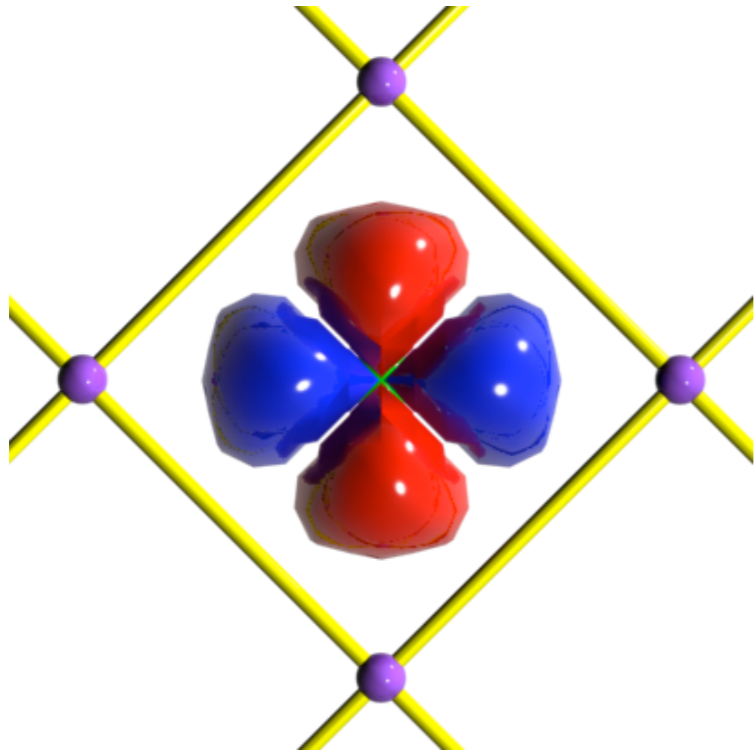


# LDA-DCA Calculations of Cuprate Superconductors

Paul Kent

University of Cincinnati / ORNL  
CMSN Oak Ridge / 20 November 2004  
<http://www.physics.uc.edu/~pkent>

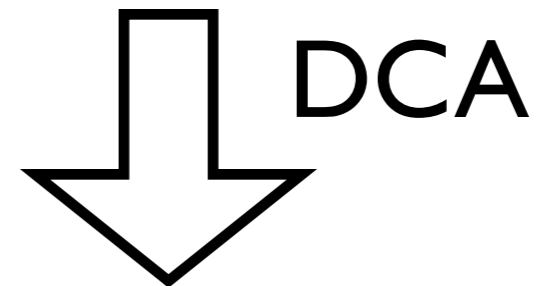
$n(\mathbf{r})$



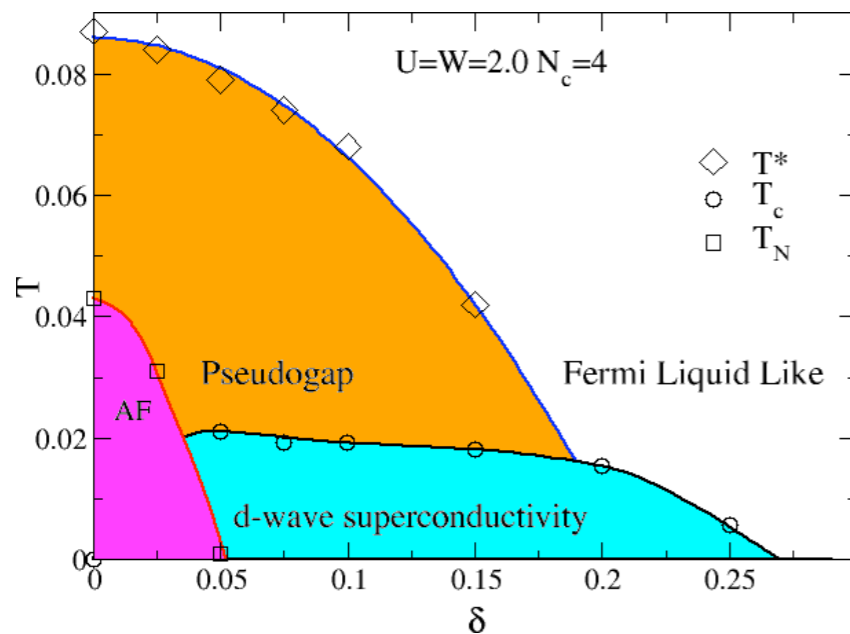
1. DFT LDA ground state



2. Wannier Basis & Hamiltonian



3.  $T_c$ , Phase Diagram



**Aims:** Avoid empirical parameters  
What are the materials trends in  $T_c$ ?

# Acknowledgements

## Collaborators:

Mark Jarrell, Alexandru Macridin / UC

Thomas Maier, Thomas Schulthess / ORNL

Ole K. Andersen, Tanusri Dasgupta, Ove  
Jepsen / MPI Stuttgart

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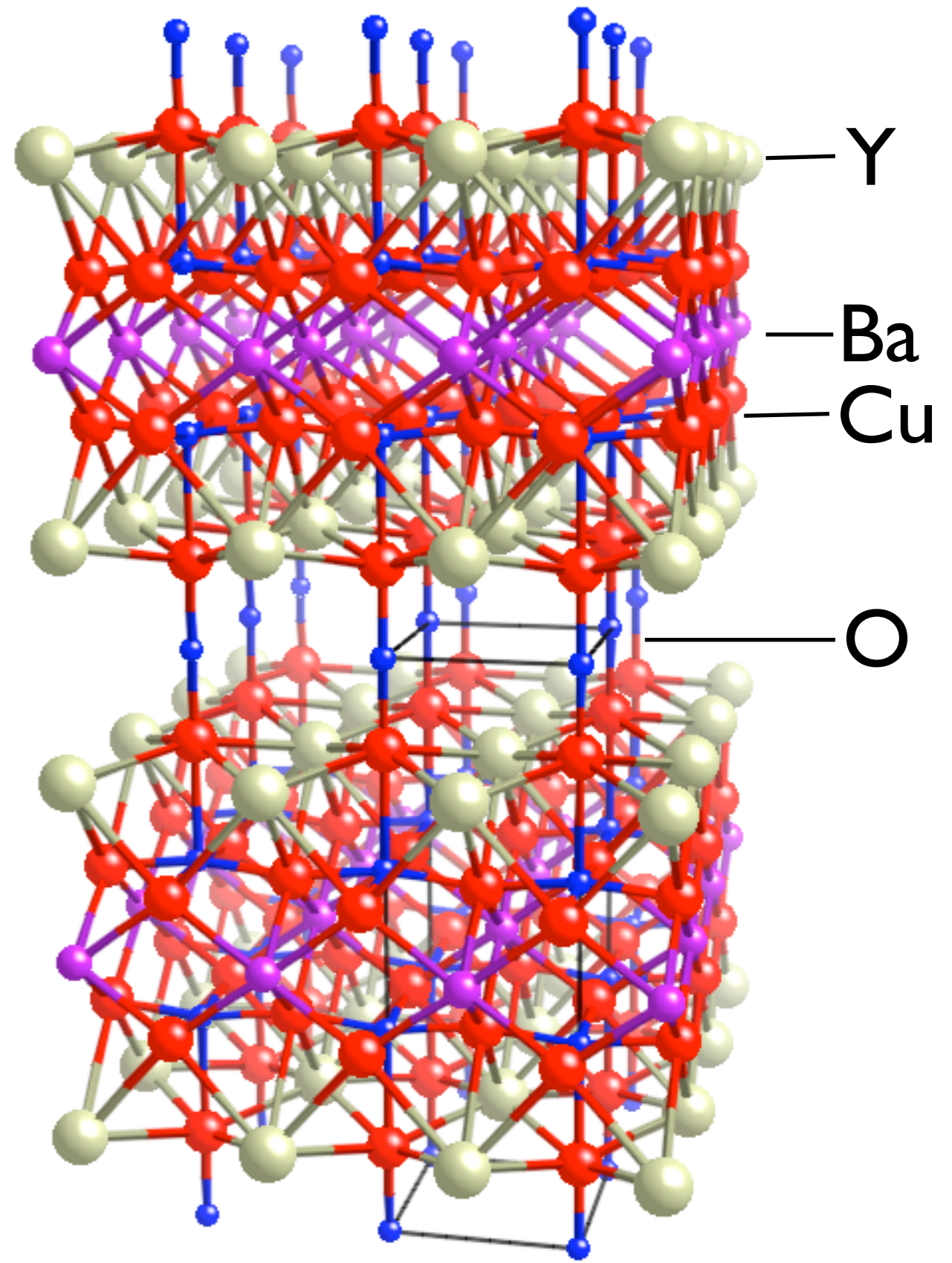
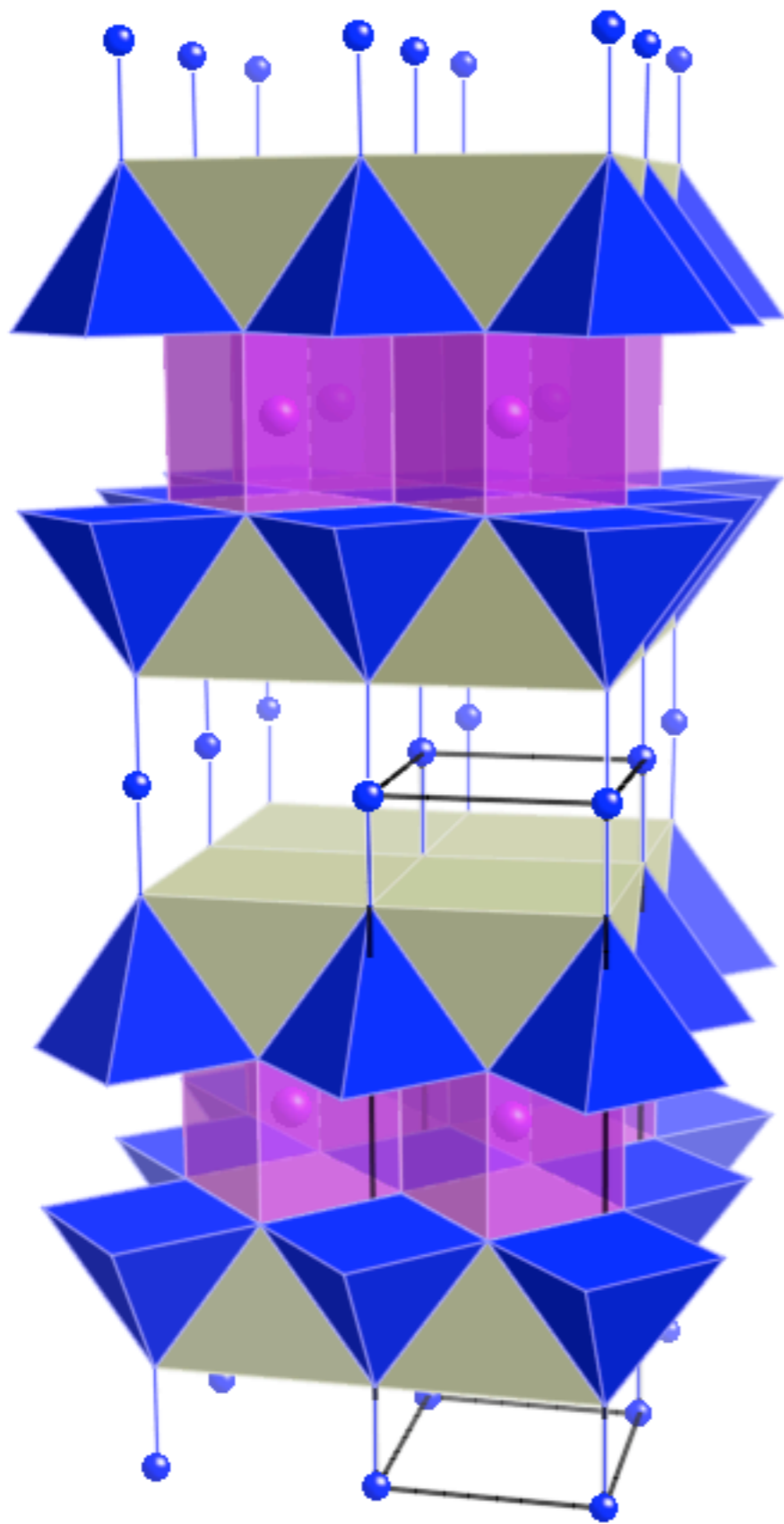
DOE / CMSN

## Computer time:

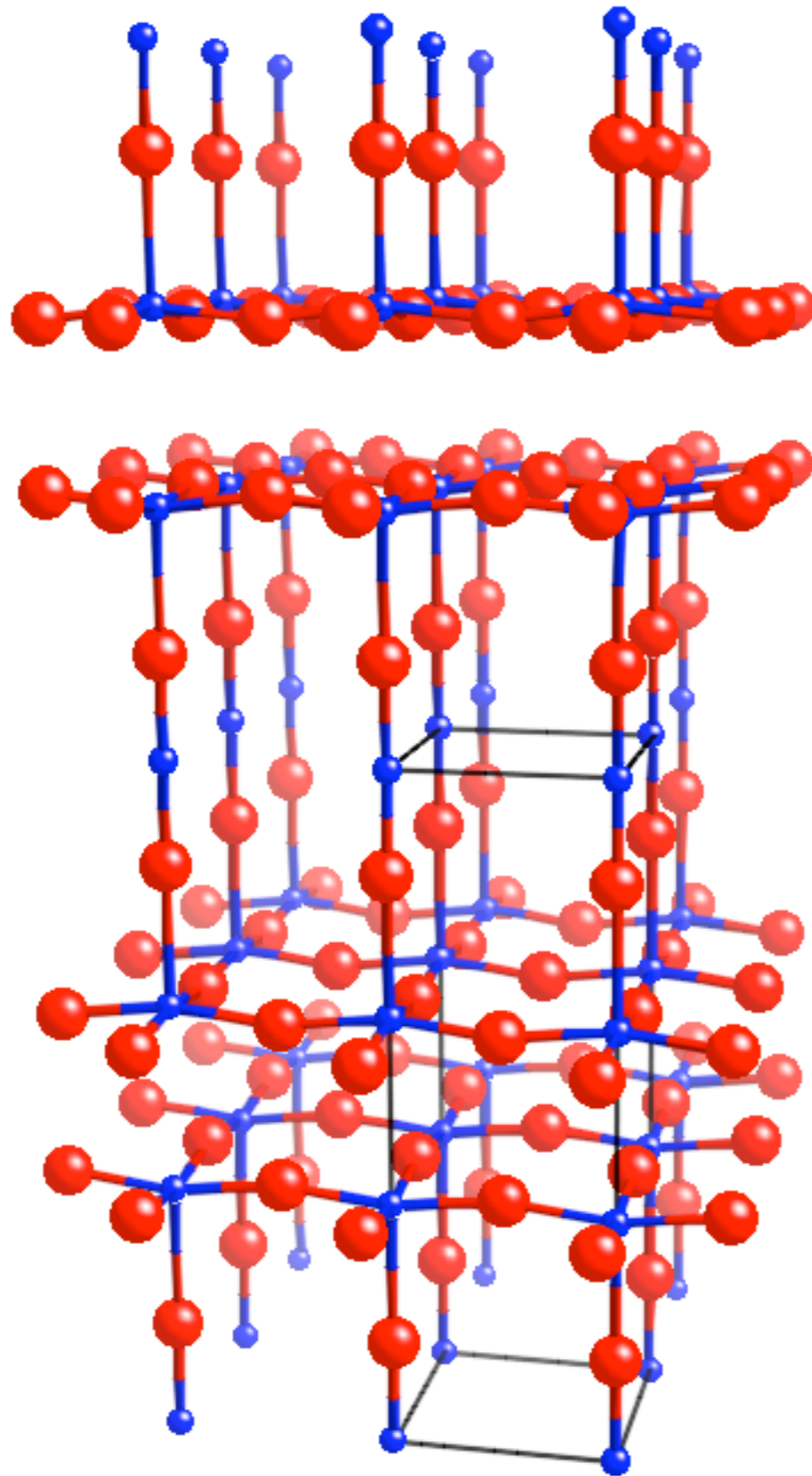
Cray XI / ORNL

# Outline

1. Background - Experiment and Theory
2. Our Approach
3. Results for single-layer materials
4. Next Steps and Summary



YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6</sub>

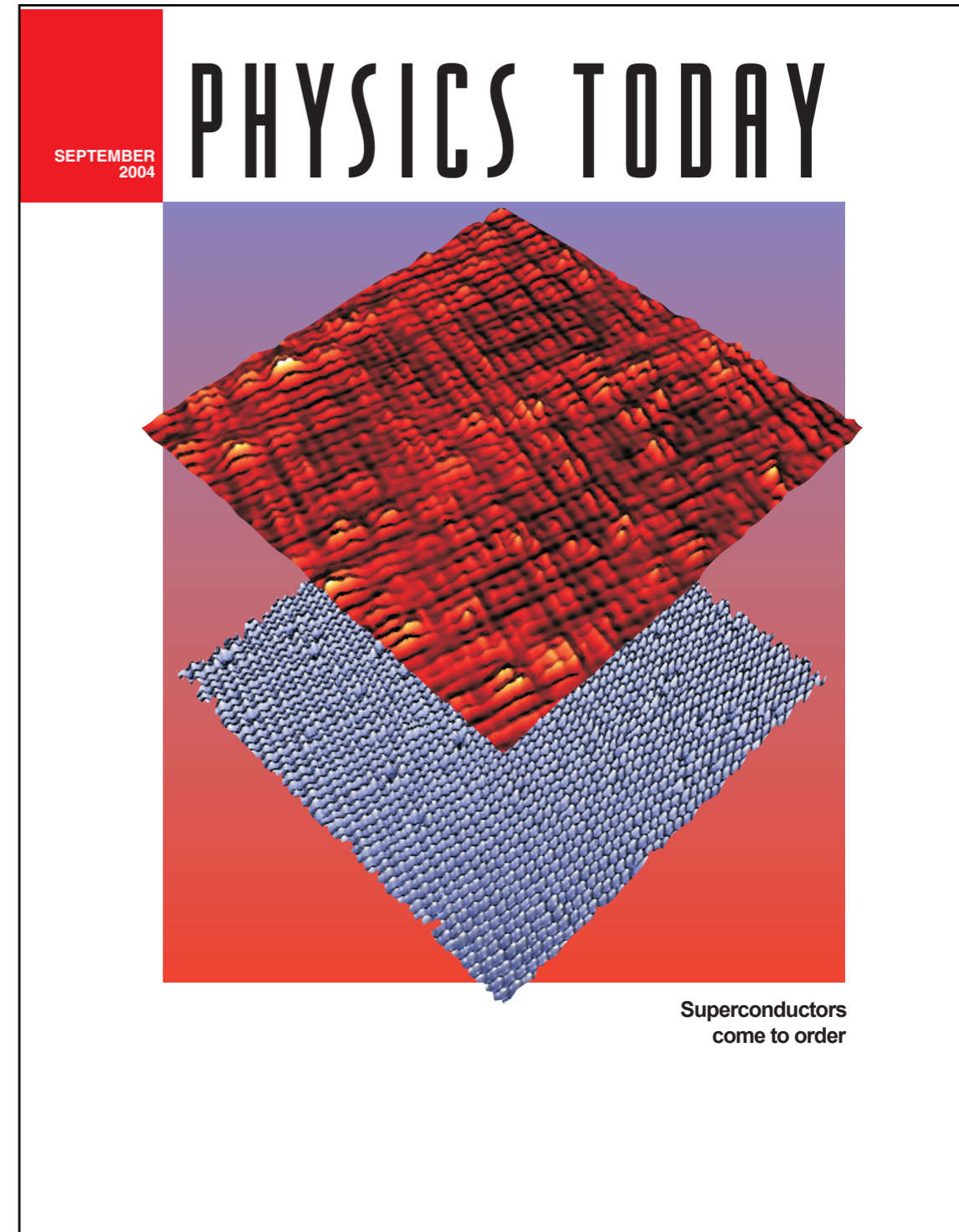
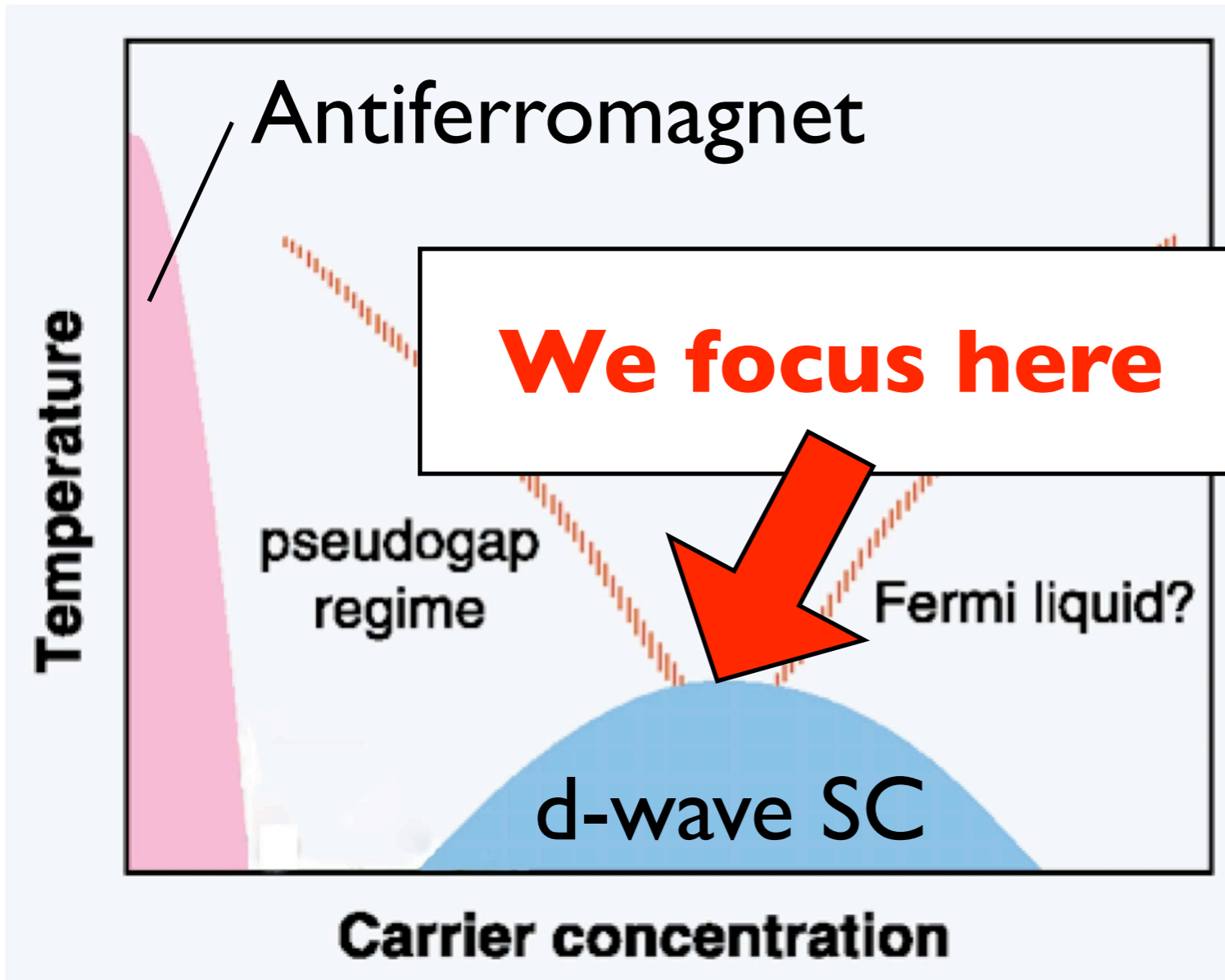


— Cu-O plane  
common to all  
cuprates

How does  
entire structure  
influence Cu-O  
plane physics?

YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6</sub>: Cu, O atoms only

# Rich Phenomenology



# “Key” Properties

Single layer compounds:  $T_c=30-80\text{K}$

e.g.  $\text{La}_2\text{CuO}_4$  “La214”  $T_c=40\text{K}$

Highest  $T_c \sim 130\text{K}$   $\text{HgBa}_2\text{Ca}_2\text{Cu}_3\text{O}_8$

Pressure increases  $1\text{K/GPa}$  to  $\sim 30\text{GPa}$

We aim to find some of these trends  
from first-principles calculation



# Outline

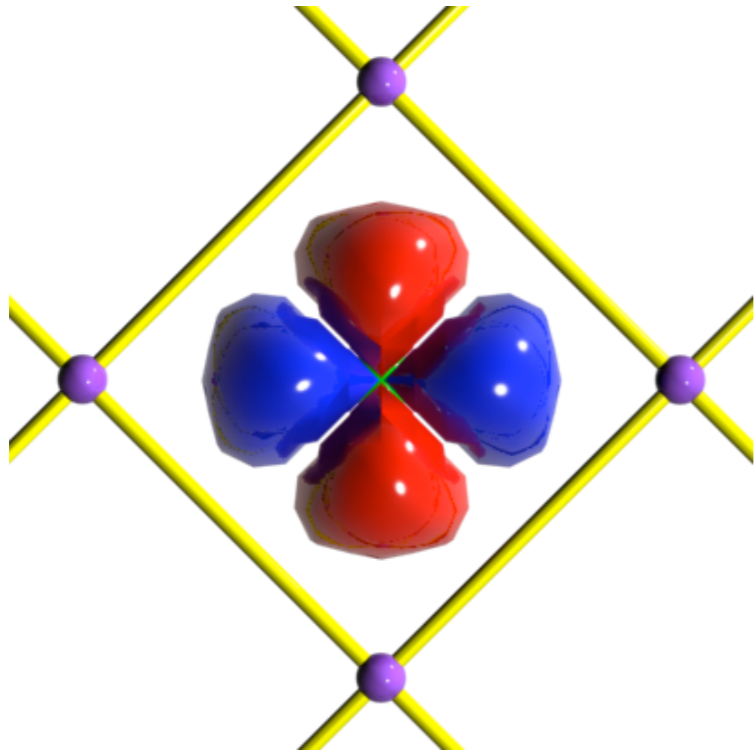
1. Background - Experiment and Theory

**2. Our Approach**

3. Parametric results for single-layer materials

4. Next Steps and Summary

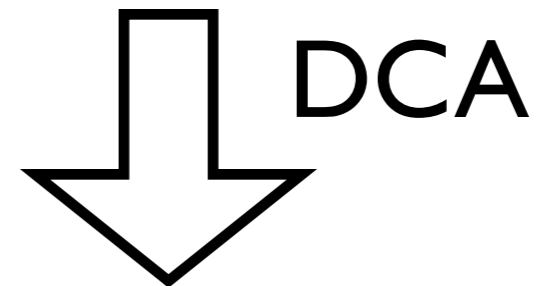
$n(\mathbf{r})$



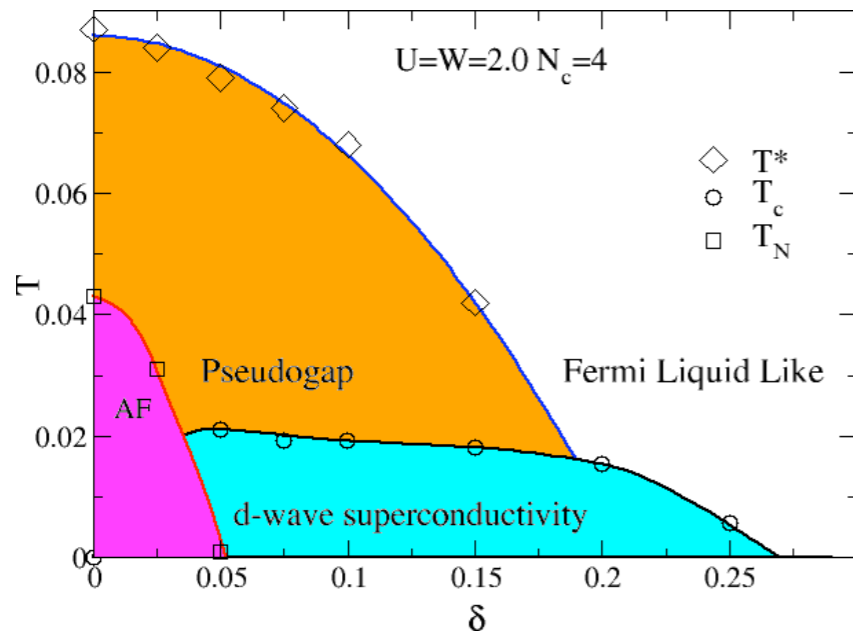
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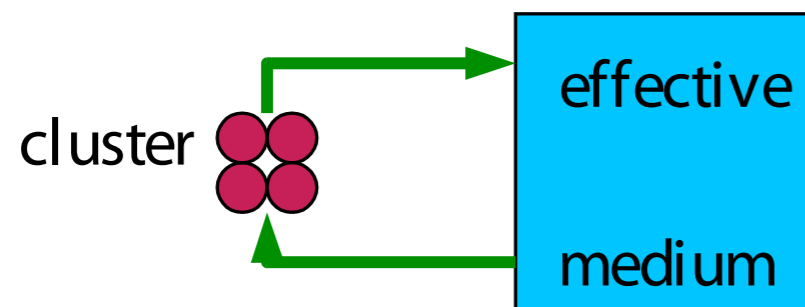
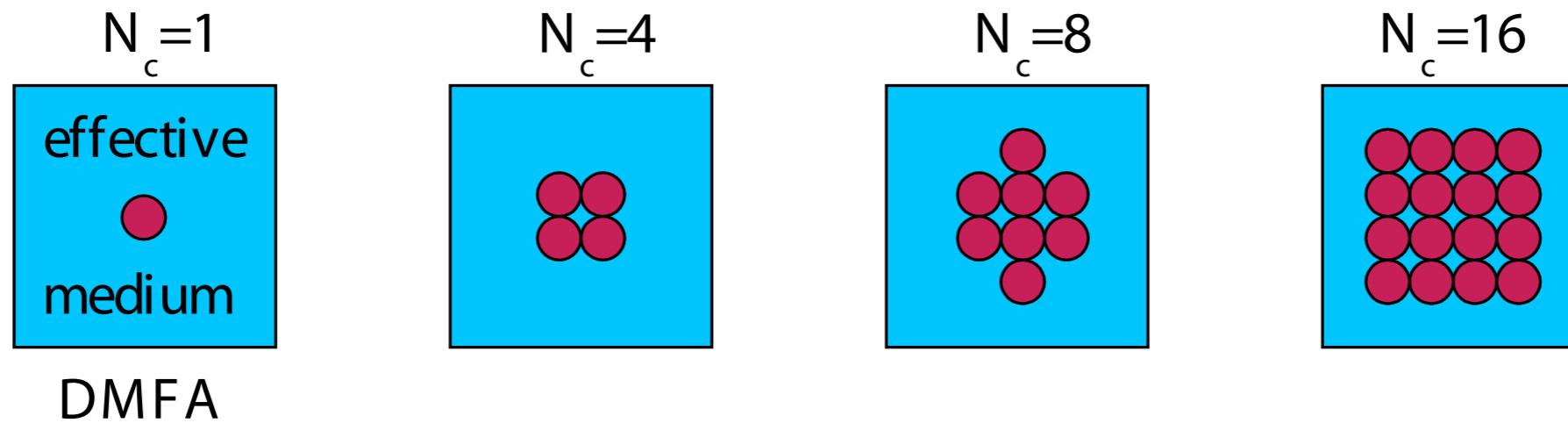


3.  $T_c$ , Phase Diagram



# Cluster Approximations

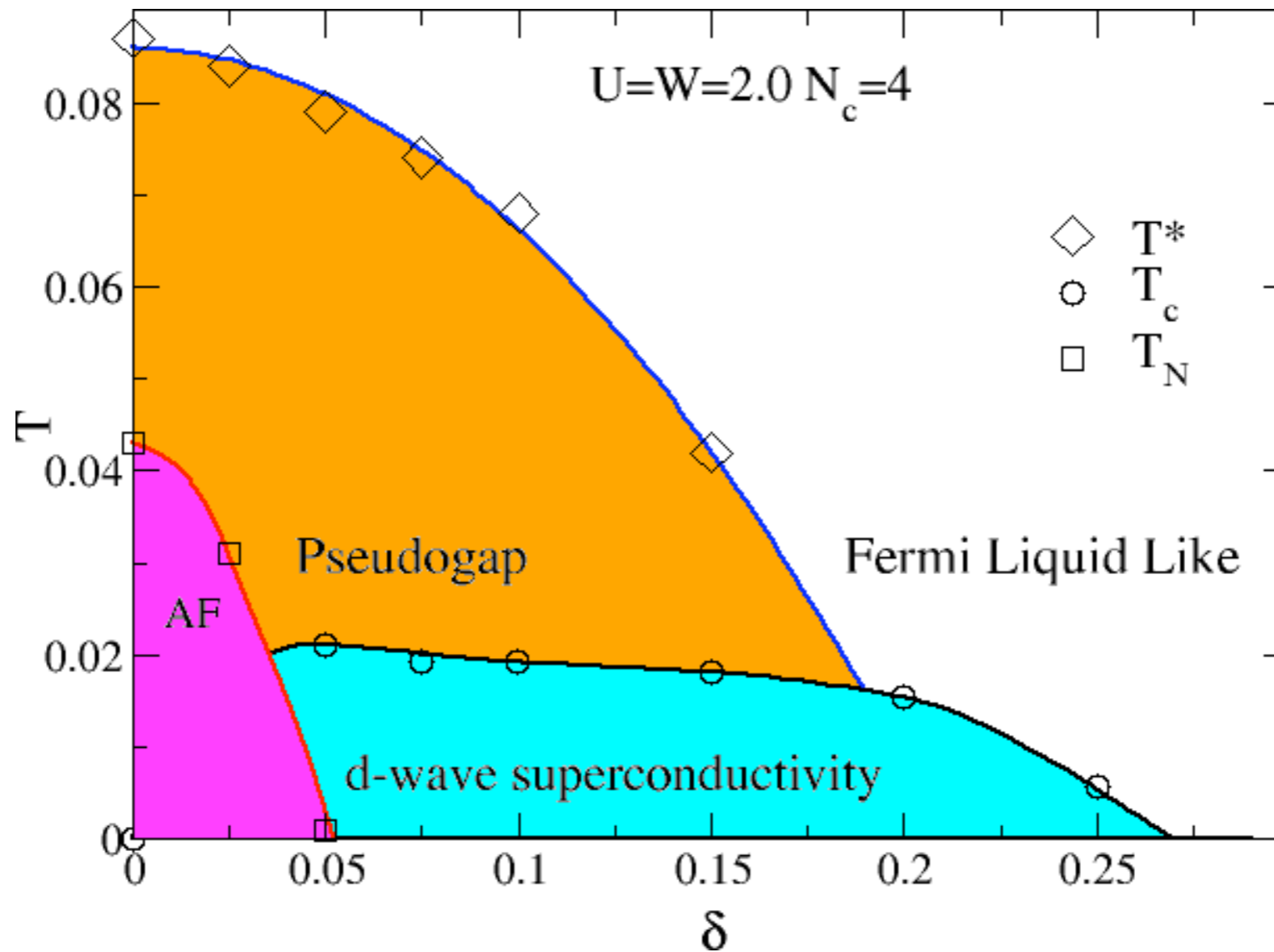
Dynamical Cluster Approximation: Expansion around the DMF/CPA Solutions



$$\sum_{\text{lattice}} \approx \sum_{\text{cluster}}$$

DCA papers <http://www.physics.uc.edu/~jarrell>

# 2x2 DCA Results



Phase diagram for 2x2 single band Hubbard model

# LDA Downfolding

Per Ole Andersen's talk last meeting; also Eva Pavarini's talk this evening

*Andersen J. Phys.Chem. Solids* **56** 1573 (1995)

We obtain a 3 band Hamiltonian:

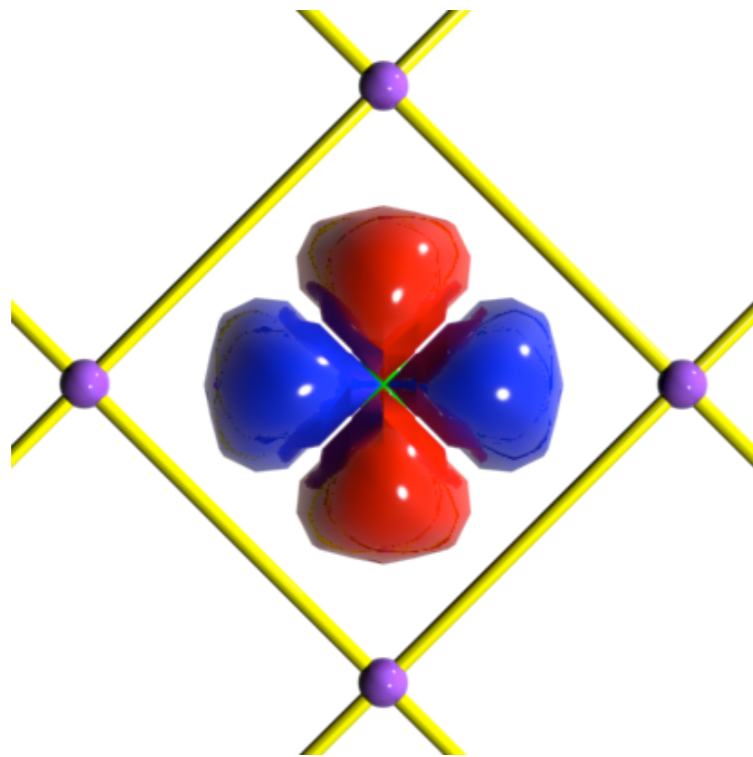
- Chemically intuitive hopping terms between orbitals
- Explicit single particle picture; not many-body (single band)

Calculate  $U$  with correct d orbital occupation

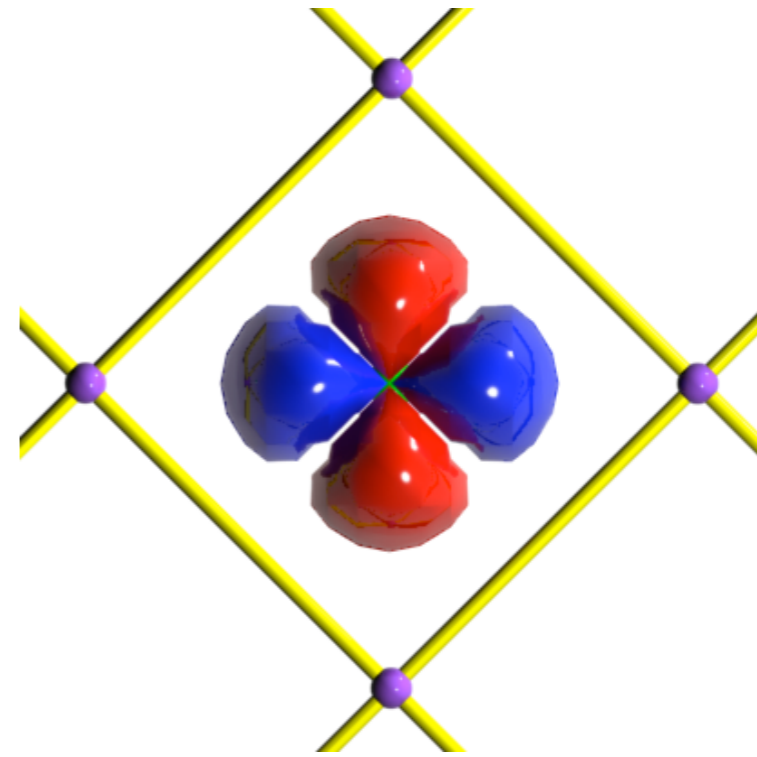
# Wannier Orbitals

Well-localized Cu d orbital obtained: small materials differences.

○  $p_x, p_y$ : strong hybridization.

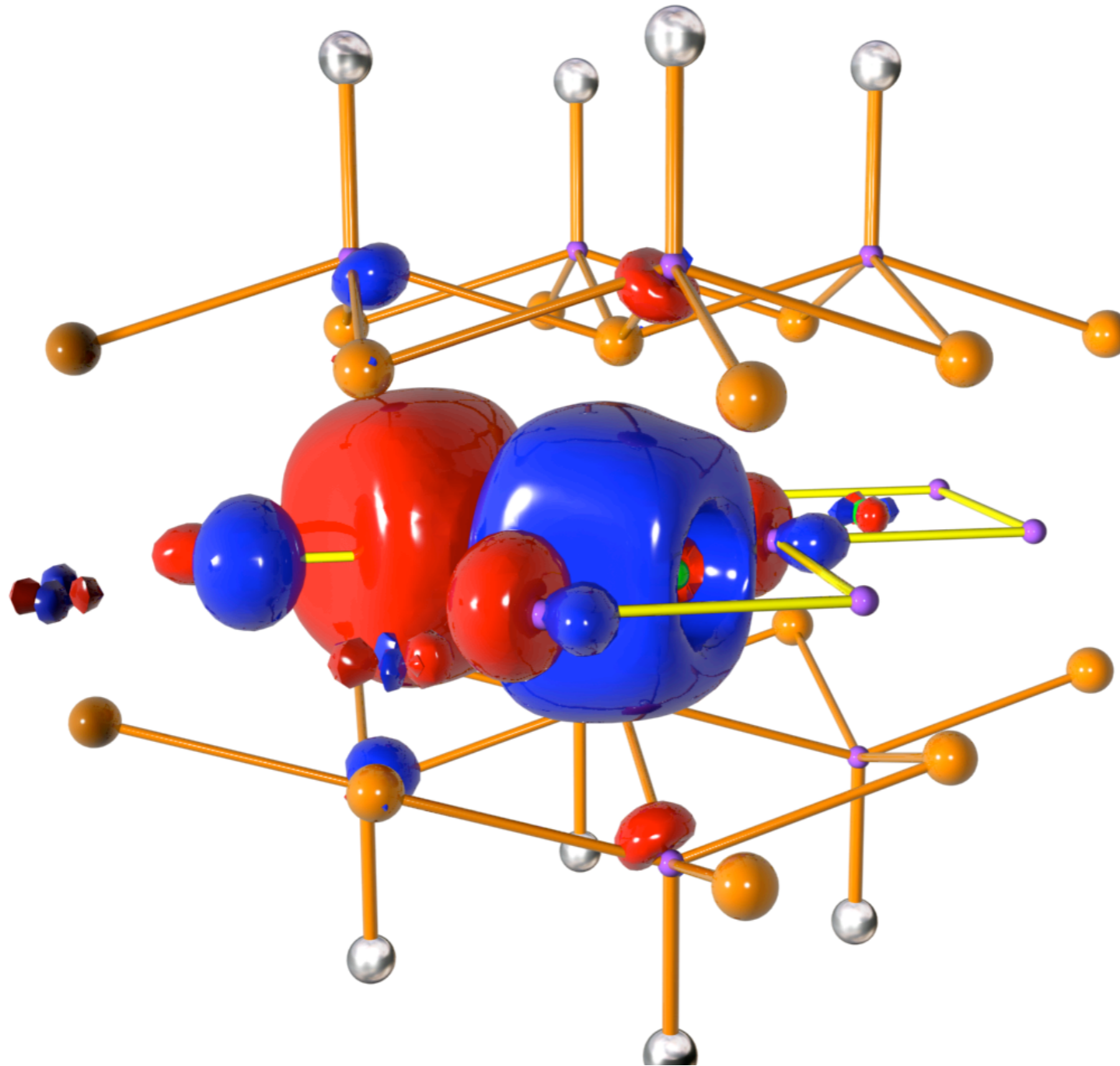


La<sub>2</sub>CuO<sub>4</sub>



HgBa<sub>2</sub>CuO<sub>4</sub>

# Wannier Orbitals



# LDA DCA Hamiltonian

Only the Cu d orbital is correlated

$$H_t = \begin{pmatrix} E_d & V_{1d} & V_{2d} \\ & E_1 & V_{12} \\ & & E_{12} \end{pmatrix}$$

$$E_d(k) = E_d + 2t_{dd1}(\cos(k_x) + \cos(k_y)) + \dots$$

$$E_1(k) = E_p + 2t_{pp1}\cos(k_x) + \dots$$

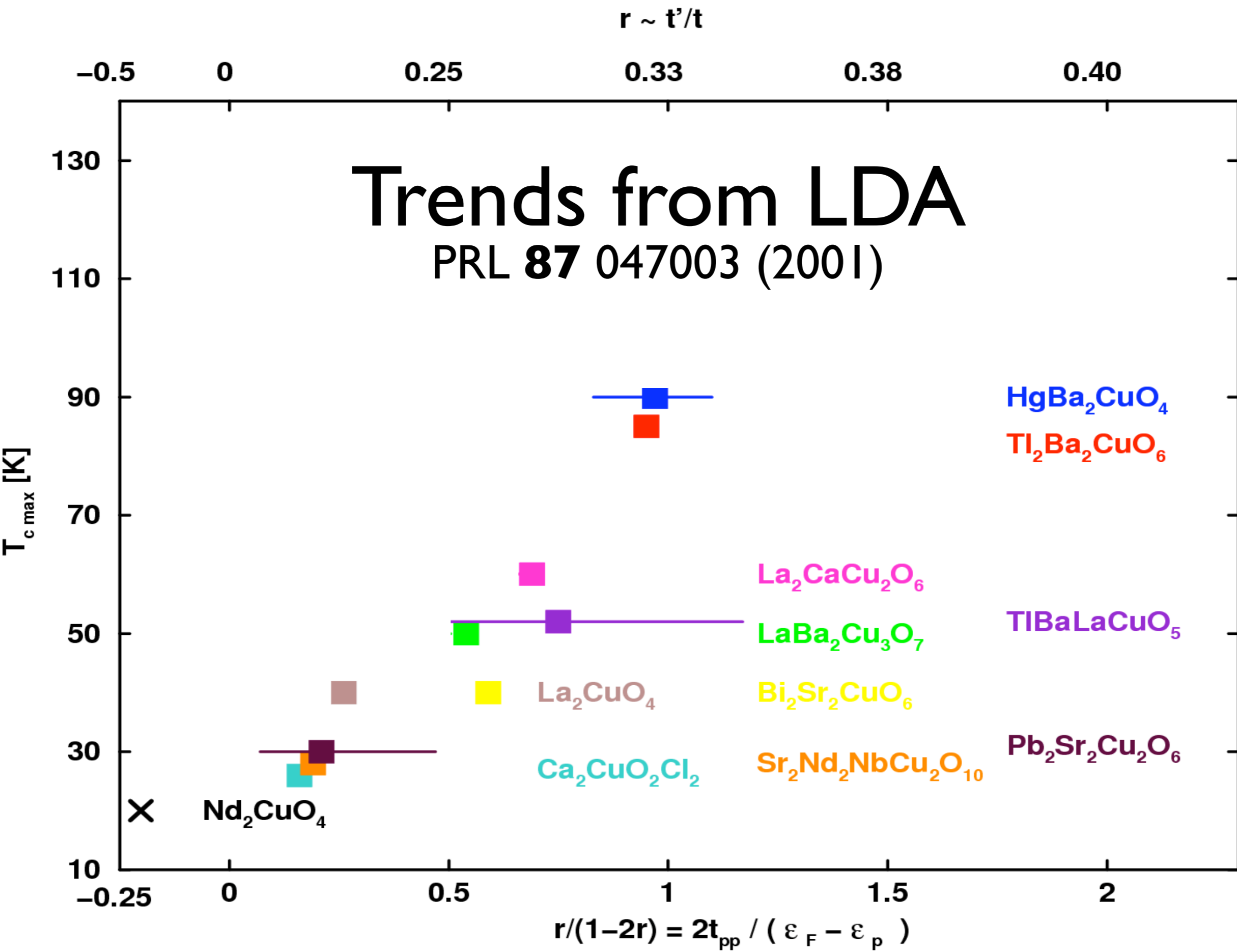
$$V_{1d}(k) = -2t_{pd1}\sin(k_x/2) - 4t_{pd2}\sin(k_x/2)\cos(k_y) + \dots$$

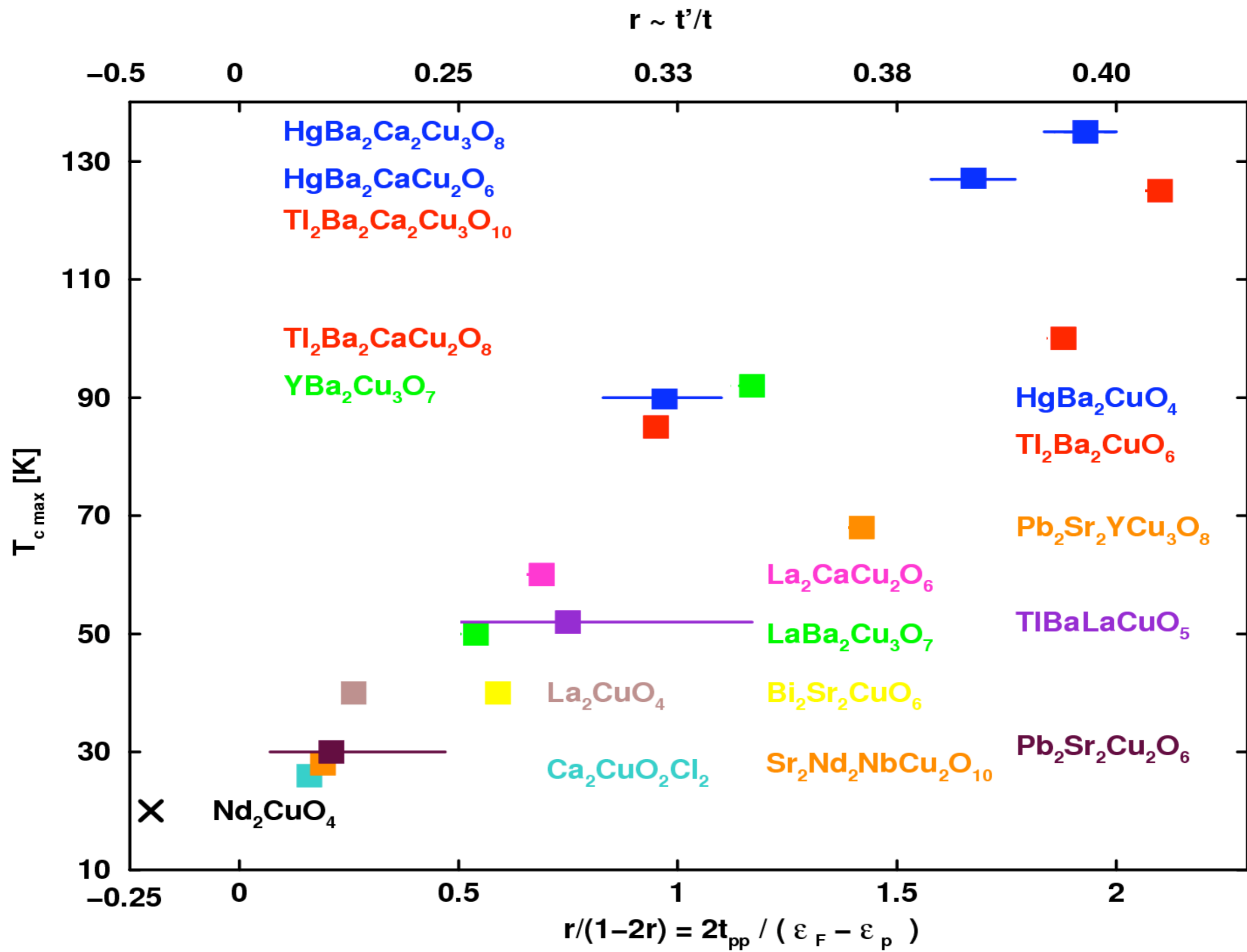
+ Hubbard terms for d orbital



# Can this work?

LDA already shows interesting trends/correlations

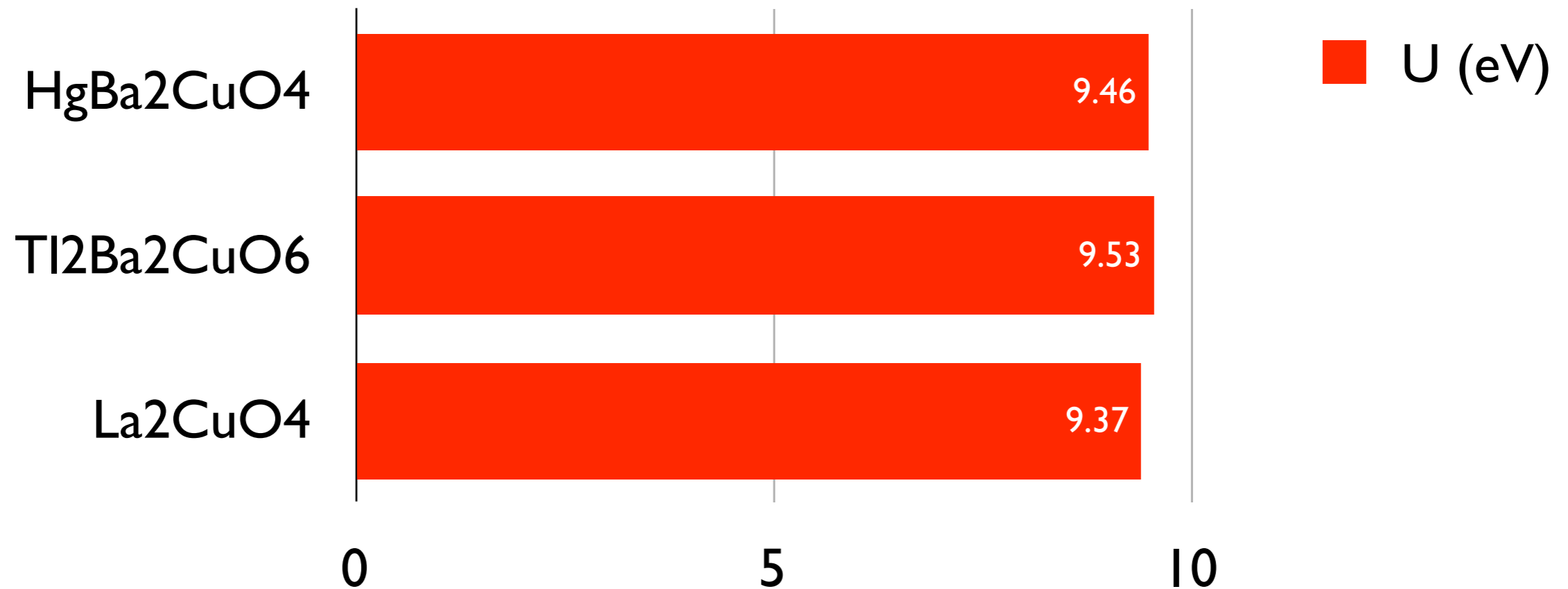




# Outline

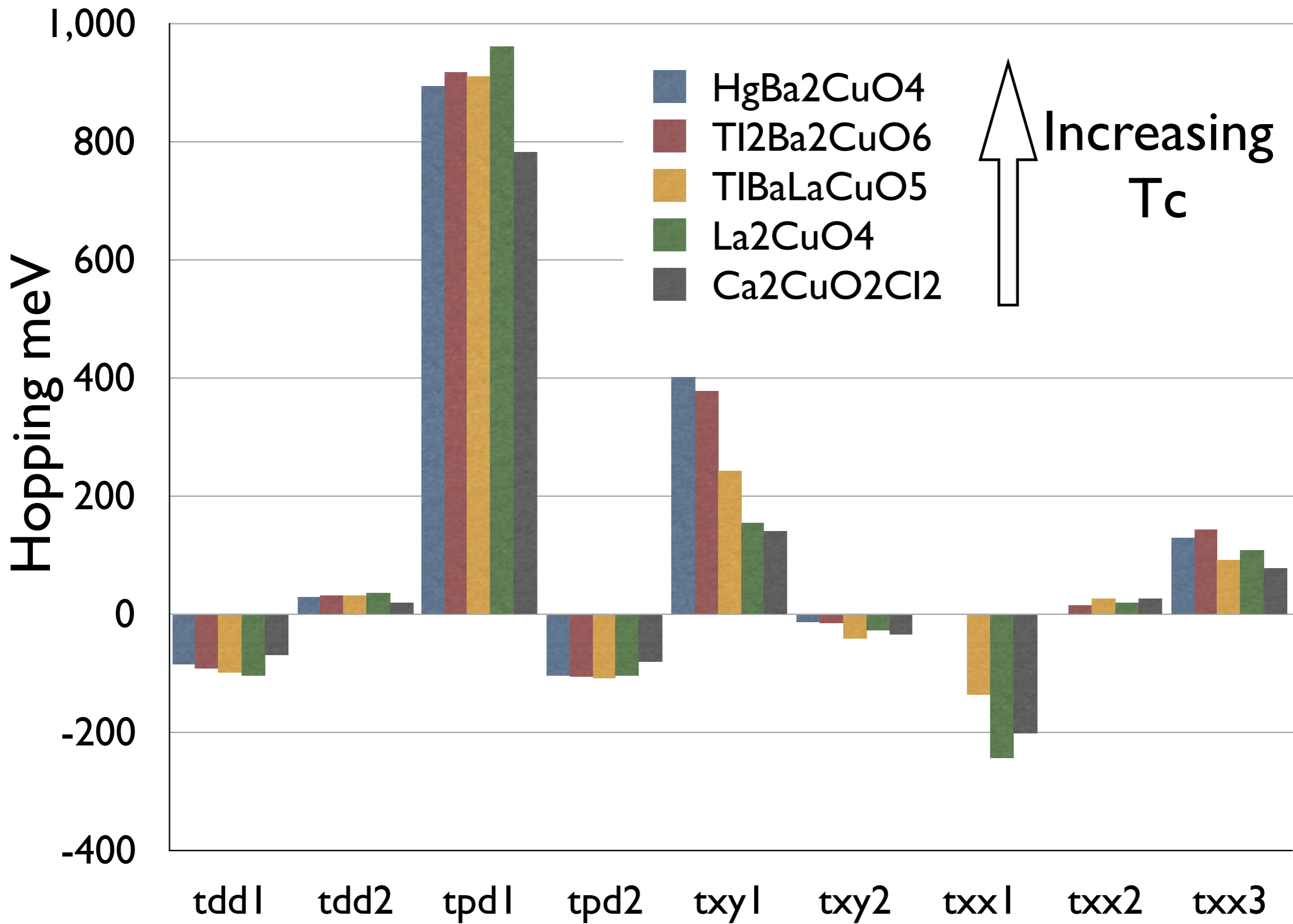
1. Background - Experiment and Theory
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# Calculated U



Few % variation in U; similar in all materials

Any T<sub>c</sub> dependence must reside in Wannier orbitals

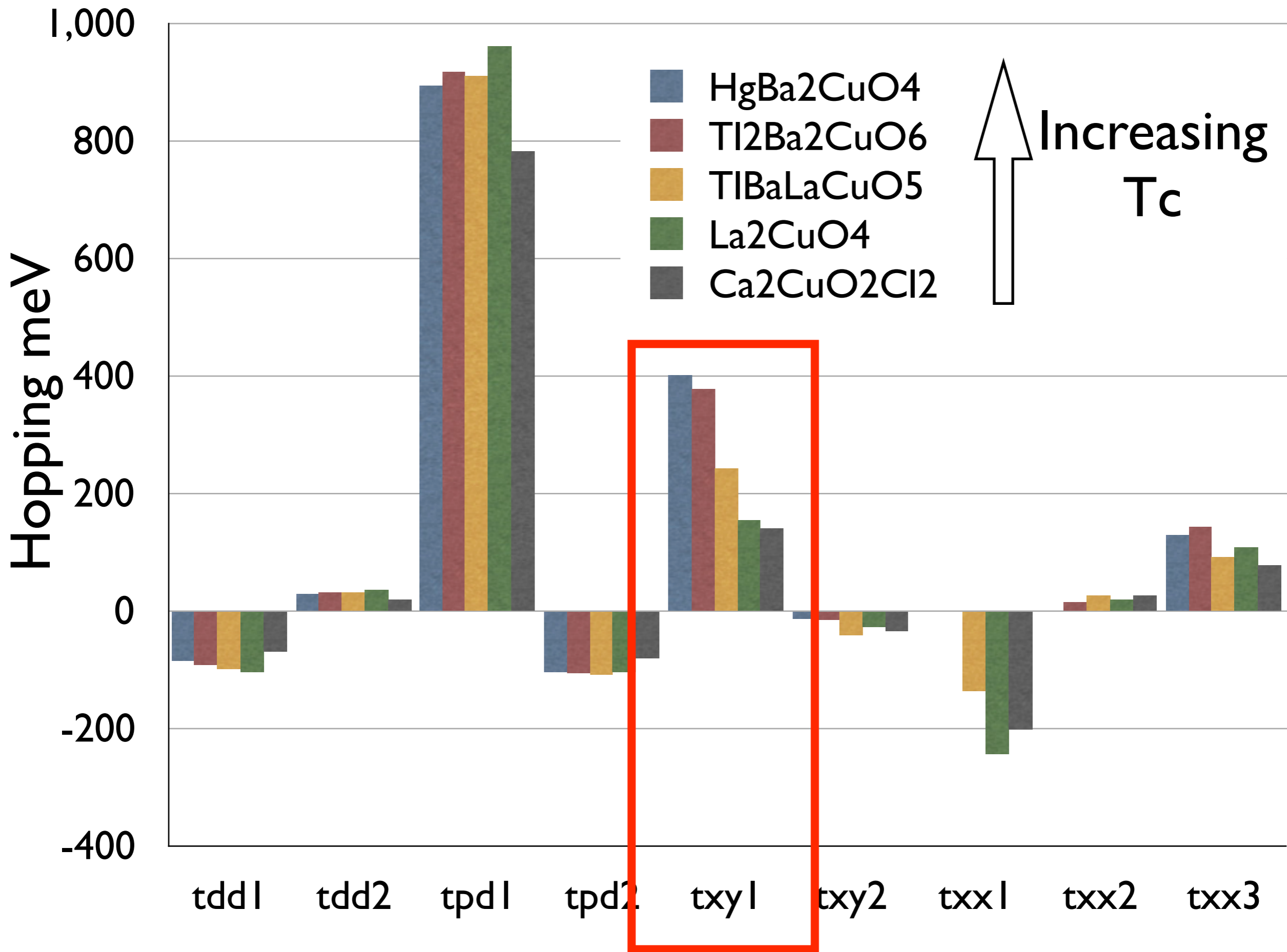


# Downfolding Results

- ~6 terms appear significant, in this basis

*Parametric studies are possible*

- Some terms are ~constant e.g. tpd2
- Some trends apparent e.g. txy1 (=tpp) increases with increasing Tc. Similar to single band observations, but inconclusive.

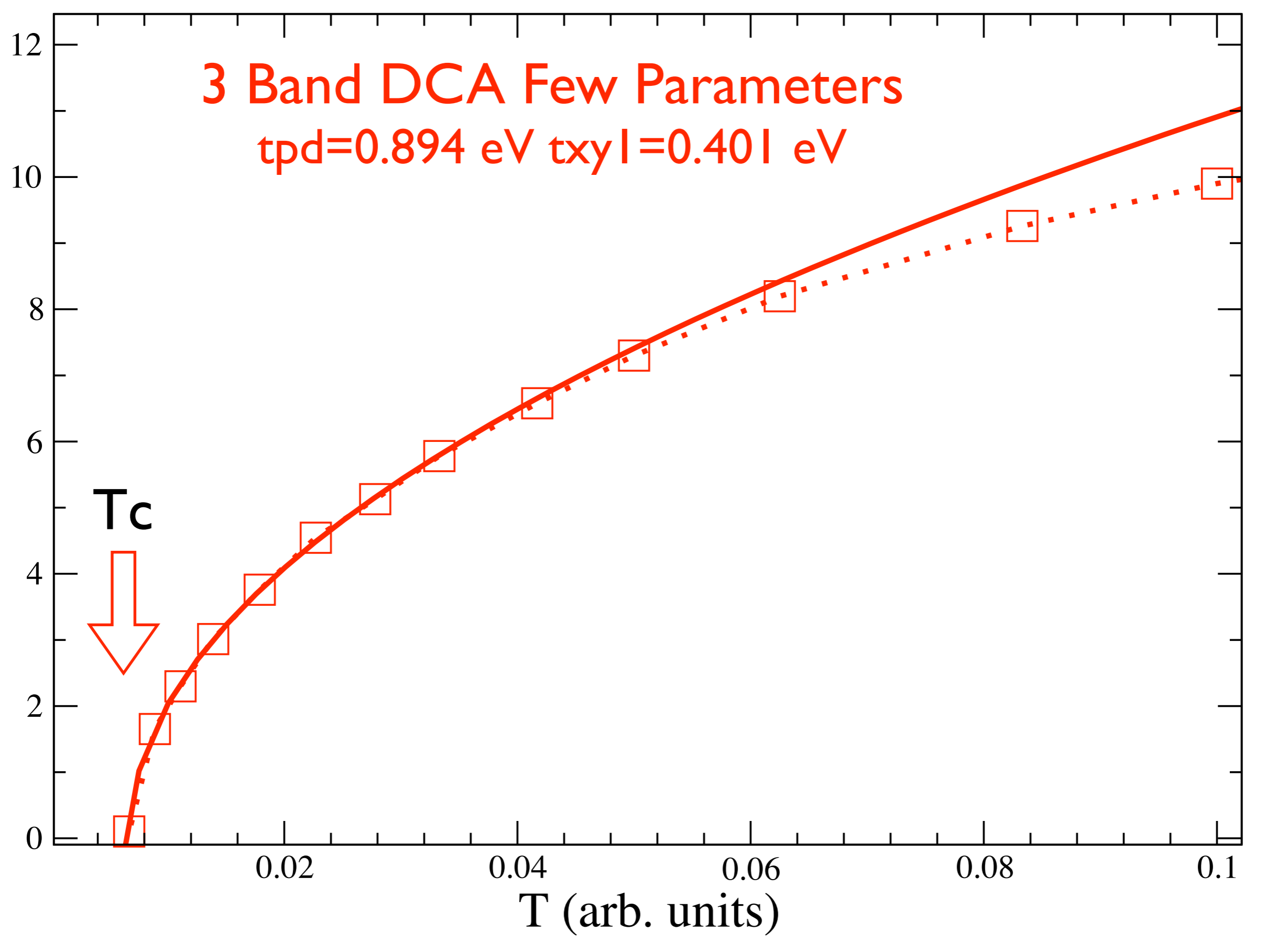
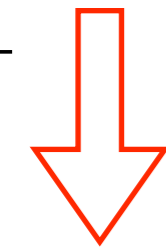


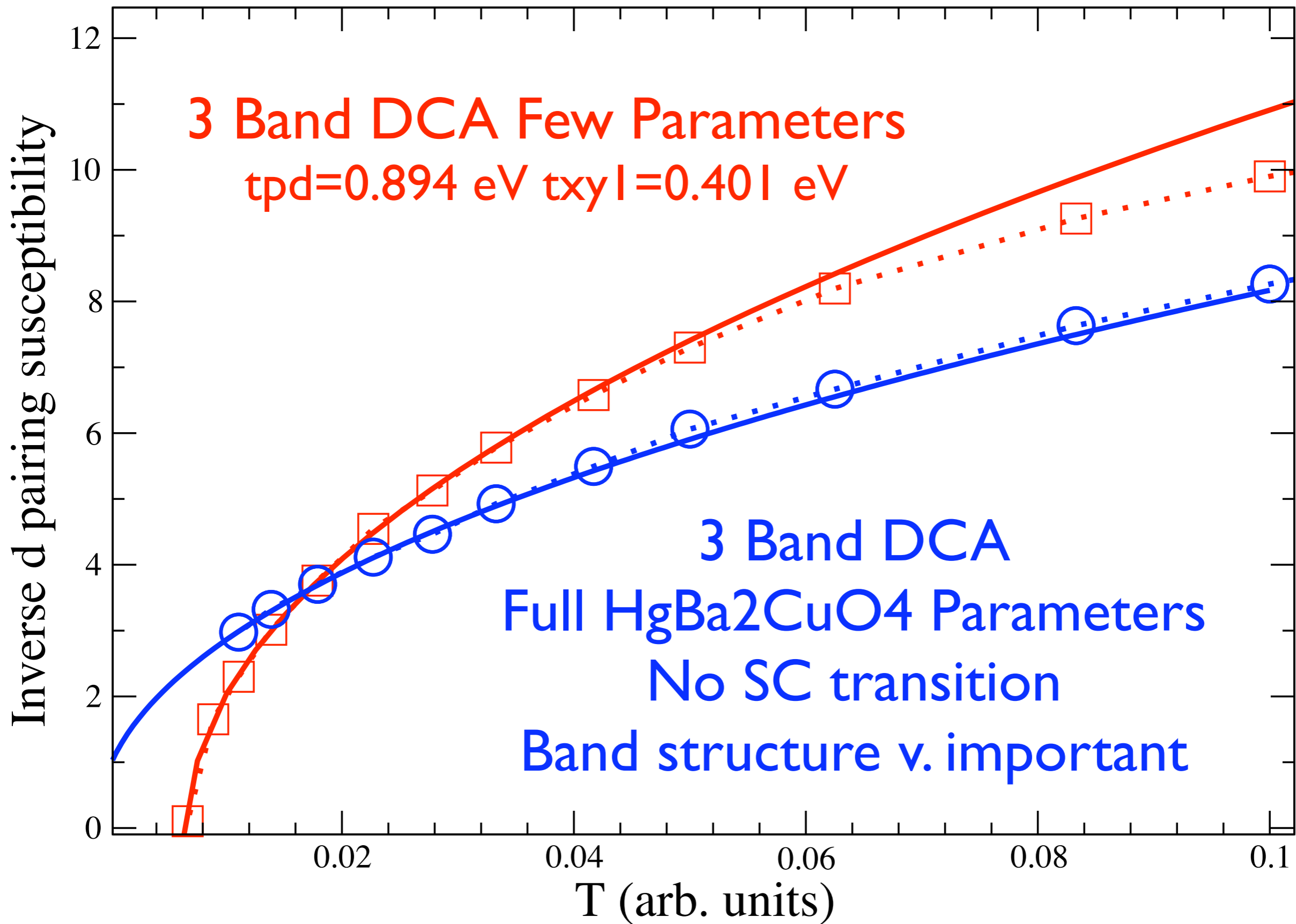


Inverse d pairing susceptibility

3 Band DCA Few Parameters  
 $t_{pd}=0.894$  eV  $t_{xy}=0.401$  eV

$T_c$





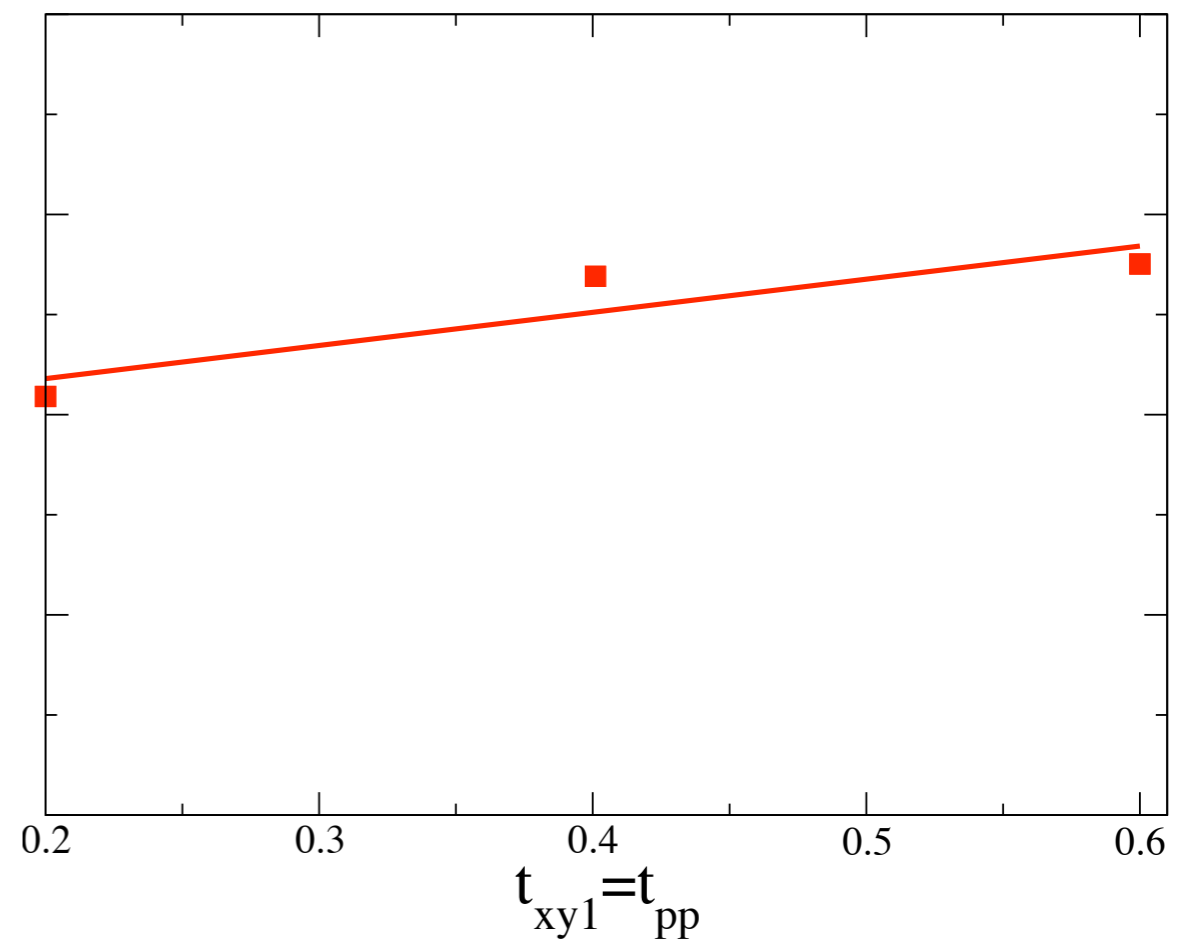
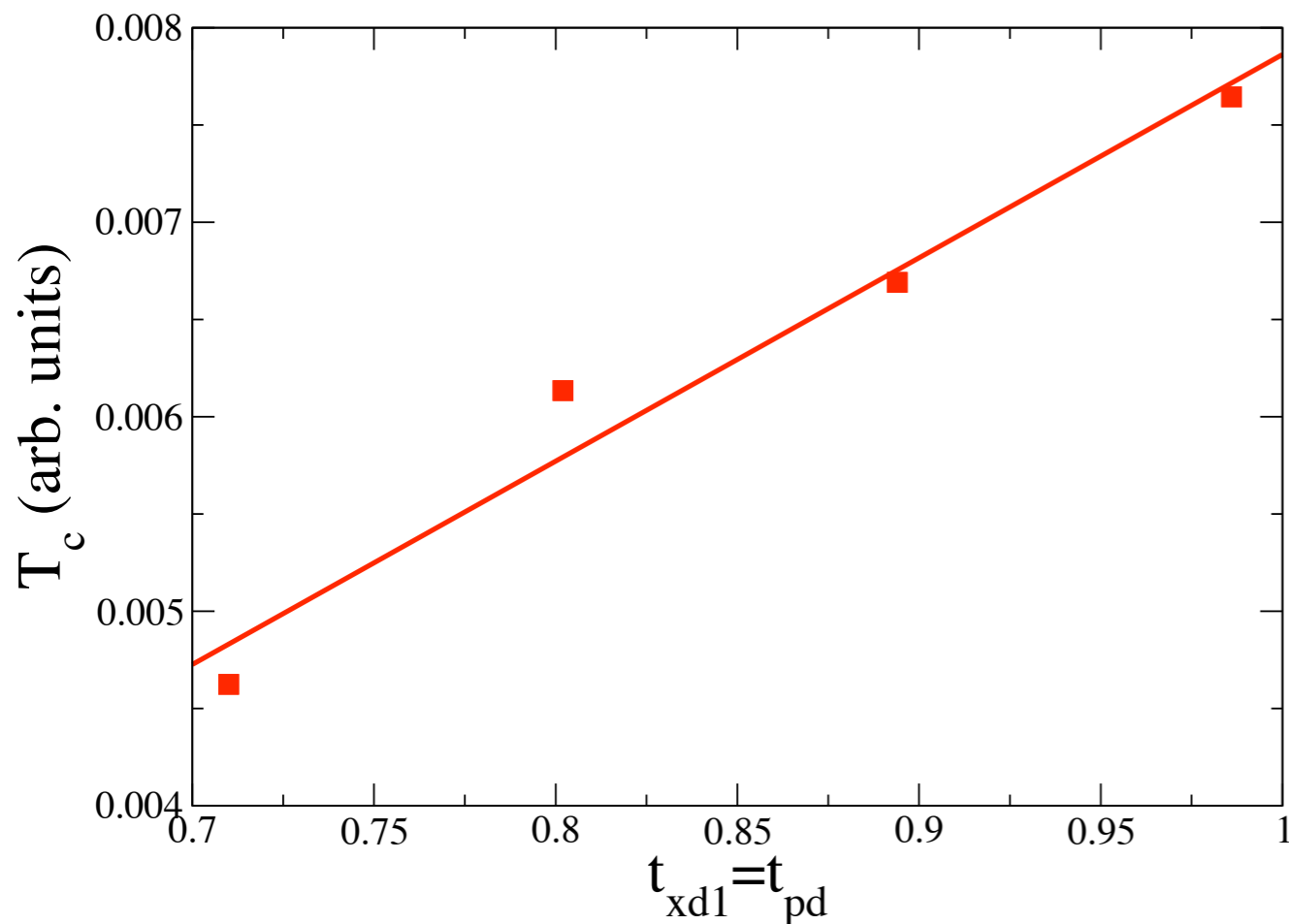
# Bug or Feature?

Favour “feature” - real physics - but checks continue

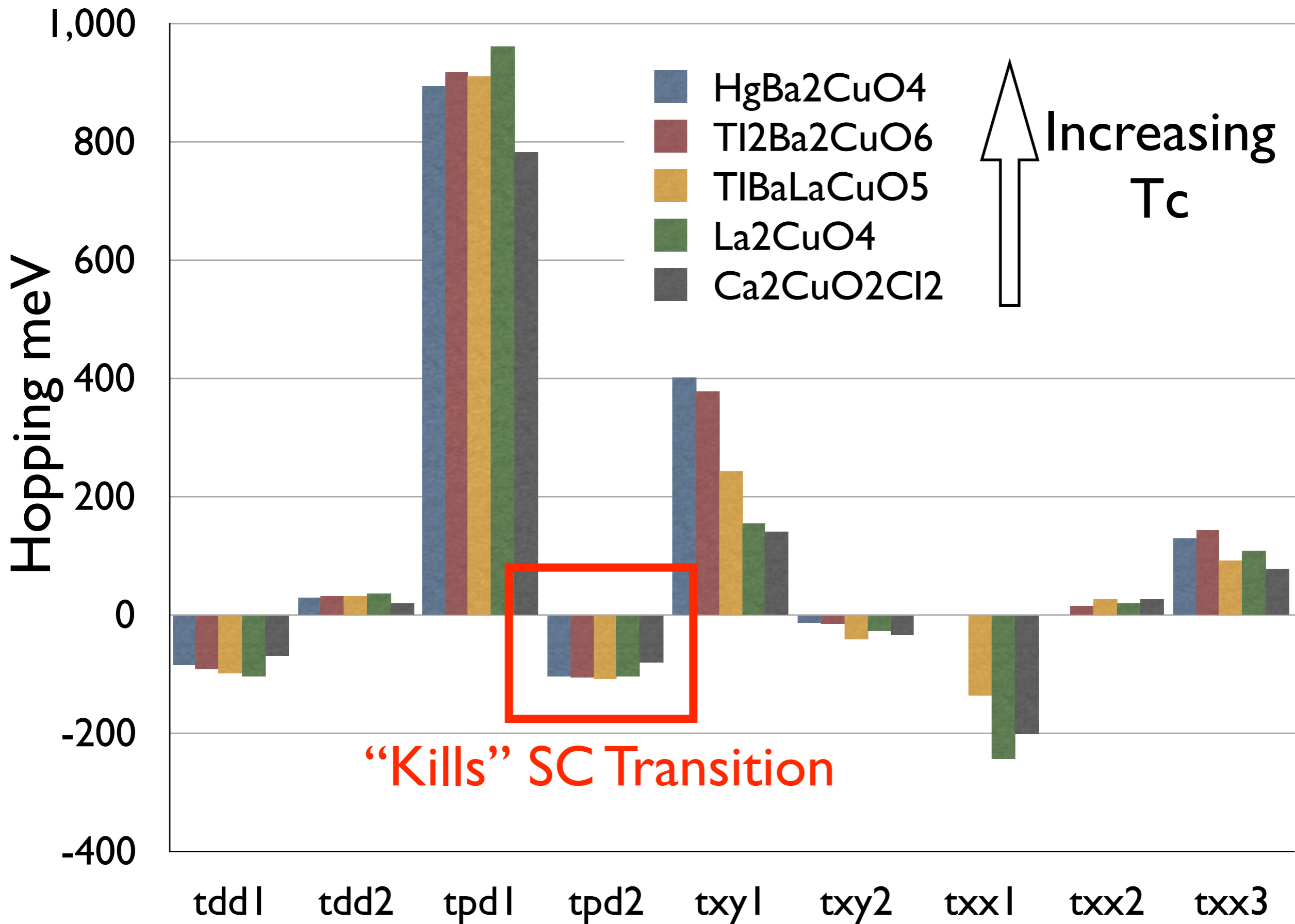
*Unsuspected parameters strongly influence  $T_c$*

# Parametric Results

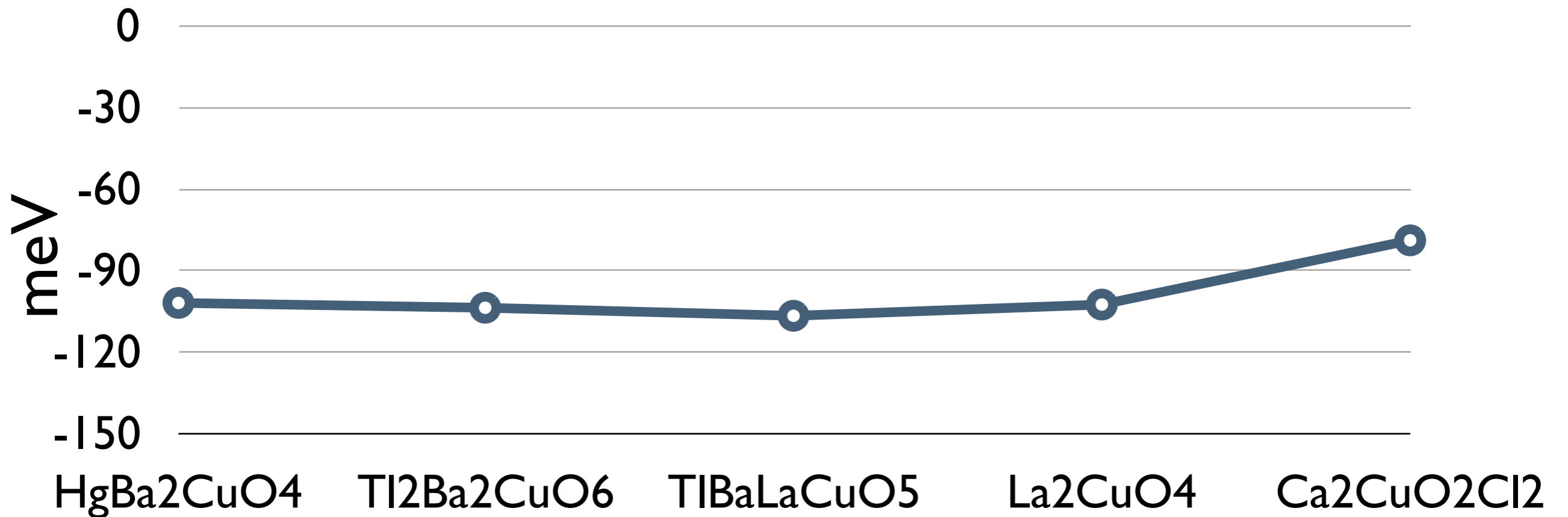
We have checked  $\sim 10$  dependencies in combination



- $T_c$  increases with increasing  $t_{pd}$  and  $t_{pp}$
- $T_c$  not critically dependent on  $U$  above threshold



# Parametric Results



2nd NN Cu-O hybridization strongly governs  $T_c$

Toy model: +ve sign,  $T_c$  increased  $\sim 60\%$  from reference

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# Next Steps

(a) Investigating influence of DFT ground state:

- LDA+U based calculations underway
- Expect “bad” p-d hybridizations to weaken...

...But other hybridizations will also change

(b) Different downfoldings

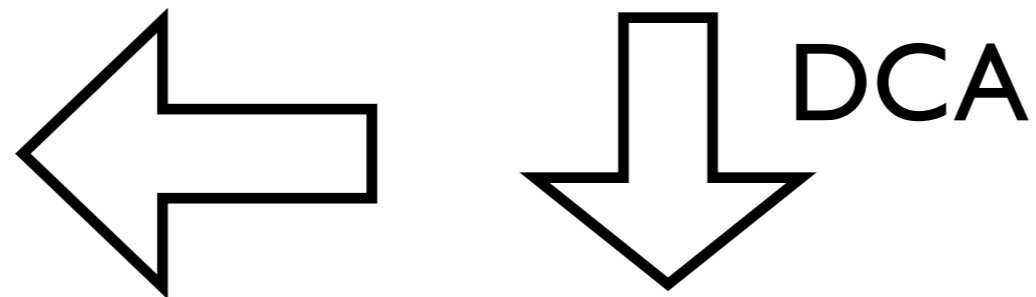
(c) Self-consistency?



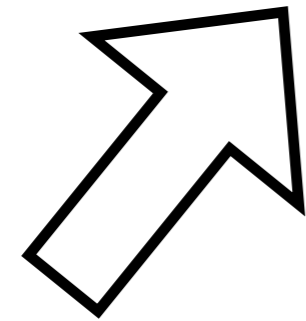
1. DFT LDA ground state



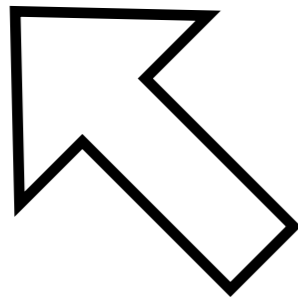
2. Wannier Basis & Hamiltonian



3.  $T_c$ , Phase Diagram



$n'(\mathbf{r})$



# Summary

We have identified a “good set” of parameters for the 3 band Hubbard model. LDA DCA calculations find:

- Strong influence of 2nd NN p-d hybridization. Destroys SC transition with LDA parameters
- $T_c$  scales with 1st NN parameters “correctly”
- A need to go beyond LDA for ground state?

Copies of this talk at <http://www.physics.uc.edu/~pkent>

