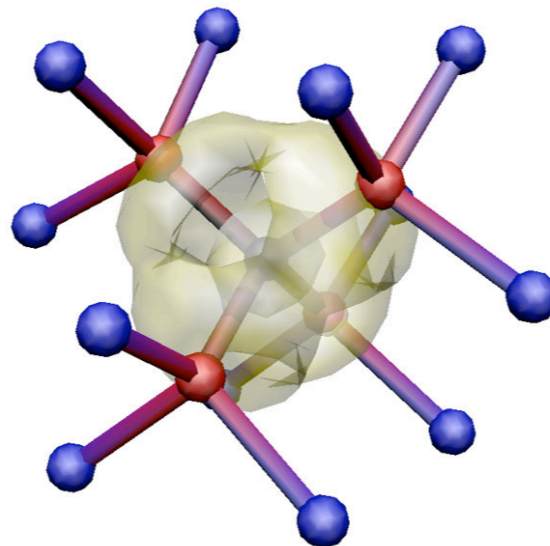
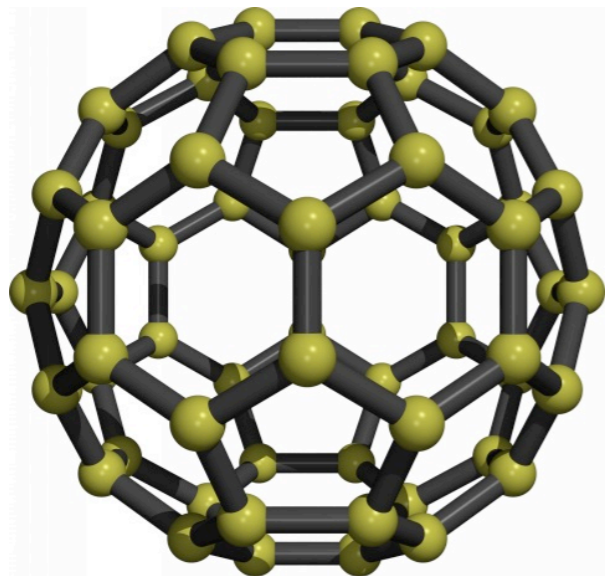


Need to include entire structure, additional orbitals

First-principles calculations

Use zero-temperature LDA density functional calculations for structure and bonding

Although these band-structure methods “fail”, structure and bonding are close to experiment: hope/look for trends.

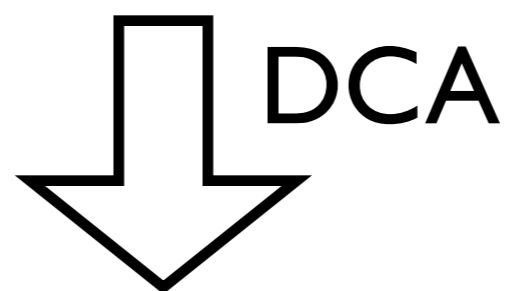


Method

1. DFT LDA ground state

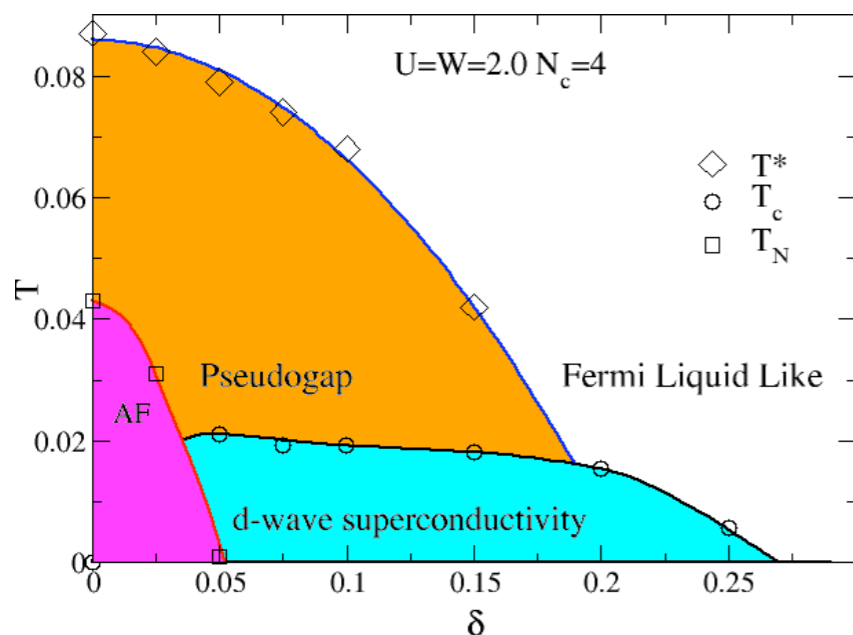
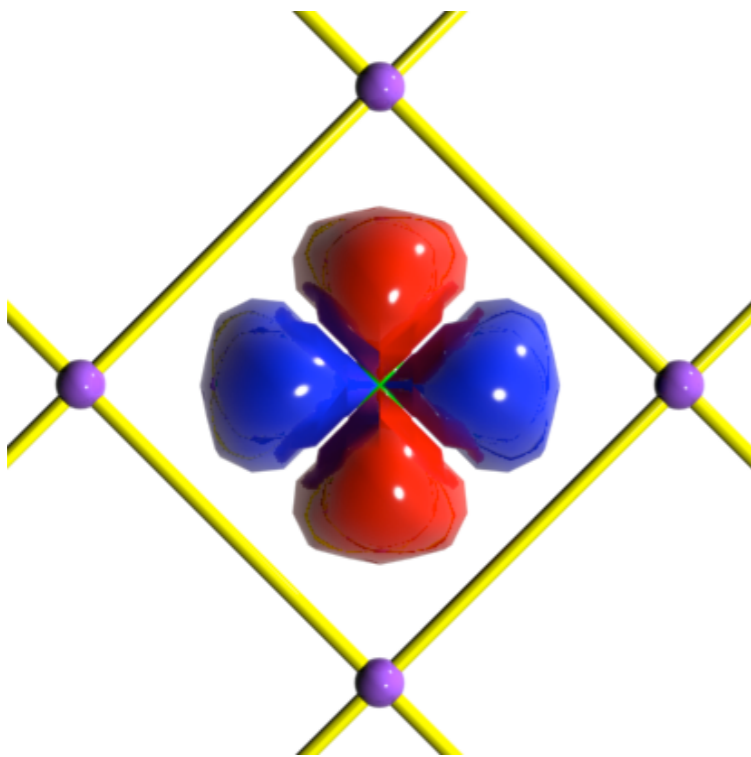


2. Multi-band Hubbard Hamiltonian



3. Phase Diagram

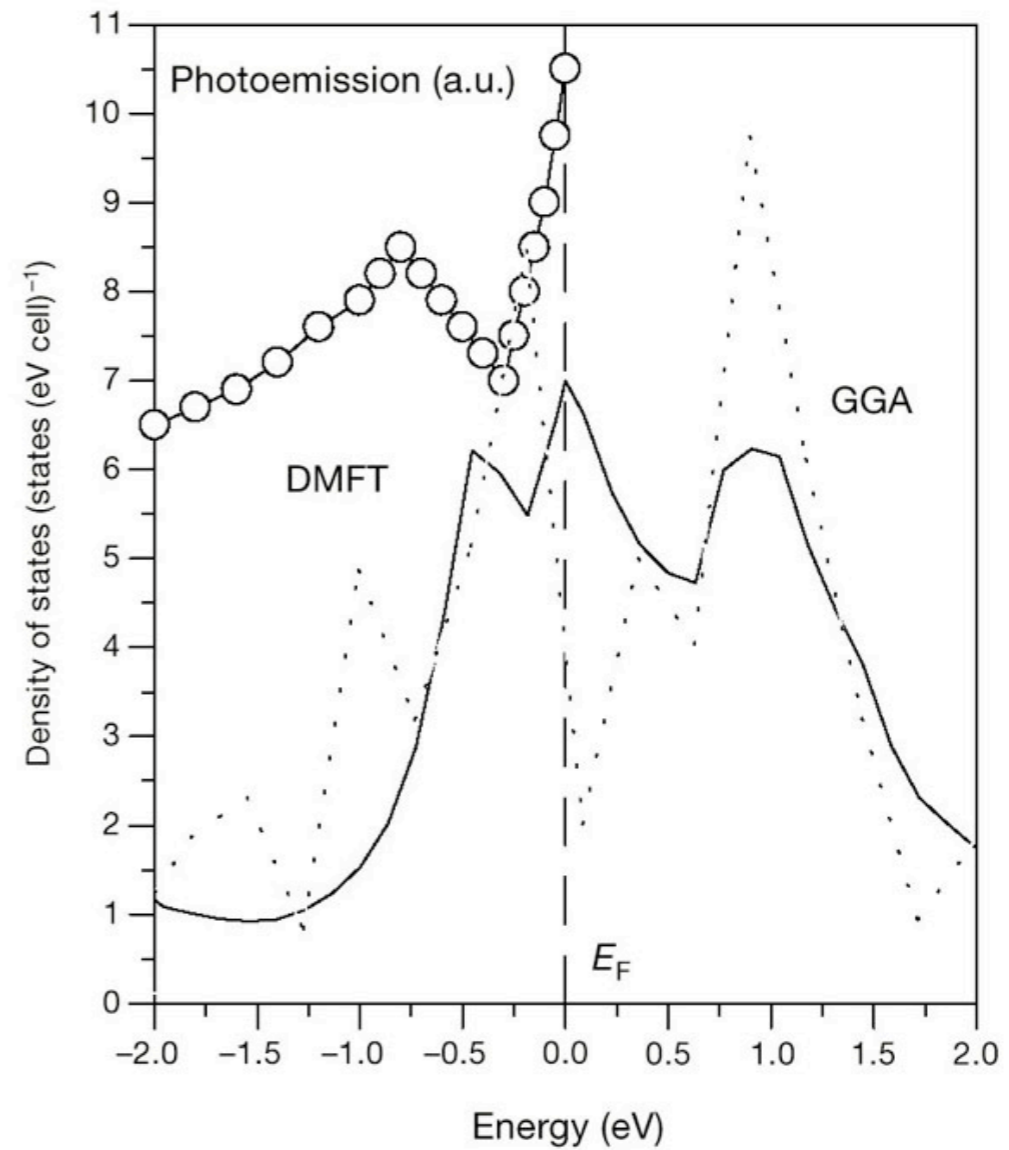
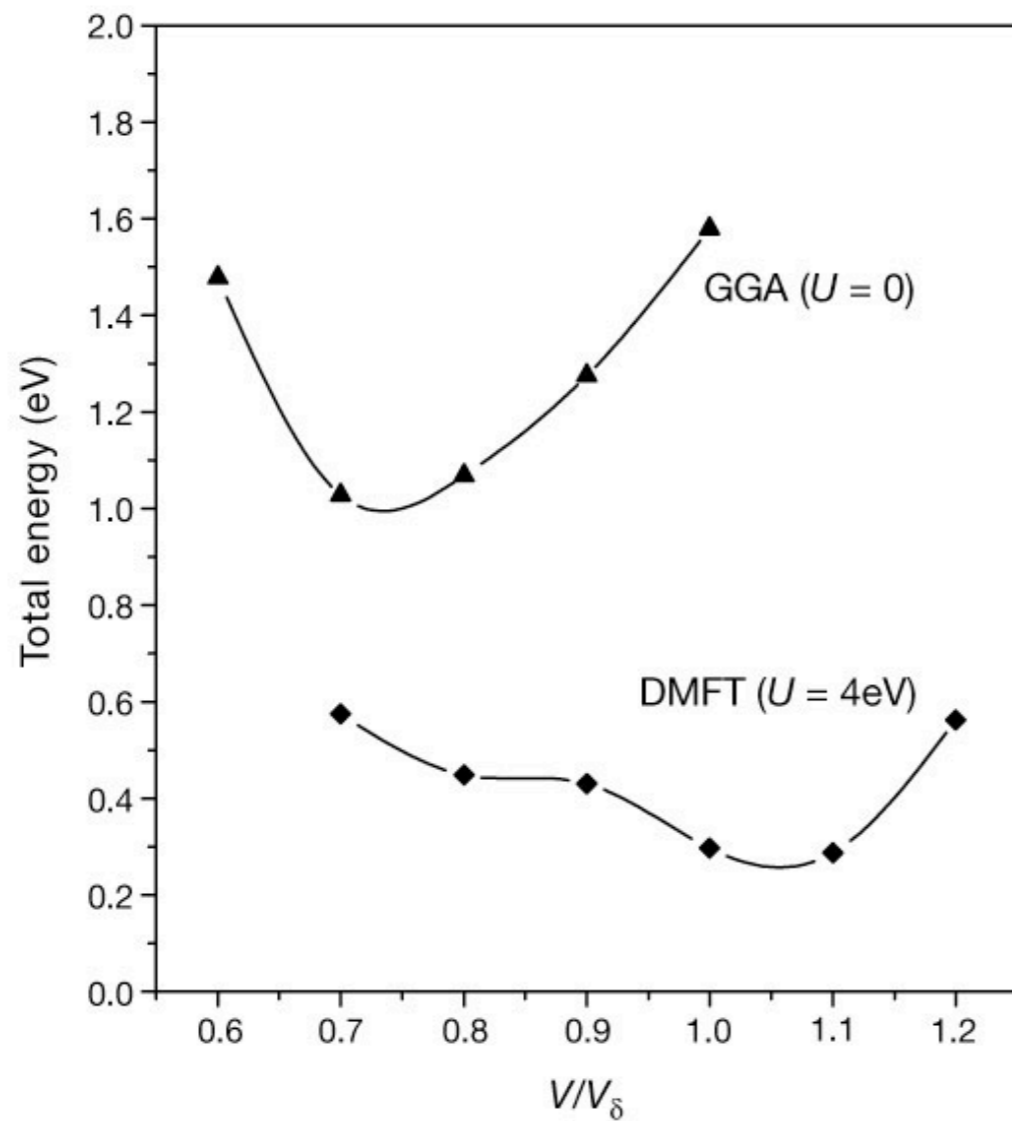
$n(\mathbf{r})$



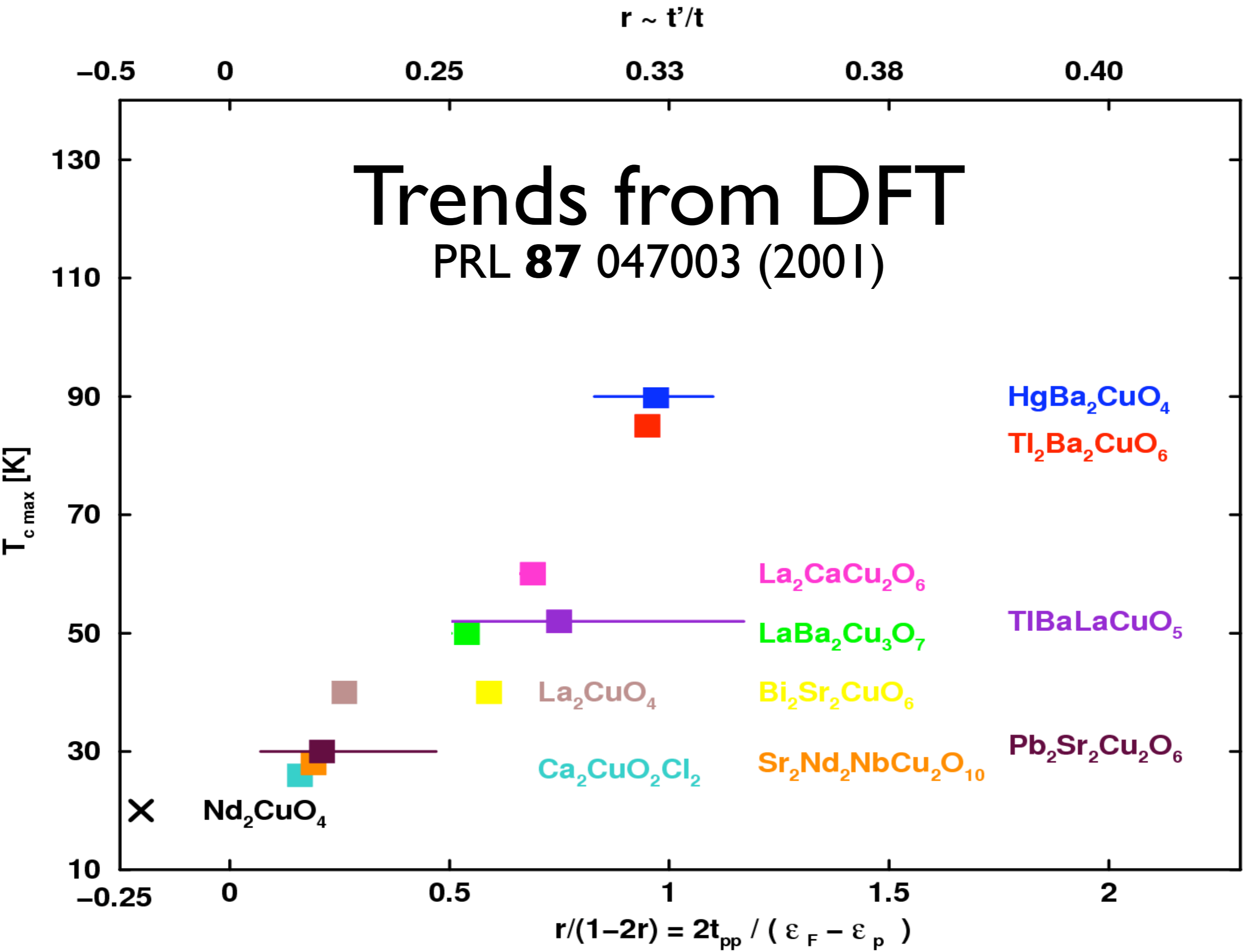
Can this work?

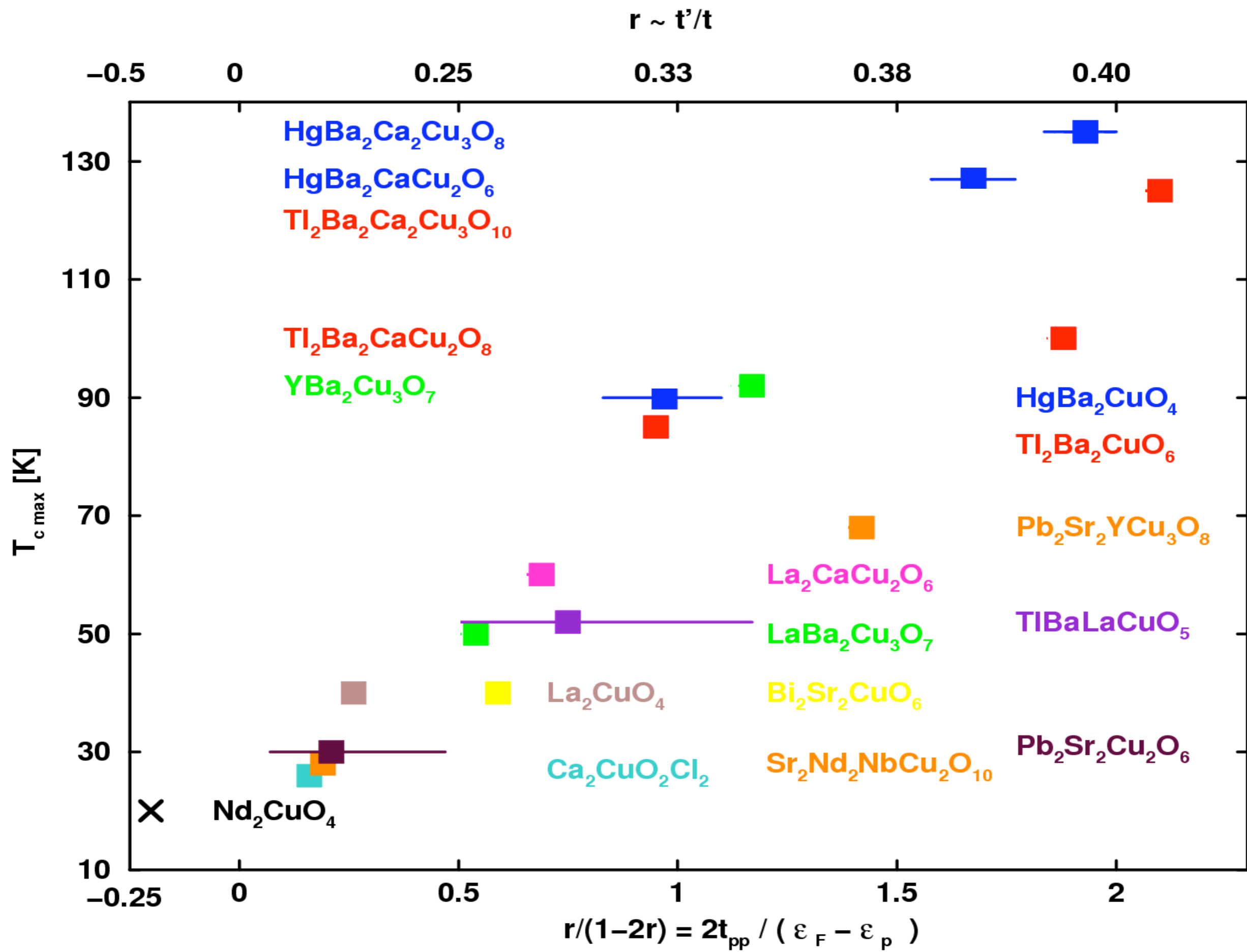
LDA+DMFT

Similar method recovers structural phase transition in Pu



Kotliar Nature **410** 793 (2001)

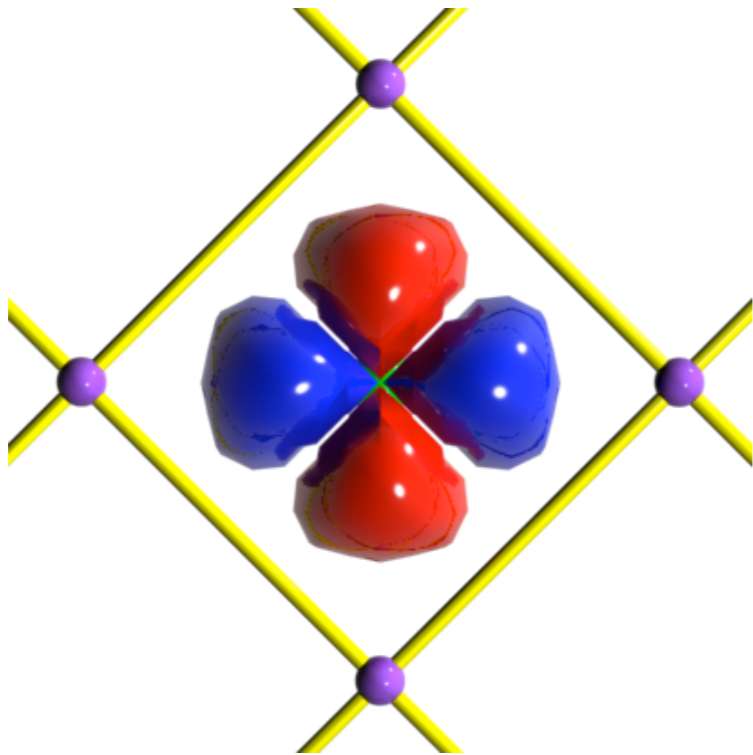




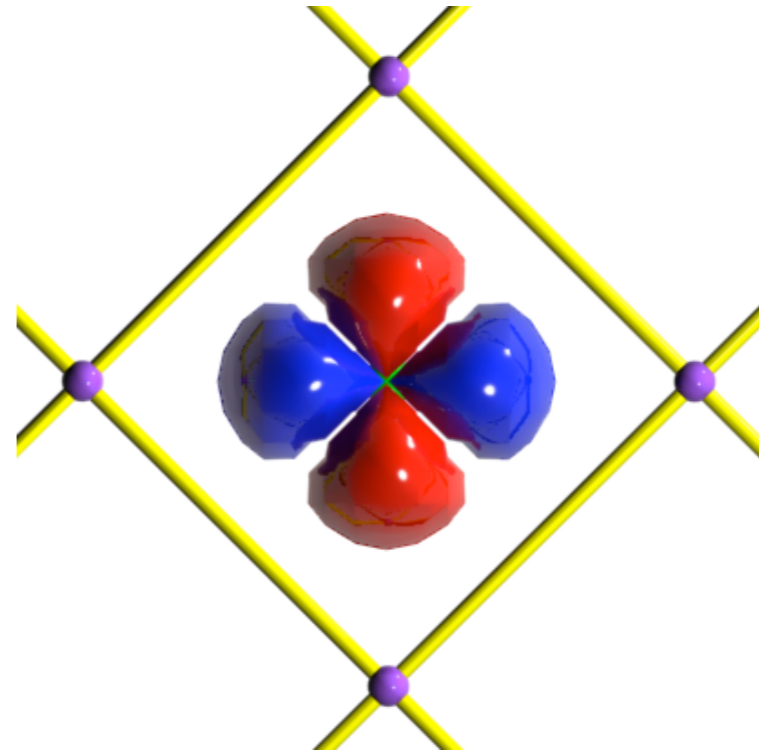
DFT Orbitals

Well-localized Cu d orbital obtained: small materials differences.

○ p_x, p_y : strong hybridization.



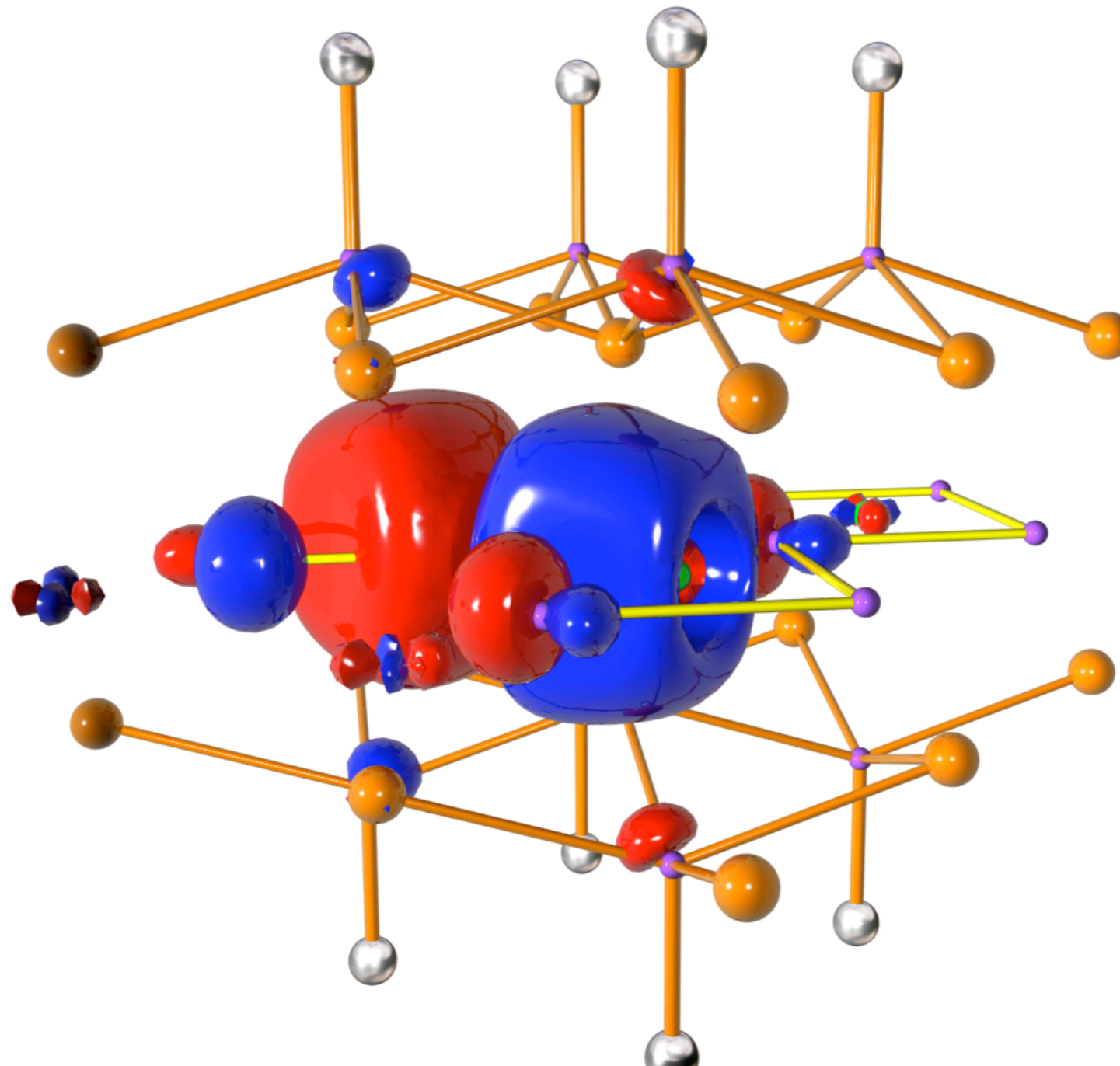
La₂CuO₄

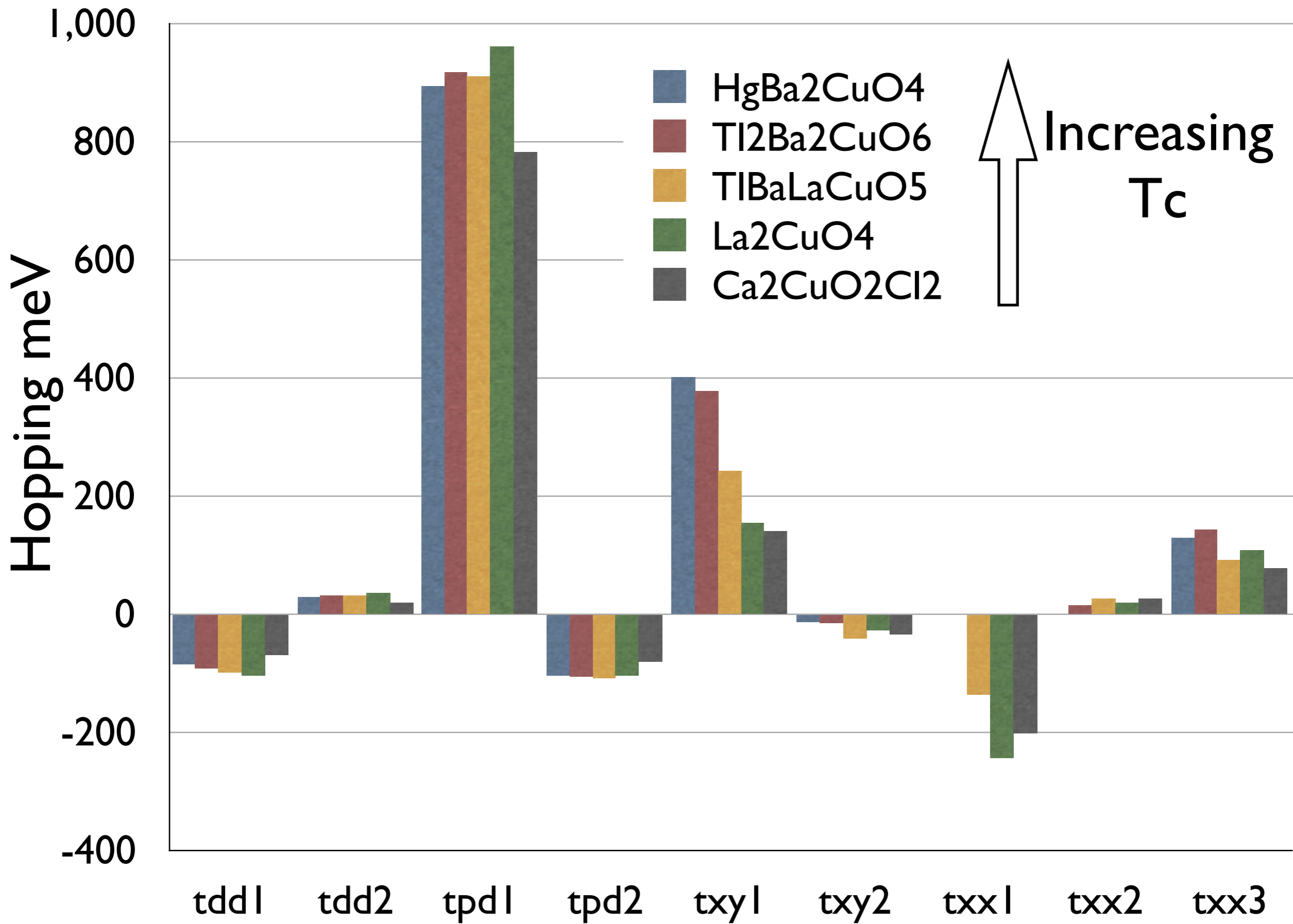


HgBa₂CuO₄

DFT Orbitals

Some far from atomic picture



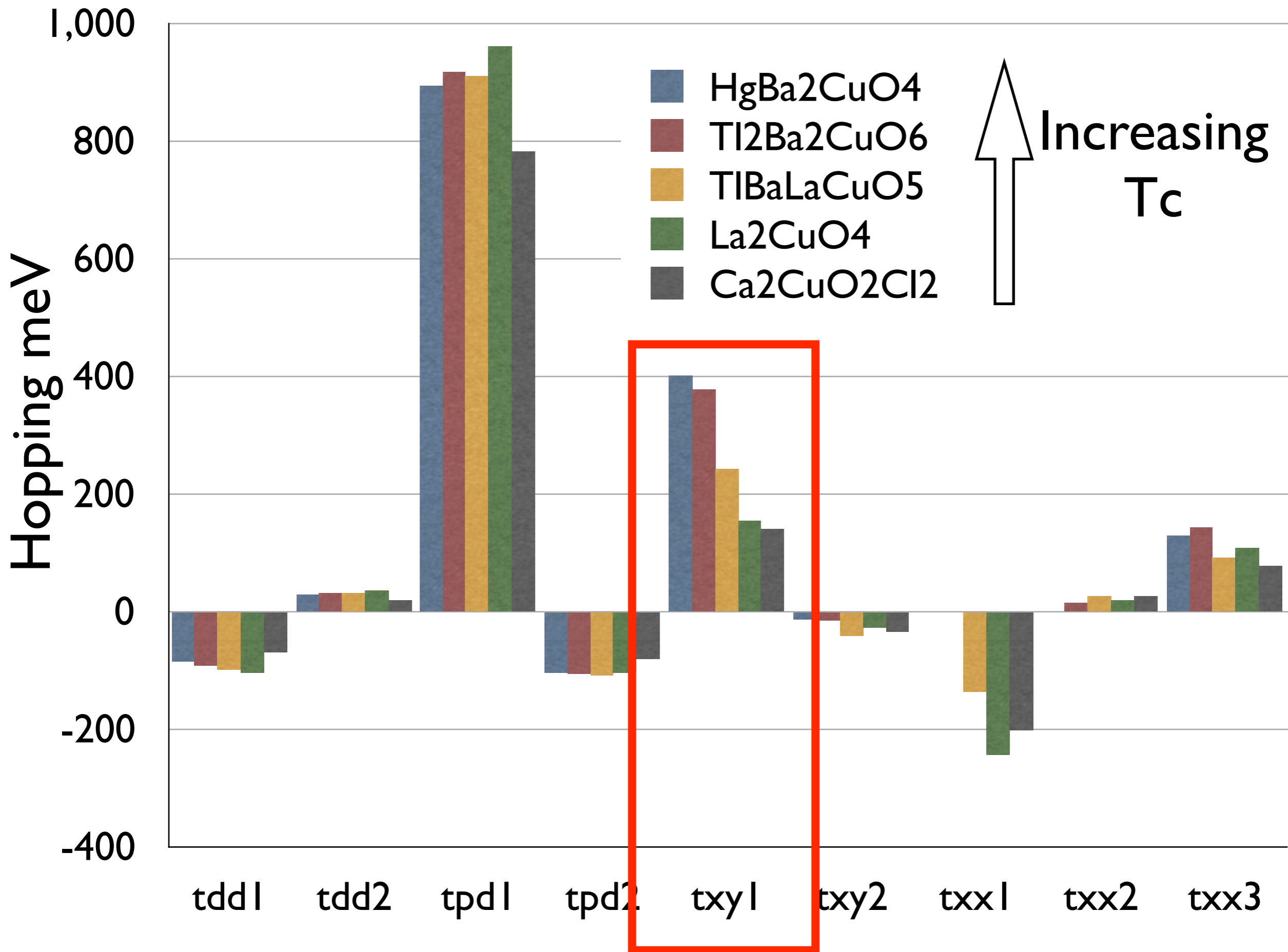


DFT Results

- ~6 terms appear significant, in this basis

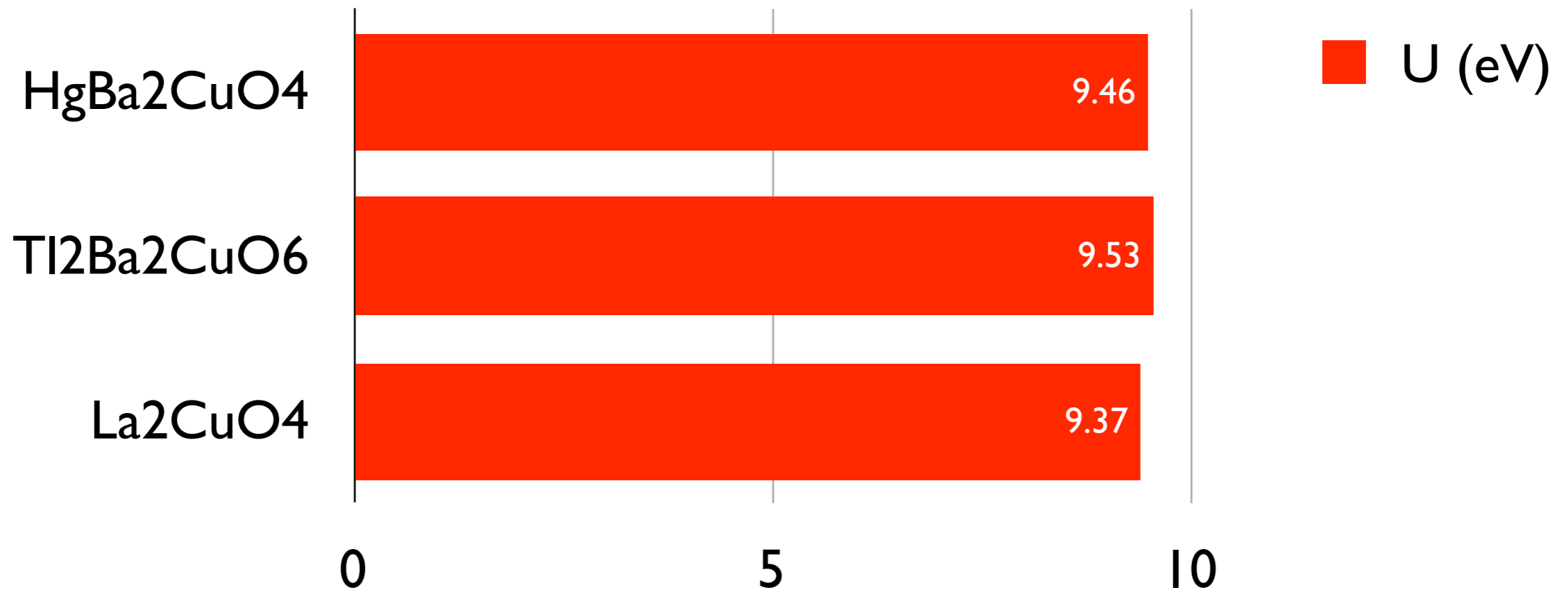
Parametric studies are possible

- Parameters are close to empirical parameters used in model calculations
- Some trends apparent e.g. t_{xy1} (=tpp) increases with increasing T_c . Similar to single band observations, but inconclusive.



LDA+DCA results

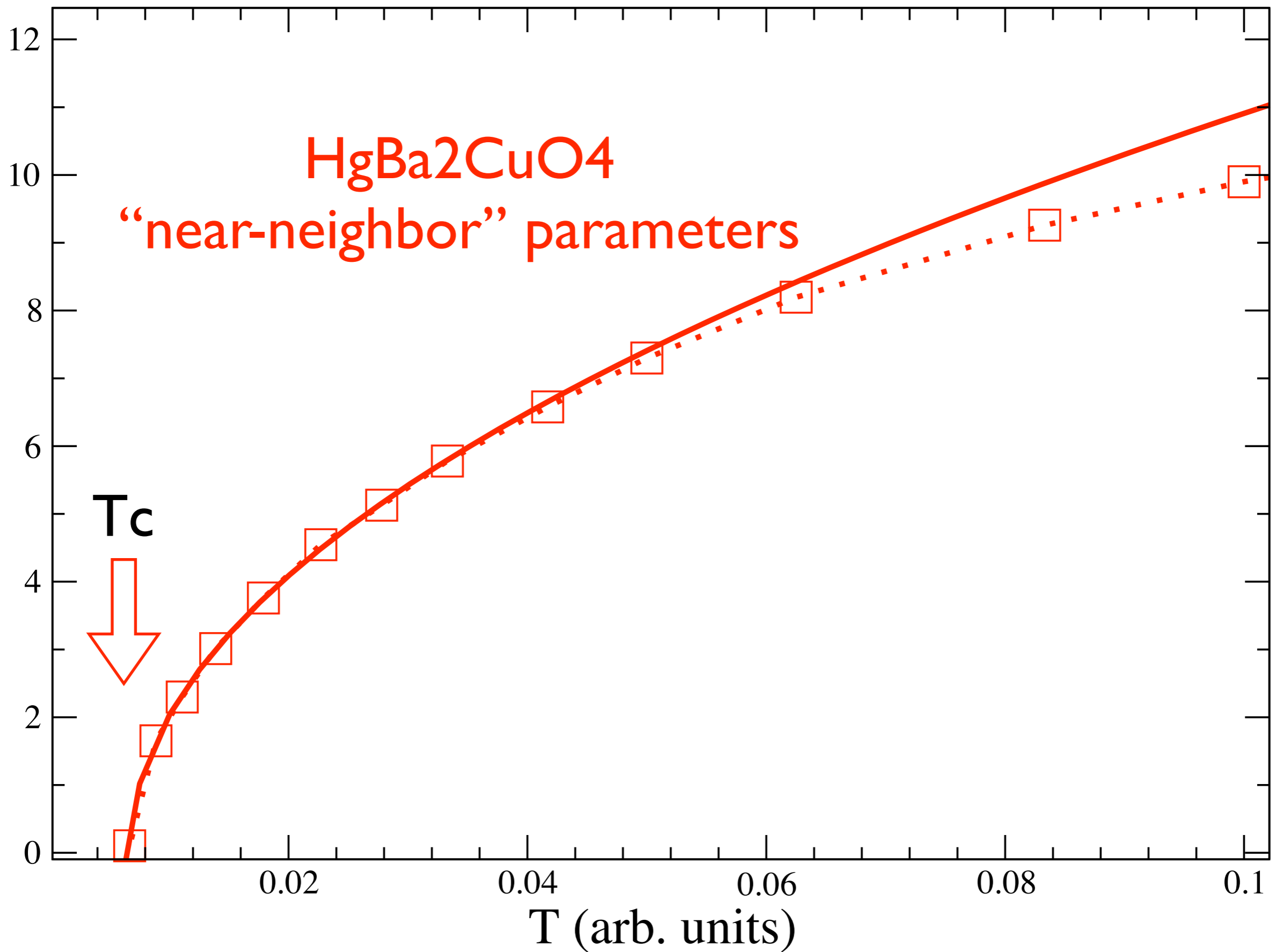
Calculated U

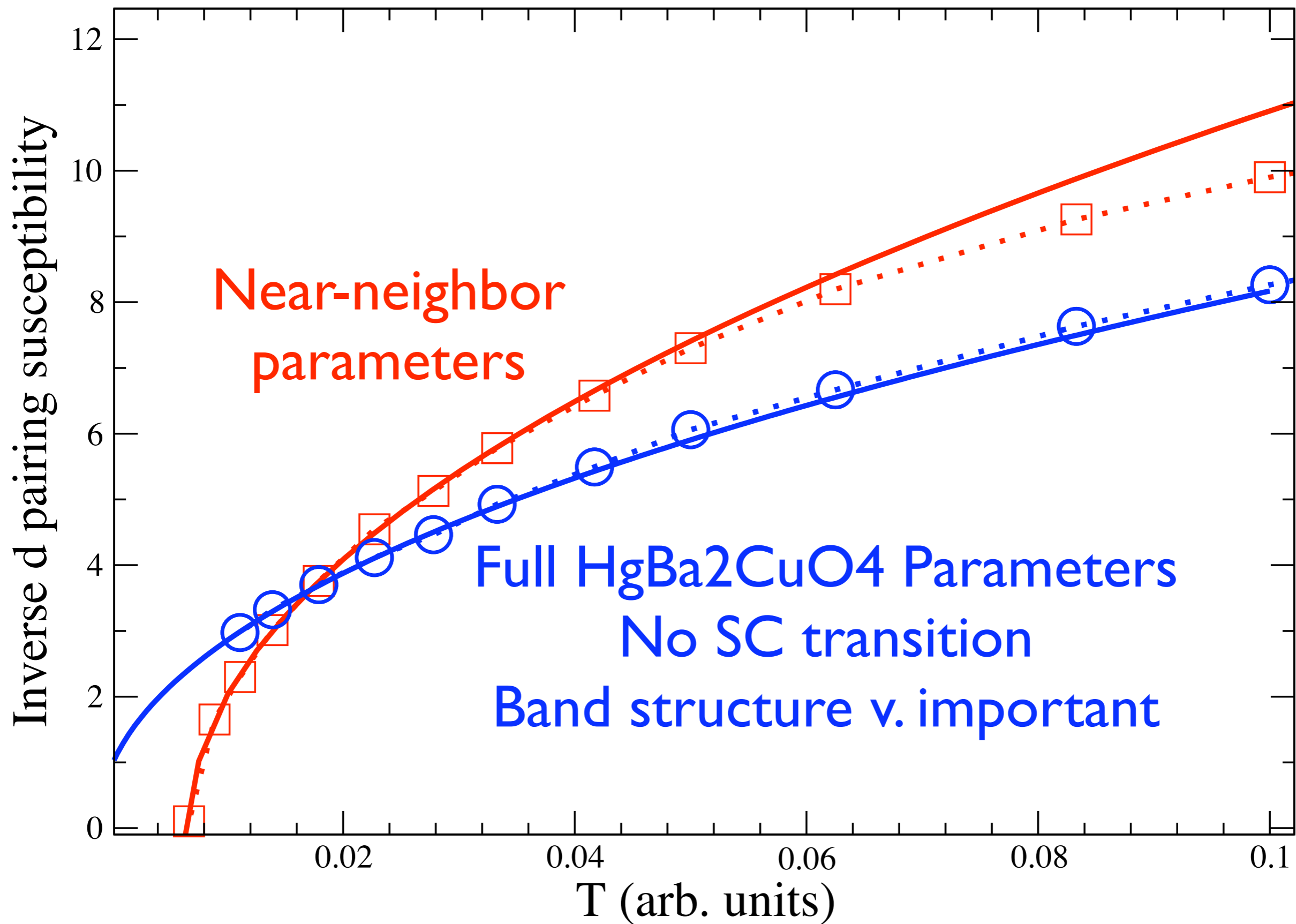


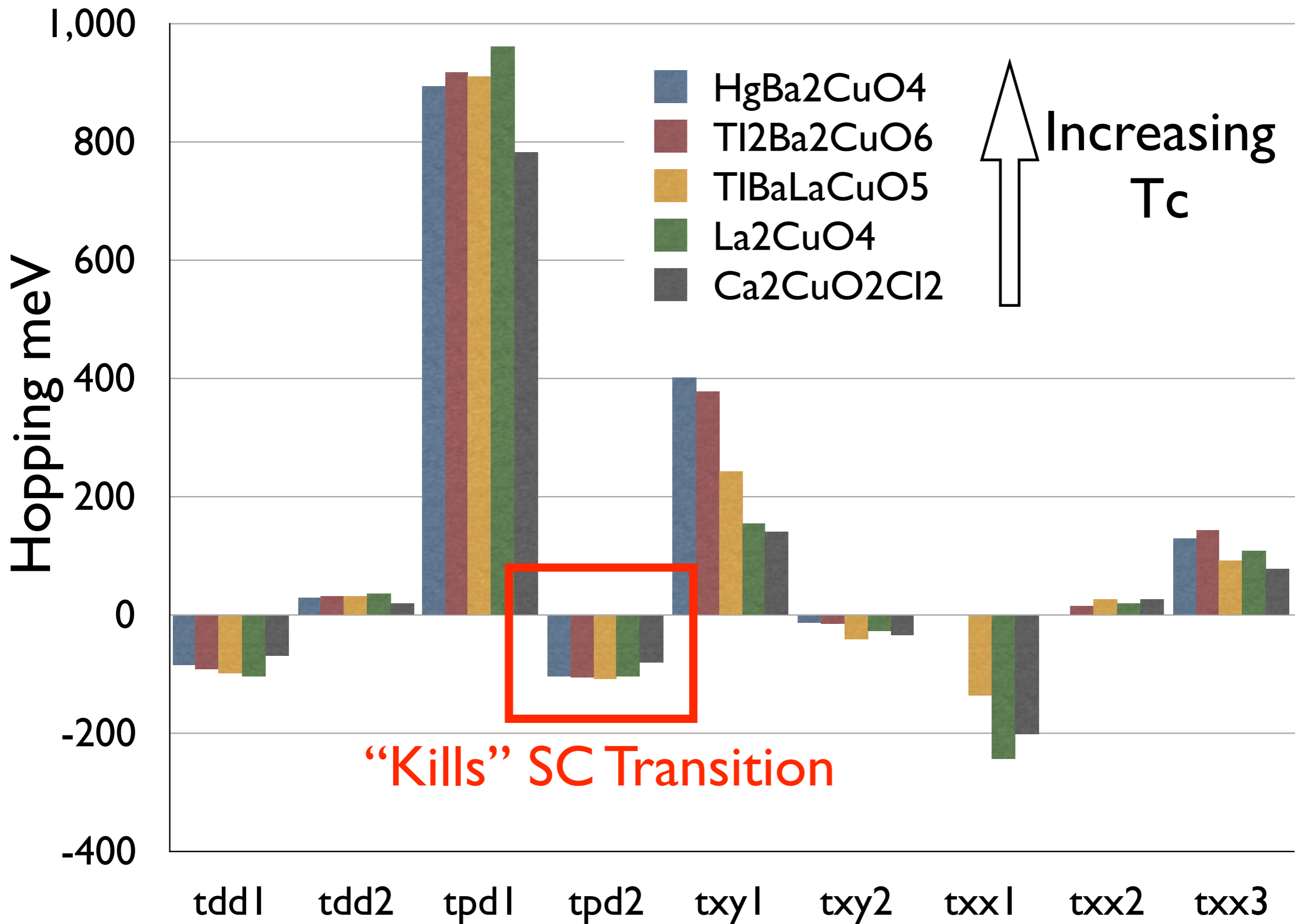
Few % variation in U; similar in all materials

Any T_c dependence must reside in orbitals or additional interactions (e.g. phonons)

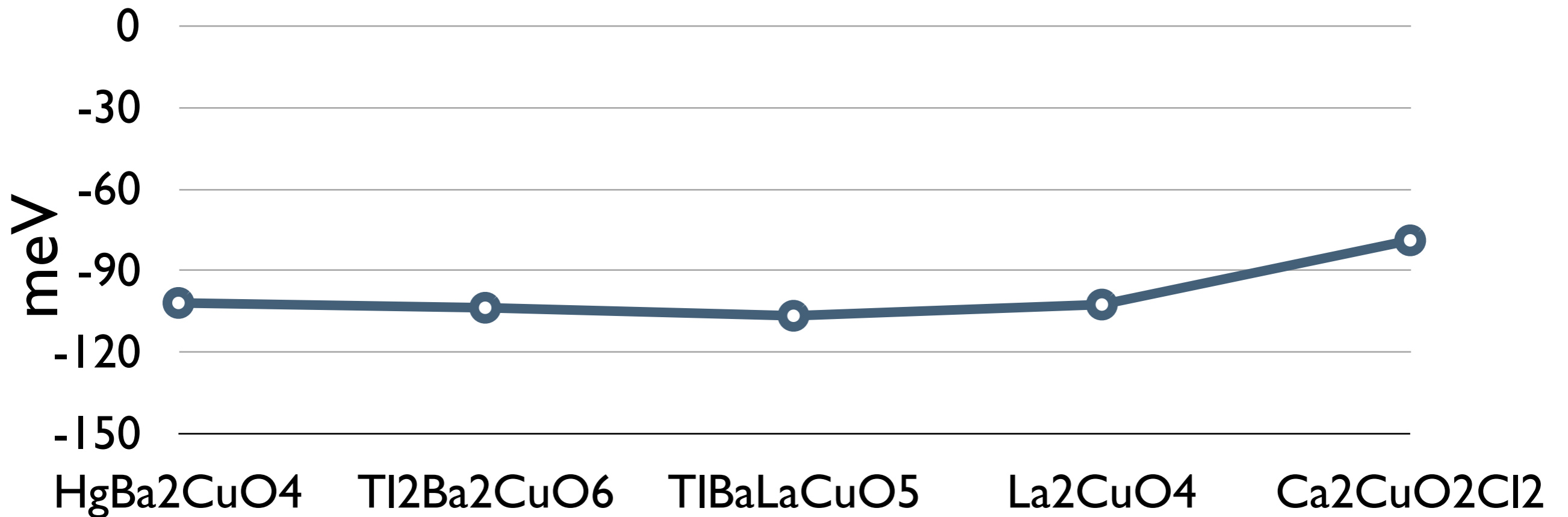
Inverse d pairing susceptibility







Parametric Results



2nd NN Cu-O hybridization strongly governs T_c

Toy model: +ve sign, T_c increased $\sim 60\%$ from reference

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Next Steps

Investigating influence of DFT ground state

More accurate calculations underway

If we fail, we will have shown “something extra” is needed to describe HTSC in real materials.

If we succeed, we expect to obtain “materials trends” in real HTSC materials.

Oxygen Superstructures Throughout the Phase Diagram of $(Y, Ca)Ba_2Cu_3O_{6+x}$ J. Stempfer,¹ I. Zegkinoglou,¹ U. Rütt,¹ M. v. Zimmermann,² C. Bernhard,¹ C.T. Lin,¹ Th. Wolf,³ and B. Keimer¹¹*Max-Planck-Institut für Festkörperforschung, Heisenbergstr. 1, D-70569 Stuttgart, Germany*²*Hamburger Synchrotronstrahlungslabor HASYLAB at Deutsches Elektronen-Synchrotron DESY,
Notkestr. 85, D-22603 Hamburg, Germany*³*Forschungszentrum Karlsruhe, ITP, D-76021 Karlsruhe, Germany*

(Received 12 November 2003; published 7 October 2004)

The doping dependence of short-range lattice superstructures in $(Y, Ca)Ba_2Cu_3O_{6+x}$ has been studied with high-energy x-ray scattering. We observe diffuse features with a well defined periodicity which depend on the oxygen concentration but not on the charge carrier concentration. In addition, we find that diffuse scattering is absent in underdoped $YBa_2Cu_4O_8$, which does not sustain oxygen defects. Our combined data highlight that the diffuse scattering arises from short-range oxygen ordering and associated lattice distortions. Signatures of stripe ordering or fluctuations are not seen and therefore must be much weaker.

Four-Unit-Cell Superstructure in the Optimally Doped $\text{YBa}_2\text{Cu}_3\text{O}_{6.92}$ Superconductor

Zahirul Islam,^{1,*} X. Liu,² S. K. Sinha,² J. C. Lang,¹ S. C. Moss,³ D. Haskel,¹ G. Srajer,¹ P. Wochner,⁴ D. R. Lee,¹
D. R. Haeffner,¹ and U. Welp⁵

¹*Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439, USA*

²*Department of Physics, University of California, San Diego, California 92093, USA*

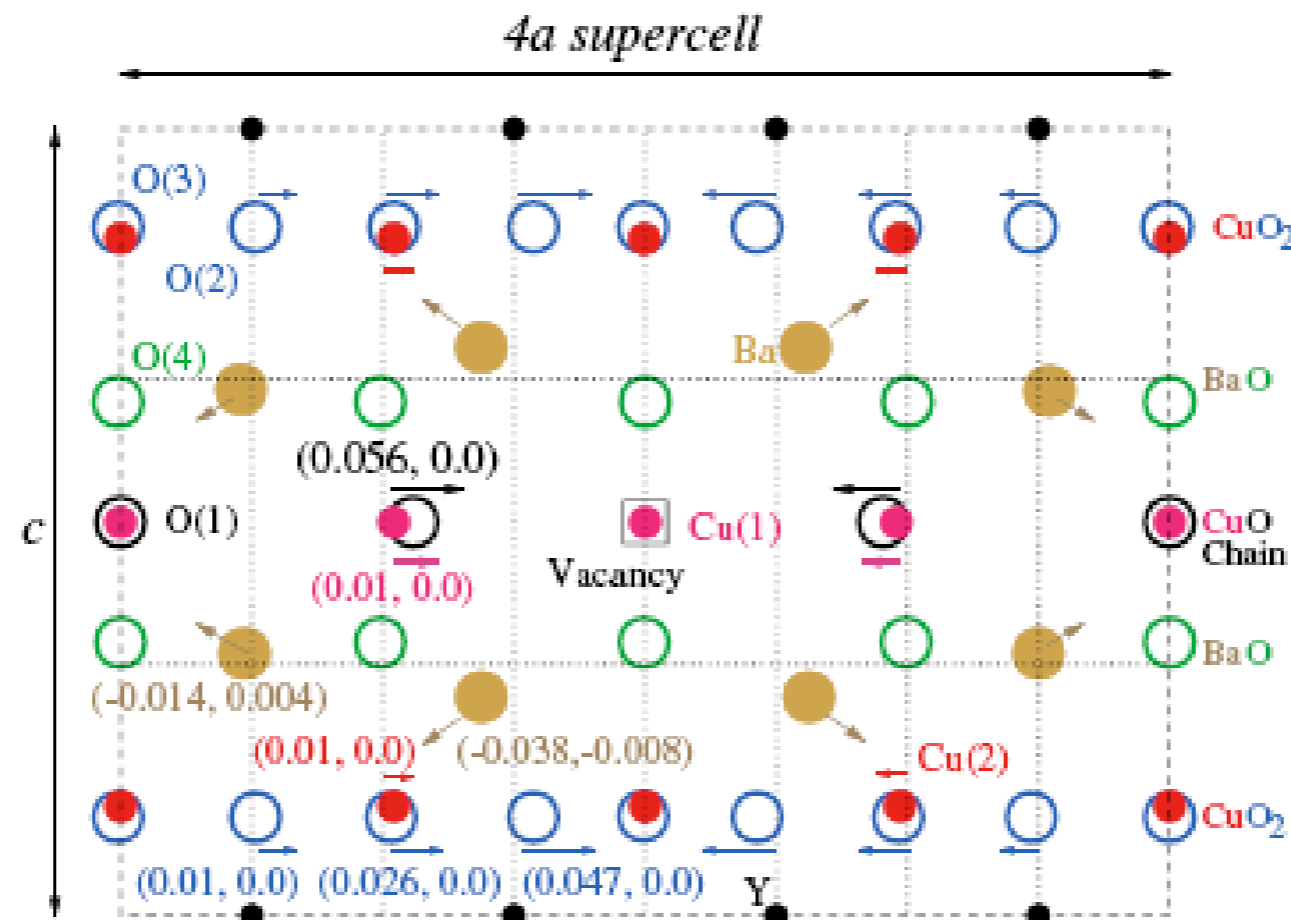
³*Department of Physics and Texas Center for Superconductivity and Advanced Materials, University of Houston, Houston, Texas 77204, USA*

⁴*Max-Planck-Institut für Metallforschung, 70569 Stuttgart, Germany*

⁵*Materials Science Division, Argonne National Laboratory, Argonne, Illinois 60439, USA*

(Received 23 December 2003; published 7 October 2004)

Diffuse x-ray scattering measurements reveal that the optimally doped $\text{YBa}_2\text{Cu}_3\text{O}_{6.92}$ superconductor is intrinsically modulated due to the formation of a kinetically limited 4-unit-cell superlattice, $\mathbf{q}_0 = (\frac{1}{4}, 0, 0)$, along the shorter Cu-Cu bonds. The superlattice consists of large anisotropic displacements of Cu, Ba, and O atoms, respectively, which are correlated over ~ 3 – 6 unit cells in the ab plane, and appears to be consistent with the presence of an O-ordered “ortho-IV” phase. Long-range strains emanating from these modulated regions generate an inhomogeneous lattice which may play a fundamentally important role in the electronic properties of yttrium-barium-copper-oxides.



Summary

Small cluster DCA Hubbard calculations display key features of cuprate phase diagram.

LDA+DCA calculations are feasible. We are testing fundamental assumptions of many cuprate theories.

<http://www.physics.uc.edu/~pkent>

