

ornl

OAK RIDGE
NATIONAL
LABORATORY

MARTIN MARIETTA

OPERATED BY
MARTIN MARIETTA ENERGY SYSTEMS, INC.
FOR THE UNITED STATES
DEPARTMENT OF ENERGY

MARTIN MARIETTA ENERGY SYSTEMS LIBRARIES

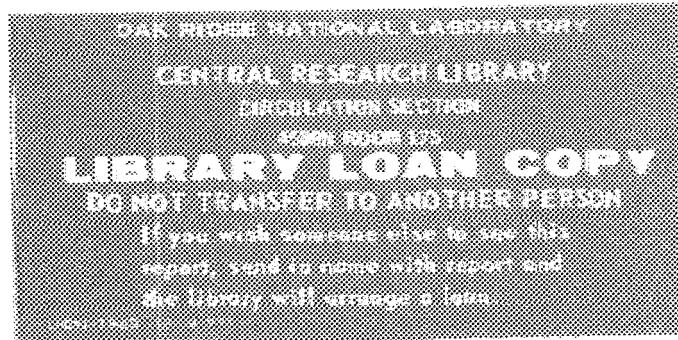


3 4456 0069239 2

ORNL/TM-10069

**RUMS, A PC-Based FORTRAN Program
for Estimating Consumer Surplus
Changes Using Multinomial Logit
and Hedonic Demand Models**

David L. Greene



Printed in the United States of America. Available from
National Technical Information Service
U.S. Department of Commerce
5285 Port Royal Road, Springfield, Virginia 22161
NTIS price codes—Printed Copy: A05 Microfiche: A01

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

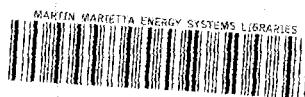
Energy Division

RUMS, A PC-BASED FORTRAN PROGRAM FOR ESTIMATING CONSUMER SURPLUS
CHANGES USING MULTINOMIAL LOGIT AND HEDONIC DEMAND MODELS

David L. Greene

Date Published: August 1986

Prepared by the
OAK RIDGE NATIONAL LABORATORY
Oak Ridge, Tennessee 37831
operated by
MARTIN MARIETTA ENERGY SYSTEMS, INC.
for the
U.S. DEPARTMENT OF ENERGY
under Contract No. DE-AC05-84OR21400



3 4456 0069239 2

CONTENTS

| | <u>Page</u> |
|--|-------------|
| ACKNOWLEDGEMENTS | v |
| ABSTRACT | vii |
| 1. INTRODUCTION | 1 |
| 2. THEORY | 3 |
| 3. IMPLEMENTATION | 7 |
| 4. USER INSTRUCTIONS | 17 |
| 5. REFERENCES | 21 |
| Appendix A. RUMS Program Listing | A-1 |
| Appendix B. Sample Model Runs | B-1 |

ACKNOWLEDGEMENTS

The author thanks Dr. Carmen Difiglio of the Office of Policy Integration, U.S. Department of Energy for his encouragement and support. Thanks are due to the many colleagues who patiently discussed this problem with me, especially Bruce Peterson, Frank Southworth, Dan Hamblin, David Trumble, N. Scott Cardell, and Jin-Tan Liu. Thanks are also due to Stephanie Floyd, who prepared this manuscript.

ABSTRACT

This report describes a computer program for calculating the value, in dollars per consumer, of the difference in consumer satisfaction between two different sets of alternatives from which consumers must choose. Multinomial Logit and Hedonic Demand formulations of discrete choice, random utility models are used to measure the difference in consumer surplus between the two sets of alternatives, which may differ both in number and characteristics. The user must supply attribute weights for the characteristics of interest, as well as quantitative measures of the characteristics themselves. The program also has limited capability to predict changes in market shares resulting from changes in vehicle attributes. Consumer surplus change in the Hedonic Demand Model is estimated by means of Monte Carlo integration. The program is written in FORTRAN 77 for an IBM PC, with an 8087 math coprocessor chip.

RUMS, A PC-BASED FORTRAN PROGRAM FOR ESTIMATING CONSUMER SURPLUS
CHANGES USING MULTINOMIAL LOGIT AND HEDONIC DEMAND MODELS

David L. Greene

1. INTRODUCTION

Random utility models of consumer choice can be used to calculate the change in consumer surplus resulting from a change in the set of choices of goods and their characteristics available to consumers.

Within the context of random utility theory, precise and elegant measures of consumer surplus change can be derived. These measures are sensitive to changes in both the number of choices and the attributes of choices available.

RUMS (Random Utility Models Surplus) is a program for computing consumer surplus changes for fixed coefficient and random coefficient (Hedonic Demand) variants of the multinomial logit model. Given the characteristics of choices in a base and a new choice set, and the values of the respective attribute weights, the model computes the difference in consumer surplus between the two choice sets. The model also has limited capabilities for predicting the effects of changes in characteristics on market shares. Its prediction capability is suited to cases where only part of the typical consumer utility function is known, and where the "new" choice set is a subset of the original. The program is written in Microsoft (TM) FORTRAN 77 for MS- and PC-DOS operating systems.

2. THEORY

Random utility models of consumer choice address the consumer's decision to purchase one discrete item from an array of possible choices which satisfy the same need. The consumer is presumed to select that option which offers him the greatest utility, or satisfaction. The utility (U) of an alternative is assumed to be a stochastic function of the attributes (x_i , $i=1,N$) of the alternative and a set of taste parameters (a_i , $i=1,N$), which describe the weight attached to each attribute in determining utility.

$$U = U(x_i, a_i) . \quad (1)$$

Typically, U is assumed to be linear. The simplest stochastic specification of U is to assume an additive random term (e_{tj}) for each individual, t , and alternative, j .

$$U_{tj} = \sum_i a_i x_{ij} + e_{tj} . \quad (2)$$

If the e_{tj} 's follow the Weibull extreme value distribution, then the probability of consumer t choosing alternative j is given by the multinomial logit (MNL) model (Hensher and Johnson, 1981).

$$P_{tj} = \frac{\exp\{U_{tj}\}}{\sum_k \exp\{U_{tk}\}} . \quad (3)$$

The functions $\exp\{ \}$ and $\ln\{ \}$ indicate exponentiation and natural logarithms. If, in equation (2), the parameters a_i are also assumed to be randomly distributed over the population of consumers according to

lognormal distributions (e_{tj} 's still distributed extreme value) then the Hedonic Demand Model (HDM) results (Beggs, 1981). The HDM is considerably more complex, since evaluating the probability of choice of j requires integrating over the probability distribution of all N attribute weights. This involves a multiple integral with order equal to the number of attributes.

The concept of consumer's surplus recognizes that when the price of a good changes, the consumer will experience a change in utility which can be translated into dollars (e.g., Varian, 1978, p. 209). Consider a consumer with a demand function for good j a function of prices of all goods, p , and income, y . By using Roy's identity x_1 can be expressed in terms of the consumer's indirect utility function U ,

$$x_1(p, y) = - \frac{\partial U(p, y)}{\partial p_1} / \frac{\partial U(p, y)}{\partial y} . \quad (4)$$

If p_1 changes, the consumer's surplus will equal the area under the demand curve between the initial, p_1^i , and final, p_1^f , prices,

$$\begin{aligned} \Delta CS &= \int_{p_1^f}^{p_1^i} x_1(p, y) dp_1 \\ &= \int_{p_1^f}^{p_1^i} - \frac{\partial U(p, y)}{\partial p_1} / \frac{\partial U(p, y)}{\partial y} dp_1 . \end{aligned} \quad (5)$$

If the marginal utility of income is constant (as in the linear utility function (2) above), the integral (5) becomes

$$\Delta CS = \frac{1}{a_0} [U(p^f, y) - U(p^i, y)] , \quad (6)$$

where a_0 is the marginal utility of income.

It is intuitively clear that when the number of choices available to consumers, or the attributes of choices available are changed, the levels of satisfaction which can be reached may (generally, will) also change. In a discrete choice situation, the demand for an alternative, x_j , can be written,

$$x_j(p, y) = P_j[U^1(p, y), U^2(p, y)] . 1 , \quad (7)$$

since only one unity of x_j will be consumed if x_j is chosen, and it will be chosen with probability P_j , a function of the utility levels of j and all other alternatives. This demand function can be integrated over changes in utility brought about by price changes, or any other changes which cause the utility of alternatives to change. For the MNL model, it can be shown (Williams, 1977; Small and Rosen, 1981) that the precise change in the consumer surplus (satisfaction measured in dollars) is,

$$\$CSL = \sum_t (1/a_0) [\ln\{\sum_{j:M2} \exp\{U_{tj}(a, x')\}\} / \sum_{j:M1} \exp\{U_{tj}(a, x)\}] . \quad (8)$$

For the HDM, the corresponding consumer surplus change is given by (Cardell and Dunbar, 1980),

$$\$CSL = T \int \dots \int (1/a_0) \ln\{\dots\} f(a|m, \Sigma) da , \quad (9)$$

where M_1 and M_2 represent the base and new choice sets with x' being the new characteristics of choice set M_2 . The expression $\ln\{\dots\}$ represents the same log term as in equation (8). The probability distribution of the a_i 's is $f(a:m,\Sigma)$, m representing the vector of means of the a_i 's and Σ their variance-covariance matrix (assumed here to be diagonal).

Finally, a_0 is the weight of the price of the alternatives, so that $(1/a_0)$ translates the utility measure U into dollars. The integral (9) must be computed by numerical techniques, and since the number of integrals is typically greater than four, Monte Carlo methods are most appropriate.

In order to compute the change in consumer surplus, one must know the attribute values for elements of the choice sets M_1 and M_2 , and the relevant attribute weight parameters. For the HDM, this includes both the mean and variance of each attribute weight. When the probability distribution of the attribute weights is assumed to be lognormal, the signs of the weights must also be specified. Given these data, RUMS can be used to calculate the change in consumer surplus.

3. IMPLEMENTATION

The calculation of consumer surplus using the multinomial logit and hedonic demand models has been implemented for microcomputers using Microsoft (TM) FORTRAN 77. Structured programming techniques were used, so that the program would be as clear as possible. The essence of the program is as follows:

1. A "setup" routine interactively prompts the user to determine the type of model (MNL or HDM), the type of operation (consumer surplus calculation or prediction), and to describe the format of the input data files. There are two input data files which are assumed to be on disk drive B: 1) PARAMS.DAT, which contains the relevant model parameters, and 2) CHARS.DAT, which contains the characteristics of each choice set. These data sets are explained in more detail below.
2. Subroutines read the parameter (PAR1, PAR2) and characteristics (CHOICE) data sets.
3. Subroutines (WEIGHTS, SHRS, SUM) compute weights if any are to be used in the calculation of consumer surplus. If the model is to be used for prediction, other subroutines (CALIB,BSUM1, BSUM2,SUM) calibrate the model to the actual market shares of the base year choice set. This step is especially important when characteristics and attribute weights are available for only a subset of the full complement of relevant characteristics.

4. If the model is MNL, subroutines are called which compute the consumer surplus change (SURPLS,ACCUM). If the operation is prediction, these are skipped and the MNL prediction subroutine (PRED1) is called.
5. If the model is HDM, calculations must be done by means of Monte Carlo integration. For consumer surplus, subroutine HDMSUR is called. HDMSUR calls RANSET, which requests the number of iterations and a seed for the subroutines which generate pairs of independent normal random numbers (RANDCO, NORMAL,RAN1) and then use these to generate a set of log-normally distributed random coefficients. Each set of coefficients is, in turn, passed to the subroutines which calculate consumer surplus change (SURPLS,ACCUM), or predict the changes in market shares (PRED2). The average change over all iterations is then computed.
6. Finally, a subroutine (SURPRN or PREPRN) is called which prints the results.

The flow chart in Figure 1 illustrates the above process. While the calculation of consumer surplus in the MNL model is essentially instantaneous, calculations for the HDM can be time consuming. The amount of time required is primarily a function of the number of characteristics (attributes) rather than the number of choices since the number of characteristics determines the number of random numbers which must be generated. For a small choice set (six choices) and six attributes, a Monte Carlo simulation of 1000 iterations requires twenty minutes of run time on an IBM-PC (TM) without the faster 8087 math coprocessor chip.

ORNL-DWG 86-13554

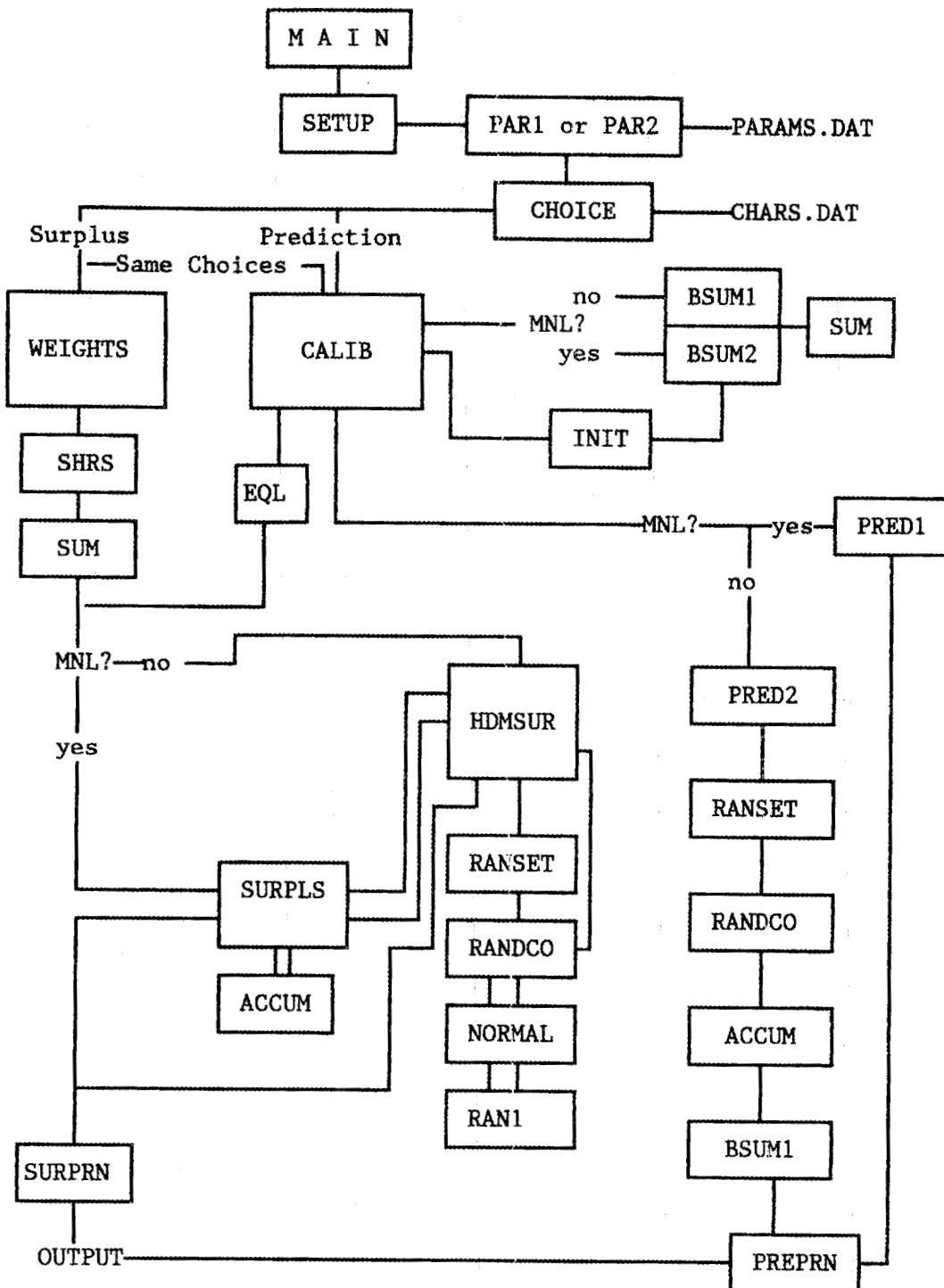


Fig. 1. Flow chart of RUMS3.

The same problem requires less than two minutes on an IBM PC equipped with an 8087 chip. Increasing the number of attributes would increase the run time roughly proportionately.

Three choices are available for computing consumer surplus using either the MNL or HDM models: 1) unweighted, 2) market share weighted, or 3) with calibration constants for the special case where the characteristics of alternative choices change but the membership of choice sets 1 and 2 is the same. If the utility function described by the available characteristics is considered to be complete, that is, either no attributes are missing or those that are missing are uncorrelated with those present, then unweighted calculation is appropriate. In many cases, however, a large number of relevant attributes may be missing. If this is believed to be true then it may be preferable to compute a market shares weighted consumer surplus. In the special case that exactly the same alternative choices are available in both sets, but with somewhat changed characteristics, a calibration method can be used to complete the utility value for each alternative.

The method of market shares weighting is novel and, thus, needs some explanation. The linear utility function can be partitioned into unknown (A) and known (B) parts,

$$U_j = A_j + B_j . \quad (10)$$

The unknown part, A, represents, in effect, a weight for the known part in the logsum terms of equations (4) and (5).

$$\ln\{\sum_j W_j \exp\{B_j\}\} , W_j = \exp\{A_j\} . \quad (11)$$

If A_j is very large relative to B_j , then the market share of alternative j , P_j , can be used as an approximation to W_j .

It can be shown that the estimated change in consumer surplus obtained by using P_j as a weight is the consumer surplus change with B_j multiplied by 2 minus the actual consumer surplus change. By inserting the definition of p_j from (3) into (11), and using the partitioning of the utility function in (10), one obtains,

$$\begin{aligned} \ln \sum_{j:M} p_j e^{B_j} &= \ln \sum_{j:M} (e^{U_j + B_j} / \sum_{i:M} e^{U_i}) \\ &= \ln [(\sum_{i:M} e^{U_i})^{-1} (\sum_{j:M} e^{A_j + 2B_j})] . \end{aligned} \quad (12)$$

This, of course, is half of the formula for consumer's surplus. The full expression is,

$$\begin{aligned} \Delta CS &= \frac{1}{a_0} \ln [(\sum_{i:M2} e^{U_i})^{-1} (\sum_{j:M2} e^{A_j + 2B_j}) / \\ &\quad (\sum_{k:M1} e^{U_k})^{-1} (\sum_{\ell:M1} e^{A_\ell + 2B_\ell})] \\ &= (1/a_0) [\ln \{\sum_{j:M2} \exp\{A_j + 2B_j\} / \sum_{j:M1} \exp\{A_j + 2B_j\}\} - \\ &\quad \ln \{\sum_{j:M2} \exp\{A_j + B_j\} / \sum_{j:M1} \exp\{A_j + B_j\}\}] . \end{aligned} \quad (13)$$

The second line of equation (13) is the total consumer surplus change as shown in equation (8). The first part is also a kind of total consumer surplus change but with the values of the observed variables doubled.

The difference is an approximation to the consumer surplus change due to changes in observed variables alone.

A heuristic interpretation of (13) can be based on equation (6) which states that consumer's surplus is equal to a change in utility levels translated into dollars. Using the partitioning of the utility function into known and unknown parts, together with the fact that the utility functions are linear, we can see that in equation (13) we are subtracting a ΔA plus ΔB (the actual change in utility) from a ΔA plus $2\Delta B$. This would give exactly ΔB were it not for the fact that probabilities of choosing alternatives changes (in a nonlinear way) as their utility levels change. As a result, (13) is an approximation only, and likely to be good only for small changes in utility levels.

If B_j is very large relative to A_j , then B_j approaches the total utility function and no weights are needed. If A_j is very large relative to B_j , then shares-weighting should be better. Since neither of these two conditions is likely to be exactly true, it will usually be wise to carry out the estimation with and without weighting in order to bound the inaccuracy caused by an incomplete representation of the utility function.

In the special case that there are no changes in the membership of choice sets 1 and 2 and (only the observed characteristics of the alternatives change, a more precise method can be used. This third method calculates constants A_j such that, given the observed characteristics and attribute weights of choice set 1, the MNL (or HDM) model will predict the actual market shares exactly. The method of calculating the A_j is the same as that used when RUMS is used for shares prediction and

is described below. The A_j from choice set 1 are added to the B_j for choice sets 1 and 2 in computing consumer's surplus.

The market shares weighting method treats the missing part of the utility function as nonstochastic. This is actually not consistent with the HDM, where the entire utility function is stochastic. Unfortunately, there are insufficient degrees of freedom to estimate both the weights and their variances. Thus, when the HDM is used and the variance of the missing portion of the utility function is believed to be important, one must interpret the computed consumer surplus changes with caution.

The inclusion of weighting factors in the model accomplishes two things: 1) it weights the changes in utility for individual choices according to their market share, so that changes in very popular models will count more than changes in rare ones, and when market shares weighting is used, 2) it allows for changes in other, unmeasured attributes from one time period to the next. These refinements should increase the accuracy of the estimated changes in consumer surplus.

When RUMS is used for prediction, it must be calibrated so that it accurately predicts the base year shares. Calibration of the model consists of computing constants for each member of the choice sets such that the multinomial logit or hedonic demand models predict exactly the observed market shares for each alternative. Again, consider the representative utility function as being composed of two parts: 1) the utility derived from the attributes for which we have measures, and 2) the utility derived from all other factors. The linear utility function of equation (2) can be partitioned into the calibration constant, A_j , and the remaining sum of attributes times attribute weights:

$$U_j = A_j + \sum_i a_i x_{ij} . \quad (14)$$

Equation (14) can be substituted in equation (3), and the probability of individual t choosing j replaced by the observed market share of j . This gives a set of M (the number of alternatives) equations in M unknowns (the A_j). However, the sum of shares must equal 1, so that one of the A_j must be chosen arbitrarily to satisfy this constraint.

A particularly convenient estimating equation can be derived by first taking the ratio of the shares of alternatives j and k :

$$P_j/P_k = (\exp\{A_j\}\exp\{B_j\})/(\exp\{A_k\}\exp\{B_k\}) , \quad (15)$$

where B_k represents the summation term of equation (6) for alternative k . Taking logarithms and rearranging gives:

$$A_j = \ln\{P_j\} - \ln\{P_k\} + (B_k - B_j) + A_k . \quad (16)$$

Now if we express each share relative to alternative 1 and choose $A_1 = -B_1$, then the remaining A_j 's can be computed using:

$$A_j = \ln\{P_j\} - \ln\{P_1\} - B_j . \quad (17)$$

It can be easily shown that A 's computed in this way will yield shares which sum to one for any B 's.

Calibration of the Hedonic Demand Model differs slightly from the Multinomial Logit in that there is no single value for an attribute weight. Instead, the mean is used. Since the parameters are lognormally distributed, the means are,

$$\exp\{m_i + 0.5s_i^2\} , \quad (18)$$

where m_i and s_i are parameters of the lognormal distribution. Clearly, there are insufficient degrees of freedom to compute both A's and variances for the A's. Thus, the A's are constants which produce constant weighting factors for each alternative. This is not an exact representation of the HDM, since it allows random coefficients only for those attributes which are explicitly included. Still, it appears to be the best that can be done, and is undoubtedly superior to ignoring the calibration constants altogether.

Computation of consumer surplus is accomplished according to the formulas described in Section 2. Generation of normally distributed random numbers is accomplished in two steps. First, uniform random numbers on the interval [0,1] are generated using an algorithm proposed by Monro (1982, pp. 52-53). Next, two successive, independent uniform random numbers (R_n , R_{n+1}) are transformed to produce a pair of independent normal (0,1) random numbers (S_n , S_{n+1}) using a method proposed by Wilf (1967, p. 255). Wilf's transformation equations are as follows:

$$\begin{aligned} S_n &= (-2\ln\{R_n\})^{1/2} \cos\{2(\pi)R_{n+1}\} \\ S_{n+1} &= (-2\ln\{R_n\})^{1/2} \sin\{2(\pi)R_{n+1}\} . \end{aligned} \quad (19)$$

These normal random variates are used to produce lognormally distributed attribute weights using the given lognormal parameters, m and s , and the transformation,

$$a_i = \text{sgn}(i)\exp\{m_i + S_n s_i\} . \quad (20)$$

In (20), the term $\text{sgn}(i)$ represents + or - 1 depending on the sign of the attribute (i.e., whether more of it is good or bad). When the parameters are assumed to be distributed lognormally, the sign of each must be specified a priori. For the HDM, then, the parameter data set (PARAMS.DAT) contains three values for each attribute: the lognormal parameters m and s , and the sign of the attribute weight (+/-1).

4. USER INSTRUCTIONS

This section describes how to set up the model on an IBM (TM) PC with two disk drives. The program will run without an 8087 coprocessor chip, but this will slow the execution time greatly. This is followed by a sample run including sample data sets of parameters and attributes based on an automobile choice model by Boyd and Mellman (1980). Finally, common problems which may be encountered are discussed.

The first step is to start the computer and install the disk operating system (DOS). The program RUMS.EXE should be available on diskette or hard disk. It does not matter in which drive this diskette is placed, however, because the program will prompt the user for the names of required data files. The user must supply a complete pathname for each data file. If the user has a hard disk or can set up a ramdisk, it may be worthwhile to read data from disk c: to increase the program's speed. If the number of alternatives is large (say 100 or more) this can significantly reduce execution time.

Two separate data files are required:

1. The first file must contain the necessary parameter values (in the examples this is called PARAMS.DAT). For the MNL model, the program will read the i attribute weights, in order, using an implied DO loop. The first parameter must always be the attribute weight for the price of the good. For the HDM, the program consecutively reads the lognormal parameters m (the logarithm of the median), s (the standard deviation of m), and sign, before proceeding to the next attribute weight.

2. the file containing the attributes of all elements in both the base and new choice sets (called CHARS.DAT in the sample runs). Each alternative constitutes one record. The order of attributes in this file must be the same as that in PARAMS.DAT. The first variable in each record must be the alternative's price, the last variable must be either the total sales or the market share of that alternative. All base choice set elements and attributes must appear first, followed by the attributes of the new choice set. The model will assume that the first M1 records are the base alternatives and the following M2 records are the new alternatives attributes.

The user will be prompted to specify the following information:

1. type of model (MNL or HDM),
2. type of operation (Consumer's Surplus or Prediction),
3. numbers of elements in the base and new choice sets,
4. number of characteristics (including price but not sales or shares),
5. record formats (FORTRAN format statements) for the parameter and characteristics data files (both may be printed, if desired), and
6. the type of weighting to be used if consumer surplus change is to be computed.

The sample runs in Appendix A illustrate these prompts. The user responses are in lower case letters. The user must hit the carriage return (or ENTER key) following each response. The parameters and data used in the samples have been borrowed from Boyd and Mellman (1980).

The program may fail to operate as expected for several reasons. The most common will probably be that the attribute weight parameters specified are unrealistic. The result is most often a real math overflow error, although an underflow can also result. This is most likely to be a problem with the HDM model, where the Monte Carlo simulation may produce values too large to exponentiate (the current version of the program uses double precision real numbers for such calculations). The values of m may be too large, or it may be that the variance of m , s , is too large and occasionally produces a very large number when a large random number is generated. Similar errors can also occur when attribute data are unrealistic (e.g., cause the utility function to take on values as large as 80 or higher). Such problems can usually only be solved by correcting errors in or changing the values of the attribute weight parameters or characteristics data, although simply changing the random number seed may provide a quick fix on rare occasions.

Since these kinds of errors are indicative of problems with the model parameters being used (because they suggest that unreasonably large, or small, values are being placed on some attributes), it is generally unwise to ignore them. When overflow errors are encountered, the user should carefully examine the model parameters and data being used.

5. REFERENCES

1. Beggs, S. D., 1981. "The demand for electric automobiles," EA-2072, Research Project 1145-1, for the Electric Power Research Institute, Palo Alto, California, October 1981.
2. Boyd, J. H. and R. E. Mellman, 1980. "The effect of fuel economy standards on the U.S. automotive market: an hedonic demand analysis," Transportation Research, vol. 14A, no. 5-6, pp. 367-378, October-December 1980.
3. Cardell, N. S. and F. C. Dunbar, 1980. "Measuring the societal impacts of downsizing," Transportation Research, vol. 14A, no. 5-6, pp. 423-434, October-December 1980.
4. Hensher, D. A. and L. W. Johnson, 1981. Applied Discrete Choice Modeling, John Wiley, New York.
5. Microsoft Corporation, 1983. Microsoft FORTRAN, Reference Manual and User's Guide, Bellevue, Washington.
6. Monro, D. M., 1982. FORTRAN 77, Edward Arnold, London.
7. Moshman, J., 1967. "Random number generation," in Wilf, H.S., Mathematical Methods for Digital Computers, John Wiley & Sons, Inc., New York.
8. Small, K. A. and H. S. Rosen, 1981. "Applied Welfare Economics with Discrete Choice Models," Econometrica, vol. 49, no. 1, pp. 105-130.
9. Varian, H. R., 1978. Microeconomic Analysis, W. W. Norton and Co., N.Y.

10. Williams, H.C.W.L., 1977. "On the formation of travel demand models and economic evaluation measures of user benefit," Environment and Planning A, vol. 9, pp. 285-344.

Appendix A

RUMS Program Listing

Appendix A

RUMS Program Listing

Page 1
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
1 C*****
2 C
3 C
4 C RUMS IS A PROGRAM FOR CALCULATING CONSUMER SURPLUS CHANGE
5 C AND PREDICTING MARKET SHARE CHANGES USING MULTINOMIAL LOGIT
6 C AND HEDONIC DEMAND MODELS.
7 C CREATED BY D L GREENE ORNL 6-09-1986
8 C
9 C
10 C*****
11 C
12 C
13 C
14 C PROGRAM RUMS
15 C REAL*8 B(15),SAL1(200),SAL2(200),A1(200),A2(200),BLN(15),
16 C 1 RAN(16),CONSUR,E(15),SGN(15),X1(200,10),X2(200,10)
17 C CHARACTER*2 IDSK
18 C OPEN DATA FILES FOR PARAMETERS AND CHARACTERISTICS
19 C
20 C
21 C WRITE (*,5)
22 C 5 FORMAT(1H0,'PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS')
23 C WRITE (*,6)
24 C 6 FORMAT(1H)
25 C OPEN(11,FILE=' ')
26 C WRITE (*,6)
27 C WRITE (*,7)
28 C 7 FORMAT(1H0,'PLEASE ENTER FILENAME FOR CHARACTERISTICS')
29 C OPEN(12,FILE=' ')
30 C
31 C
32 C DEFAULTS STATUS=OLD ACCESS=SEQUENTIAL FORM=FORMATTED
33 C
34 C PROGRAM SETUP SUBROUTINE MNL OR HDM
35 C CALL SETUP (MODEL,M1,M2,N,IPRE)
36 C
37 C READ PARAMETERS
38 C IF (MODEL .EQ. 1) CALL PAR1 (N,B)
39 C IF (MODEL .EQ. 2) CALL PAR2 (N,B,E,SGN)
40 C
41 C READ CHOICE SET CHARACTERISTICS
42 C CALL CHOICE (M1,M2,N,X1,X2,SAL1,SAL2)
43 C
44 C CALIBRATE SHARE WEIGHTS OR UTILITY FUNCTION CONSTANTS
45 C IF (IPRE .EQ. 1) CALL WEIGHTS (M1,M2,SAL1,SAL2,A1,A2)
46 C IF (IPRE .EQ. 2) CALL CALIB (M1,N,B,E,X1,X2,SAL1,SAL2,A1,SGN,
47 C 1 MODEL,M2,IPRE)
48 C IF (IPRE .EQ. 3) CALL CALIB (M1,N,B,E,X1,X2,SAL1,SAL2,A1,SGN,
49 C 1 MODEL,M2,IPRE)
50 C IF (IPRE .EQ. 3) CALL EQL (M1,A1,A2)
51 C IF (IPRE .EQ. 2) GOTO 99
52 C
53 C CALCULATE CONSUMER SURPLUS CHANGE
54 C IF (MODEL .EQ. 1) CALL SURPLS (M1,M2,N,B,X1,X2,CONSUR,A1,A2)
55 C IF (MODEL .EQ. 2) CALL HDMSUR (M1,M2,N,B,E,X1,X2,CONSUR,SGN,A1,A2)
56 99 CONTINUE

Page 2
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

```

57 C
58 C OUTPUT RESULTS
59     IF (IPRE .EQ. 1) CALL SURPRN (M1,M2,N,MODEL,CONSUR)
60     IF (IPRE .EQ. 2) CALL PREPRN (MODEL,M1,SAL1,SAL2,M2)
61     IF (IPRE .EQ. 3) CALL SURPRN (M1,M2,N,MODEL,CONSUR)
62 C
63     END

```

| Name | Type | Offset | P Class |
|--------|-----------|--------|---------|
| A1 | REAL*8 | 35824 | |
| A2 | REAL*8 | 37424 | |
| B | REAL*8 | 16 | |
| BLN | REAL*8 | 35456 | |
| CONSUR | REAL*8 | 39154 | |
| E | REAL*8 | 35704 | |
| IDSK | CHAR*2 | ***** | |
| IPRE | INTEGER*4 | 39150 | |
| M1 | INTEGER*4 | 39138 | |
| M2 | INTEGER*4 | 39142 | |
| MODEL | INTEGER*4 | 39134 | |
| N | INTEGER*4 | 39146 | |
| RAN | REAL*8 | 35576 | |
| SAL1 | REAL*8 | 136 | |
| SAL2 | REAL*8 | 1736 | |
| SGN | REAL*8 | 3336 | |
| X1 | REAL*8 | 3456 | |
| X2 | REAL*8 | 19456 | |

```

A1      REAL*8      35824
A2      REAL*8      37424
B       REAL*8      16
BLN     REAL*8      35456
CONSUR  REAL*8      39154
E       REAL*8      35704
IDSK    CHAR*2      *****
IPRE    INTEGER*4    39150
M1      INTEGER*4    39138
M2      INTEGER*4    39142
MODEL   INTEGER*4    39134
N       INTEGER*4    39146
RAN     REAL*8      35576
SAL1    REAL*8      136
SAL2    REAL*8      1736
SGN     REAL*8      3336
X1      REAL*8      3456
X2      REAL*8      19456

64 C
65 C
66 C*****
67 C
68 C      SUBROUTINE SETUP (MODEL, M1, M2, N, IPRE)
69 C
70 C      > OBTAIN PROBLEM DESCRIPTION FROM USER
71 C
72 C      M1: NUMBER OF OBSERVATIONS IN FIRST CHOICE SET
73 C      M2: NUMBER OF OBSERVATIONS IN SECOND CHOICE SET
74 C      N: NUMBER OF ATTRIBUTES
75 C      IPRE: INDICATOR FOR TYPE OF CALCULATION
76 C      MODEL: INDICATOR FOR TYPE OF MODEL
77 C
78 C*****
79 C
80      SUBROUTINE SETUP (MODEL,M1,M2,N,IPRE)
81 C
82 C      READ TYPE OF MODEL FROM KEYBOARD
83      WRITE (*,10)
84 10      FORMAT(1H )
85      WRITE (*,12)
86 12      FORMAT(1HO,'ESTIMATION OF CONSUMER SURPLUS IN RUMS')
87      WRITE (*,14)
88 14      FORMAT(1HO,'WHAT TYPE OF MODEL? ENTER: ')
89      WRITE (*,16)

```

Page 3
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 90 16 FORMAT(1HO,' 1 FOR MULTINOMIAL LOGIT')
 91 WRITE (*,18)
 92 18 FORMAT(1HO,' 2 FOR HEDONIC DEMAND MODEL')
 93 READ (*,52) MODEL
 94 52 FORMAT (I1)
 95 WRITE (*,20) MODEL
 96 20 FORMAT(1HO,'YOU CHOSE MODEL ',I1,'.')
 97 WRITE (*,100)
 98 100 FORMAT(1HO,'WHAT TYPE OF ESTIMATION? ENTER 1')
 99 WRITE (*,110)
 100 110 FORMAT(1HO,' 1 FOR CONSUMER SURPLUS CHANGE')
 101 WRITE (*,120)
 102 120 FORMAT(1HO,' 2 FOR SHARES PREDICTION')
 103 WRITE (*,130)
 104 130 FORMAT(1HO,' 3 FOR C S CHANGE, CORRESPONDING SET MEMBERS')
 105 READ (*,52) IPRE
 106 IF (IPRE .EQ. 3) WRITE (*,140)
 107 140 FORMAT(1HO,'FOR OPTION 3 SETS NUMBER AND ORDER MUST AGREE')
 108 C
 109 C READ NUMBER OF CHOICES AND NUMBER OF CHARACTERISTICS
 110 WRITE (*,22)
 111 22 FORMAT(1HO,'ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -')
 112 READ (*,54) M1
 113 54 FORMAT(I3)
 114 WRITE (*,23)
 115 23 FORMAT(1HO,'ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -')
 116 READ (*,54) M2
 117 WRITE (*,24)
 118 24 FORMAT(1HO,'ENTER NUMBER OF CHARACTERISTICS -')
 119 READ (*,56) N
 120 56 FORMAT(I2)
 121 WRITE (*,26) M1,M2,N
 122 26 FORMAT(1HO,'THERE ARE ',I3,' & ',I3,' CHOICES & ',I2,' CHARS.')
 123 IF ((IPRE .EQ. 3) .AND. (M1 .NE. M2)) WRITE (*,200)
 124 200 FORMAT(1HO,'ERROR M1 NE M2: CHOICE SETS DO NOT CORRESPOND')
 125 C
 126 END

| Name | Type | Offset | P | Class |
|-------|-----------|--------|---|-------|
| IPRE | INTEGER*4 | 16 | * | |
| M1 | INTEGER*4 | 4 | * | |
| M2 | INTEGER*4 | 8 | * | |
| MODEL | INTEGER*4 | 0 | * | |
| N | INTEGER*4 | 12 | * | |

127 C
 128 C
 129 ****
 130 C
 131 C SUBROUTINE PAR1 (N, B)
 132 C
 133 C > READ MNL PARAMETERS
 134 C
 135 C B: ATTRIBUTE COEFFICIENTS

Page 4
 06-10-86
 14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 136 C N: NUMBER OF ATTRIBUTES
 137 C
 138 C*****
 139 SUBROUTINE PAR1 (N, B)
 140 C READ MNL MODEL PARAMETERS
 141 REAL*8 B(N)
 142 CHARACTER*25 AFMT
 143 WRITE (*,100)
 144 100 FORMAT(1HO,' READING MNL MODEL PARAMETERS . . .')
 145 WRITE (*,99)
 146 99 FORMAT(1HO,'ENTER RECORD FORMAT FOR PARAMS.DAT.')
 147 READ (*,9) AFMT
 148 9 FORMAT(A25)
 149 READ (11,AFMT) (B(I),I=1,N)
 150 WRITE (*,105)
 151 105 FORMAT(1HO,'ENTER 1 TO PRINT PARAMETERS')
 152 READ (*,107) IPRN
 153 107 FORMAT(I1)
 154 IF (IPRN .EQ. 1) WRITE (*,111) (B(I),I=1,N)
 155 111 FORMAT(1X,E15.9)
 156 RETURN
 157 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-------|
| AFMT | CHAR*25 | 39964 | | |
| B | REAL*8 | 4 | * | |
| I | INTEGER*4 | 39996 | | |
| IPRN | INTEGER*4 | 40040 | | |
| N | INTEGER*4 | 0 | * | |

158 C
 159 C
 160 C*****
 161 C
 162 C SUBROUTINE PAR2 (N, B, E, SGN)
 163 C
 164 C > READ HDM PARAMETERS
 165 C
 166 C B: ATTRIBUTE COEFFICIENT
 167 C E: STANDARD DEVIATION
 168 C SGN: SIGN OF THE PARAMETER VALUE
 169 C
 170 C*****
 171 C
 172 SUBROUTINE PAR2 (N,B,E,SGN)
 173 REAL*8 B(N),E(N),SGN(N)
 174 CHARACTER*25 AFMT
 175 C READ HDM PARAMETERS
 176 WRITE (*,100)
 177 100 FORMAT(1HO,' READING HDM MODEL PARAMETERS . . .')
 178 WRITE (*,99)
 179 99 FORMAT(1HO,'ENTER RECORD FORMAT FOR PARAMS.DAT.')
 180 READ (*,9) AFMT
 181 9 FORMAT(A25)

Page 5
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 182 READ (11,AFMT) (B(I),E(I),SGN(I),I=1,N)
 183 WRITE (*,110)
 184 110 FORMAT(1HO,'ENTER 1 TO PRINT PARAMETERS')
 185 READ (*,112) IPRN
 186 112 FORMAT(I1)
 187 IF (IPRN .EQ. 1) WRITE (*,114) (B(I),E(I),SGN(I),I=1,N)
 188 114 FORMAT(1X,3E15.9)
 189 RETURN
 190 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-------|
| AFMT | CHAR*25 | 40148 | | |
| B | REAL*8 | 4 * | | |
| E | REAL*8 | 8 * | | |
| I | INTEGER*4 | 40180 | | |
| IPRN | INTEGER*4 | 40224 | | |
| N | INTEGER*4 | 0 * | | |
| SGN | REAL*8 | 12 * | | |

191 C
 192 ****=
 193 C
 194 C SUBROUTINE CHOICE (M1, M2, N, X1, X2, SAL1, SAL2)
 195 C
 196 C > READ CHARACTERISTICS FOR BOTH CHOICE SETS
 197 C
 198 C M1: NUMBERS IN BASE CHOICE SET
 199 C M2: NUMBERS IN NEW CHOICE SET
 200 C X1: CAR CHARACTERISTICS IN BASE YEAR
 201 C X2: CAR CHARACTERISTICS IN NEW YEAR
 202 C SAL1: SALES IN BASE YEAR
 203 C SAL2: SALES IN NEW YEAR
 204 C IPRN: INDICATOR FOR PRINTING CHARACTERISTICS DATA
 205 C
 206 ****=
 207 C
 208 C
 209 C SUBROUTINE CHOICE (M1,M2,N,X1,X2,SAL1,SAL2)
 210 C READ CHOICE CHARACTERISTICS, NEW AND BASE
 211 C CHARACTER*25 AFMT,BFMT
 212 C REAL*8 SAL1(M1),SAL2(M2),X1(M1,N),X2(M2,N)
 213 C READ BASE RECORDS, FIRST M1
 214 C WRITE (*,200)
 215 200 FORMAT(1HO,'READING CHARACTERISTICS & SALES DATA')
 216 C WRITE (*,99)
 217 99 FORMAT(1HO,'ENTER RECORD FORMAT FOR CHARS.DAT.')
 218 C READ (*,9) AFMT
 219 9 FORMAT(A25)
 220 C WRITE (*,105)
 221 105 FORMAT(1HO,'ENTER 1 TO PRINT CHARACTERISTICS DATA')
 222 C READ (*,107) IPRN
 223 107 FORMAT(I1)
 224 C IF (IPRN .EQ. 1) WRITE (*,109)
 225 109 FORMAT(1HO,'ENTER OUTPUT FORMAT, E.G. 1X,INPUT FORMAT')

Page 6
06-10-86
14:58:29

```
D Line# 1      7                               Microsoft FORTRAN77 V3.31 August 1985
226      IF (IPRN .EQ. 1) READ (*,9) BFMT
227      DO 20 I=1,M1
1 228      READ (12,AFMT)  (X1(I,J),J=1,N),SAL1(I)
1 229      IF (IPRN .EQ. 1) WRITE(*,BFMT) (X1(I,J),J=1,N),SAL1(I)
1 230 20    CONTINUE
231 C
232 C  READ NEW RECORDS M1+1 TO M1+M2
233      DO 40 I=1,M2
1 234      READ (12,AFMT)  (X2(I,J),J=1,N),SAL2(I)
1 235      IF (IPRN .EQ. 1) WRITE (*,BFMT) (X2(I,J),J=1,N),SAL2(I)
1 236 40    CONTINUE
237 C
238      END

Name      Type      Offset P Class
AFMT      CHAR*25      40331
BFMT      CHAR*25      40466
I         INTEGER*4     40492
IPRN      INTEGER*4     40408
J         INTEGER*4     40500
M1        INTEGER*4     0 *
M2        INTEGER*4     4 *
N         INTEGER*4     8 *
SAL1      REAL*8       20 *
SAL2      REAL*8       24 *
X1        REAL*8       12 *
X2        REAL*8       16 *

239 C
240 C
241 C
242 C  CALIBRATION SUBROUTINES
243 C
244 ****
245 C
246 C      SUBROUTINE WEIGHTS (M1, M2, SAL1, SAL2, A1, A2)
247 C
248 C      > COMPUTE SALES WEIGHTS FOR CONSUMER SURPLUS CALCULATION
249 C      WHEN SETS 1 AND 2 DO NOT HAVE CORRESPONDING MEMBERSHIPS
250 C
251 C      A1: UTILITY FUNCTION INTERCEPTS FOR CHOICE SET 1
252 C      A2: UTILITY FUNCTION INTERCEPTS FOR CHOICE SET 2
253 C
254 C      CALL SUBROUTINE SHRS (M1, SAL1, A1)
255 C      CALL SUBROUTINE SHRS (M1, SAL2, A2)
256 C
257 ****
258 C
259      SUBROUTINE WEIGHTS (M1,M2,SAL1,SAL2,A1,A2)
260      REAL*B SAL1(M1),SAL2(M2),A1(M1),A2(M2)
261 C
262      WRITE (*,100)
263 100   FORMAT(1HO,'WHAT TYPE OF WEIGHTING FOR LOGSUM TERMS? ENTER: ')
264      WRITE (*,110)
```

Page 7
 06-10-86
 14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 265 110 FORMAT(1HO,' 1 FOR SHARES')
 266 WRITE (*,120)
 267 120 FORMAT(1HO,' 2 FOR NO WEIGHTS')
 268 READ (*,200) IWT
 269 200 FORMAT(I1)
 270 C
 271 DO 10 I=1,M1
 1 272 A1(I)=0.0
 1 273 10 CONTINUE
 274 DO 20 I=1,M2
 1 275 A2(I)=0.0
 1 276 20 CONTINUE
 277 C
 278 IF (IWT .EQ. 1) CALL SHRS (M1,SAL1,A1)
 279 IF (IWT .EQ. 1) CALL SHRS (M2,SAL2,A2)
 280 C
 281 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-------|
| A1 | REAL*8 | 16 | * | |
| A2 | REAL*8 | 20 | * | |
| I | INTEGER*4 | 40684 | | |
| IWT | INTEGER*4 | 40620 | | |
| M1 | INTEGER*4 | 0 | * | |
| M2 | INTEGER*4 | 4 | * | |
| SAL1 | REAL*8 | 8 | * | |
| SAL2 | REAL*8 | 12 | * | |

282 C
 283 C
 284 ****
 285 C
 286 C SUBROUTINE CALIB (M1,N,B,E,X1,X2,SAL1,SAL2,A1,SGN,MODEL,M2,IPRE)
 287 C
 288 C > COMPUTE CONSTANT TERMS OF UTILITY FUNCTION WHEN:
 289 C 1. PREDICTING SHARES
 290 C 2. CHOICE SETS DON'T HAVE CORRESPONDING MEMBERSHIPS
 291 C
 292 C CALL SHRS (M1, SAL1, A1)
 293 C CALL BSUM1(M1, X1, B, N, BS1)
 294 C CALL BSUM1(M2, X2, B, N, BS2)
 295 C CALL BSUM2(M1, X1, B, E, N, BS1, SGN)
 296 C CALL PRED1(M2, A1, BS2, SAL2)
 297 C CALL PRED2(M2, A1, N, B, E, SGN, X2, BS2, SAL2)
 298 C
 299 ****
 300 C
 301 C
 302 C SUBROUTINE CALIB (M1,N,B,E,X1,X2,SAL1,SAL2,A1,SGN,MODEL,M2,IPRE)
 303 C CALIBRATE UTILITY CONSTANTS FOR MNL AND HDM MODELS
 304 C
 305 REAL*8 SAL1(M1), SAL2(M2), BS1(200), BS2(200), A1(M1), B(N),
 306 1 E(N), SGN(N), X1(M1,N), X2(M2,N)
 307 C

Page 8
06-10-86
14:58:29

```
D Line# 1      7                               Microsoft FORTRAN77 V3.31 August 1985
308     CALL SHRS (M1,SAL1,A1)
309 C
310     IF (MODEL .EQ. 1) CALL BSUM1 (M1,X1,B,N,BS1)
311     IF (MODEL .EQ. 1) CALL BSUM1 (M2,X2,B,N,BS2)
312 C
313     IF (MODEL .EQ. 2) CALL BSUM2 (M1,X1,B,E,N,BS1,SGN)
314 C
315     CALL INIT (M1,BS1,SAL1,A1)
316 C
317     IF (IPRE .EQ. 3) GOTO 99
318     IF (MODEL .EQ. 1) CALL PRED1      (M2,A1,BS2,SAL2)
319     IF (MODEL .EQ. 2) CALL PRED2 (M2,A1,N,B,E,SGN,X2,BS2,SAL2)
320 99    CONTINUE
321 C
322     END
```

| Name | Type | Offset | P | Class |
|------|------|--------|---|-------|
|------|------|--------|---|-------|

| | | | |
|-------|-----------|-------|---|
| A1 | REAL*8 | 32 | * |
| B | REAL*8 | 8 | * |
| BS1 | REAL*8 | 40696 | |
| BS2 | REAL*8 | 42296 | |
| E | REAL*8 | 12 | * |
| IPRE | INTEGER*4 | 48 | * |
| M1 | INTEGER*4 | 0 | * |
| M2 | INTEGER*4 | 44 | * |
| MODEL | INTEGER*4 | 40 | * |
| N | INTEGER*4 | 4 | * |
| SAL1 | REAL*8 | 24 | * |
| SAL2 | REAL*8 | 28 | * |
| SGN | REAL*8 | 36 | * |
| X1 | REAL*8 | 16 | * |
| X2 | REAL*8 | 20 | * |

```
323 C
324 C*****
325 C
326 C      SUBROUTINE SHRS (M, SHR, A)
327 C
328 C      > COMPUTE SALES SHARES FROM SALES DATA
329 C
330 C      SHR: SALES SHARES (FRACTION OF TOTAL)
331 C
332 C      CALL SUM (M, S, SHR)
333 C
334 C*****
335 C
336 C      SUBROUTINE SHRS (M, SHR, A)
337 C      RETURNS SHARES IN PLACE OF SALES
338 C
339 C      REAL*8 S, SHR(M), A(M)
340 C
341 C      CALL SUM (M, S, SHR)
342 C
343 C
```

Page 9
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 344 DO 10 I=1,M
 1 345 SHR(I)=SHR(I)/S
 1 346 A(I)=DLOG(SHR(I))
 1 347 10 CONTINUE
 348 C
 349 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-----------|
| A | REAL*8 | | 8 | * |
| DLOG | | | | INTRINSIC |
| I | INTEGER*4 | 43904 | | |
| M | INTEGER*4 | | 0 | * |
| S | REAL*8 | 43896 | | |
| SHR | REAL*8 | | 4 | * |

350 C
 351 C
 352 C*****
 353 C
 354 C SUBROUTINE SUM (NN, SS, XX)
 355 C
 356 C > COMPUTE THE SUM OF AN ARRAY
 357 C
 358 C NN: SIZE OF ARRAY
 359 C XX: ARRAY TO BE SUMMED
 360 C SS: SUM
 361 C
 362 C*****
 363 C
 364 C SUBROUTINE SUM (NN,SS,XX)
 365 C
 366 C REAL*8 SS,XX(NN)
 367 C
 368 C INITIALIZE
 369 C SS=0
 370 C DO 10 I=1,NN
 1 371 C SS=SS+XX(I)
 1 372 10 CONTINUE
 373 C
 374 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-------|
| I | INTEGER*4 | 43912 | | |
| NN | INTEGER*4 | | 0 | * |
| SS | REAL*8 | | 4 | * |
| XX | REAL*8 | | 8 | * |

375 C
 376 C
 377 C*****
 378 C
 379 C SUBROUTINE BSUM1 (M, X, B, N, BS)

Page 10
06-10-86
14:58:29

```
D Line# 1      7
380 C
381 C      > COMPUTE UTILITIES OF ALTERNATIVES FOR MNL MODEL
382 C
383 C      BS= UTILITY VALUE = SUM OF COEFFS*ATTRIBUTES
384 C
385 C*****SUBROUTINE BSUM1 (M,X,B,N,BS)
386 C*****SUBROUTINE BSUM1 (M,X,B,N,BS)
387      SUBROUTINE BSUM1 (M,X,B,N,BS)
388 C
389      REAL*B BS(M),B(N),X(M,N)
390 C
391      DO 10 I=1,M
1 392      BS(I)=0
1 393      DO 20 J=1,N
2 394      BS(I)=BS(I)+(B(J)*X(I,J))
2 395 20      CONTINUE
1 396 10      CONTINUE
397 C
398      END
```

| Name | Type | Offset | P | Class |
|------|-----------|--------|----|-------|
| B | REAL*B | | 8 | * |
| BS | REAL*B | | 16 | * |
| I | INTEGER*4 | 43920 | | |
| J | INTEGER*4 | 43928 | | |
| M | INTEGER*4 | | 0 | * |
| N | INTEGER*4 | | 12 | * |
| X | REAL*B | | 4 | * |

```
399 C
400 C
401 C*****SUBROUTINE BSUM2 (M, X, B, E, N, BS, SGN)
402 C*****SUBROUTINE BSUM2 (M, X, B, E, N, BS, SGN)
403 C      SUBROUTINE BSUM2 (M, X, B, E, N, BS, SGN)
404 C
405 C      > COMPUTE UTILITIES OF ALTERNATIVES FOR HDM MODEL
406 C
407 C*****SUBROUTINE BSUM2 (M, X, B, E, N, BS, SGN)
408 C*****SUBROUTINE BSUM2 (M, X, B, E, N, BS, SGN)
409      SUBROUTINE BSUM2 (M,X,B,E,N,BS,SGN)
410 C
411      REAL*B BS(M),B(N),E(N),SGN(N),X(M,N)
412 C
413      DO 10 I=1,M
1 414      BS(I)=0
1 415      DO 20 J=1,N
2 416      BS(I)=BS(I)+SGN(J)*DEXP(B(J)+0.5*E(J)**2)*X(I,J)
2 417 20      CONTINUE
1 418 10      CONTINUE
419 C
420      END
```

| Name | Type | Offset | P | Class |
|------|------|--------|---|-------|
|------|------|--------|---|-------|

Page 11
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

| | | |
|------|-----------|-----------|
| B | REAL*8 | 8 * |
| BS | REAL*8 | 20 * |
| DEXP | | INTRINSIC |
| E | REAL*8 | 12 * |
| I | INTEGER*4 | 43936 |
| J | INTEGER*4 | 43944 |
| M | INTEGER*4 | 0 * |
| N | INTEGER*4 | 16 * |
| SGN | REAL*8 | 24 * |
| X | REAL*8 | 4 * |

```

421 C
422 C*****SUBROUTINE INIT(B,M,SAL,A)
423 C
424 C      SUBROUTINE INIT (B, M, SAL, A)
425 C
426 C      > COMPUTE INTERCEPTS OF UTILITY FUNCTIONS USING KNOWN SHARES
427 C
428 C*****END SUBROUTINE INIT
429 C
430      SUBROUTINE INIT (M,B,SAL,A)
431 C
432      REAL*8 A(M),SAL(M),B(M)
433 C
434      A(1)=-B(1)
435      DO 10 I=2,M
1 436      IF ((SAL(I) .LE. 0) .OR. (SAL(I) .LE. 0)) CALL SERR (M,B,SAL,I)
1 437      A(I)=DLOG(SAL(I))-DLOG(SAL(1))-B(I)
1 438 10  CONTINUE
439 C
440      END

```

| Name | Type | Offset P Class |
|------|-----------|----------------|
| A | REAL*8 | 12 * |
| B | REAL*8 | 4 * |
| DLOG | | INTRINSIC |
| I | INTEGER*4 | 43952 |
| M | INTEGER*4 | 0 * |
| SAL | REAL*8 | 8 * |

```

441 C
442 C
443 C*****SUBROUTINE EQL (M,A1,A2)
444 C
445 C      SUBROUTINE EQL (M,A1,A2)
446 C
447 C      > EQUATES ONE VECTOR TO ANOTHER
448 C
449 C*****END SUBROUTINE EQL
450 C
451      SUBROUTINE EQL (M,A1,A2)
452 C
453      REAL*8 A1(M),A2(M)

```

Page 12
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 454 DO 10 I=1,M
 1 455 A2(I)=A1(I)
 1 456 10 CONTINUE
 457 C
 458 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-------|
| A1 | REAL*8 | | 4 | * |
| A2 | REAL*8 | | 8 | \$ |
| I | INTEGER*4 | 43960 | | |
| M | INTEGER*4 | 0 | | * |

```

459 C
460 C
461 ****
462 C
463 C      SUBROUTINE SURPLS (M1,M2,N,B,X1,X2,CONSUR,A1,A2)
464 C
465 C      > CALCULATE CONSUMER SURPLUS CHANGE FOR MNL
466 C
467 C      CONSUR: CONSUMER'S SURPLUS CHANGE
468 C
469 C          CALL ACCUM (M1, N, B, X1, BASE, A1)
470 C          CALL ACCUM (M2, N, B, X2, ANEW, A2)
471 C          CALL AERR (ANEW, BASE)
472 C
473 ****
474 C
475 C
476      SUBROUTINE SURPLS (M1,M2,N,B,X1,X2,CONSUR,A1,A2)
477 C
478      REAL*8 ANEW,BASE,A1(M1),A2(M2),B(N),CONSUR,X1(M1,N),X2(M2,N)
479 C
480 C      COMPUTE DENOMINATOR
481      CALL ACCUM (M1,N,B,X1,BASE,A1)
482 C
483 C      COMPUTE NUMERATOR
484      CALL ACCUM (M2,N,B,X2,ANEW,A2)
485 C
486 C      COMPUTE CONSUMER SURPLUS CHANGE
487 C      B(1) MUST BE PRICE COEFFICIENT
488      IF ((ANEW .LE. 0) .OR. (BASE .LE. 0)) CALL AERR (ANEW,BASE)
489      CONSUR=(DLOG(ANEW)-DLOG(BASE))/(-B(1))
490 C
491 END

```

| Name | Type | Offset | P | Class |
|--------|--------|--------|---|-------|
| A1 | REAL*8 | 28 | * | |
| A2 | REAL*8 | 32 | * | |
| ANEW | REAL*8 | 43976 | | |
| B | REAL*8 | 12 | * | |
| BASE | REAL*8 | 43968 | | |
| CONSUR | REAL*8 | 24 | * | |

Page 13
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

DLOG INTRINSIC

| | | |
|----|-----------|------|
| M1 | INTEGER*4 | 0 * |
| M2 | INTEGER*4 | 4 * |
| N | INTEGER*4 | 8 * |
| X1 | REAL*8 | 16 * |
| X2 | REAL*8 | 20 * |

```

492 C
493 ****
494 C
495 C      SUBROUTINE ACCUM (M, N, B, X, ACC, A)
496 C
497 C      > COMPUTE SUMS OF EXPONENTIATED UTILITY
498 C
499 C      ACC: SUM OF EXPONENTIATED UTILITY
500 C
501 ****
502 C
503 C
504 C      SUBROUTINE ACCUM (M,N,B,X,ACC,A)
505 C      COMPUTE SUMS OF EXPONENTIATED COMPOSITE COSTS
506 C      REAL*8 BSUM,ACC,A(M),B(N),X(M,N)
507 C
508 C      INITIALIZE SUM OF EXPONENTIALS
509 C      ACC=0.0
510 C      COMPUTE SUM
511 C      DO 20 I=1,M
1 512 C      INITIALIZE COMPOSITE PRICE SUM
1 513 C      BSUM=A(I)
1 514 C      COMPUTE COMPOSITE PRICE
1 515 C      DO 10 J=1,N
2 516 C      BSUM=BSUM+(B(J)**X(I,J))
2 517 10  C      CONTINUE
1 518 C      ACC=ACC+DEXP (BSUM)
1 519 20  C      CONTINUE
520 C
521 END

```

| Name | Type | Offset P Class |
|------|-----------|----------------|
| A | REAL*8 | 20 * |
| ACC | REAL*8 | 16 * |
| B | REAL*8 | 8 * |
| BSUM | REAL*8 | 43992 |
| DEXP | | INTRINSIC |
| I | INTEGER*4 | 43984 |
| J | INTEGER*4 | 44000 |
| M | INTEGER*4 | 0 * |
| N | INTEGER*4 | 4 * |
| X | REAL*8 | 12 * |

```

522 ****
523 C
524 C      SUBROUTINE HDMSUR (M1, M2, N, B, E, X1, X2, CONSUR, SGN, A1,A2)

```

Page 14
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

```

525 C
526 C      > CALCULATE CONSUMER'S SURPLUS CHANGE IN HDM
527 C
528 C      CALL RANSET (ITER, K, NEW1, N)
529 C      CALL RANDCO (N, B, E, BLN, K, NEW1, SGN)
530 C      CALL SURPLS (M1, M2, N, BLN, X1, X2, CON, A1, A2)
531 C
532 C*****SUBROUTINE HDMSUR (M1,M2,N,B,E,X1,X2,CONSUR,SGN,A1,A2)
533 C
534 C      SUBROUTINE HDMSUR (M1,M2,N,B,E,X1,X2,CONSUR,SGN,A1,A2)
535 C
536 C      INTEGER*4 NEW1
537 C      INTEGER*2 K
538 C      REAL*8 A1(M1),A2(M2),B(N),BLN(16),CON,CONSUR,E(N),SGN(N),
539 C      1 X1(M1,N),X2(M2,N)
540 C
541 C      CALCULATE CONSUMER SURPLUS IN HDM
542 C
543 C      CALL RANSET (ITER,K,NEW1,N)
544 C      CONSUR=0.0
545 C      DO 10 I=1,ITER
1 546 C
1 547 C      CALL RANDCO (N,B,E,BLN,K,NEW1,SGN)
1 548 C      CALL SURPLS (M1,M2,N,BLN,X1,X2,CON,A1,A2)
1 549 C      CONSUR=CONSUR+(CON/ITER)
1 550 10 C      CONTINUE
551 C
552 C      END

```

| Name | Type | Offset | P | Class |
|--------|-----------|--------|---|-------|
| A1 | REAL*8 | 36 | * | |
| A2 | REAL*8 | 40 | * | |
| B | REAL*8 | 12 | * | |
| BLN | REAL*8 | 44008 | | |
| CON | REAL*8 | 44154 | | |
| CONSUR | REAL*8 | 28 | * | |
| E | REAL*8 | 16 | * | |
| I | INTEGER*4 | 44146 | | |
| ITER | INTEGER*4 | 44136 | | |
| K | INTEGER*2 | 44140 | | |
| M1 | INTEGER*4 | 0 | * | |
| M2 | INTEGER*4 | 4 | * | |
| N | INTEGER*4 | 8 | * | |
| NEW1 | INTEGER*4 | 44142 | | |
| SGN | REAL*8 | 32 | * | |
| X1 | REAL*8 | 20 | * | |
| X2 | REAL*8 | 24 | * | |

```

553 C
554 C*****SUBROUTINE RANSET (ITER, K, NEW1, N)
555 C
556 C      SUBROUTINE RANSET (ITER, K, NEW1, N)
557 C      > OBTAIN PARAMETERS OF MONTE CARLO INTEGRATION

```

Page 15
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

```

559 C
560 C      ITER: NUMBER OF ITERATIONS
561 C      K: NUMBER OF PAIRS OF RANDOM VARIABLES
562 C      NEW1: RANDOM NUMBER SEED
563 C      N: NUMBER OF ATTRIBUTES
564 C
565 C*****SUBROUTINE RANSET (ITER,K,NEW1,N)
566 C
567      SUBROUTINE RANSET (ITER,K,NEW1,N)
568      INTEGER*4 ISEED,NEW1
569      INTEGER*2 K
570 C
571 C  OBTAIN DESIRED NUMBER OF ITERATIONS
572      WRITE (*,100)
573 100   FORMAT(1HO,'HOW MANY ITERATIONS FOR HDM MONTE CARLO?')
574      READ (*,110) ITER
575 110   FORMAT(I4)
576 C  MONTE CARLO INTEGRATION OF HDM SURPLUS
577 C
578      K=INT(N/2)
579      KK=N-2*K
580      IF (KK .GT. 0) K=K+1
581 C  OBTAIN SEED FOR RANDOM NUMBER GENERATOR
582      WRITE (*,200)
583 200   FORMAT(1HO,'ENTER A NUMBER FROM 0 TO 46300')
584      READ (*,210) ISEED
585 210   FORMAT(I5)
586      NEW1=ISEED
587 C
588      END

```

| Name | Type | Offset | P | Class |
|-------|-----------|--------|---|-----------|
| INT | | | | INTRINSIC |
| ISEED | INTEGER*4 | 44314 | | |
| ITER | INTEGER*4 | 0 | * | |
| K | INTEGER*2 | 4 | * | |
| KK | INTEGER*4 | 44270 | | |
| N | INTEGER*4 | 12 | * | |
| NEW1 | INTEGER*4 | 8 | * | |

```

589 C*****
590 C
591 C      SUBROUTINE RANDCO (N,B,E,BLN,K,NEW1,SGN)
592 C
593 C      > GENERATE RANDOM COEFFICIENTS
594 C
595 C      BLN: RANDOM COEFFICIENTS
596 C
597 C      CALL NORMAL (NEW1,RAN,K)
598 C
599 C*****
600 C
601 C
602      SUBROUTINE RANDCO (N,B,E,BLN,K,NEW1,SGN)

```

Page 16
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 603 INTEGER*4 NEW1
 604 INTEGER*2 K
 605 REAL*8 BLN(N),RAN(16),B(N),E(N),SGN(N)
 606 C
 607 C CALL SUBROUTINE FOR 2K NORMAL 0,1 RANDOM VARIABLES
 608 CALL NORMAL (NEW1,RAN,K)
 609 C COMPUTE LOG-NORMALLY DISTRIBUTED COEFFICIENTS
 610 DO 10 I=1,N
 1 611 BLN(I)=DEXP(B(I)+RAN(I)*E(I))*SGN(I)
 1 612 10 CONTINUE
 613 RETURN
 614 END

| Name | Type | Offset | P | Class |
|------|-----------|--------|----|-----------|
| B | REAL*8 | | 4 | * |
| BLN | REAL*8 | | 12 | * |
| DEXP | | | | INTRINSIC |
| E | REAL*8 | | 8 | * |
| I | INTEGER*4 | 44450 | | |
| K | INTEGER*2 | 16 | * | |
| N | INTEGER*4 | 0 | * | |
| NEW1 | INTEGER*4 | 20 | * | |
| RAN | REAL*8 | 44322 | | |
| SGN | REAL*8 | 24 | * | |

615 ****
 616 C
 617 C
 618 C SUBROUTINE NORMAL (NEW1, RAN, K)
 619 C
 620 C > GENERATE A VECTOR OF NORMAL RANDOM VARIABLES
 621 C
 622 C CALL RAN1 (SN,SN1,NEW1)
 623 C
 624 C RAN: NORMALLY DISTRIBUTED RANDOM VARIABLES
 625 C SN: FIRST OF PAIR OF NORMAL RANDOM VARIABLES
 626 C SN1: SECOND OF PAIR OF NORMAL RANDOM VARIABLES
 627 C
 628 C SUBROUTINE FOR PAIRS OF INDEPENDENT NORMAL 0,1 VARIATES
 629 C BASED ON P.F. HULTQUIST, PC TECH JOUR., 8/84, AND J MOSHMAN
 630 C RANDOM NUMBER GENERATION, IN H.S. WILF, V.2 MATHEMATICAL METHODS
 631 C FOR DIGITAL COMPUTERS
 632 C
 633 ****
 634 C
 635 SUBROUTINE NORMAL (NEW1,RAN,K)
 636 INTEGER*4 NEW1
 637 INTEGER*2 G,K
 638 REAL*8 SN,SN1,RAN(16)
 639 C
 640 J=1
 641 DO 15 I=1,K
 1 642 CALL RAN1 (SN,SN1,NEW1)
 1 643 RAN(J)=SN1

Page 17
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

```

1 644      RAN(J+1)=SN
1 645      J=J+2
1 646 15   CONTINUE
1 647      END

```

| Name | Type | Offset | P Class |
|------|-----------|--------|---------|
| G | INTEGER*2 | ***** | |
| I | INTEGER*4 | 44462 | |
| J | INTEGER*4 | 44458 | |
| K | INTEGER*2 | B * | |
| NEW1 | INTEGER*4 | O * | |
| RAN | REAL*8 | 4 * | |
| SN | REAL*8 | 44470 | |
| SN1 | REAL*8 | 44478 | |

```

648 C
649 C
650 C*****
651 C
652 C      SUBROUTINE RAN1 (SN,SN1,NEW1)
653 C
654 C      > GENERATE PAIRS OF NORMAL RANDOM NUMBERS
655 C*****
656 C*****
657      SUBROUTINE RAN1 (SN,SN1,NEW1)
658      INTEGER*4 NEW1,NEW,M
659      INTEGER*2 G
660      REAL*8 Z,SN,SN1,UNIF,UNIF1
661 C
662 C      GENERATE UNIFORM RANDOM NUMBERS
663      G=0
664      M=46300
665      NEW=9261*NEW1+3
666      NEW=MOD(NEW,M)
667      UNIF=NEW/46300.0
668 1   CONTINUE
669 C
670 C      TRANSFORM UNIFORM PAIRS TO 0,1 NORMAL PAIRS
671      IF (G-1) 7,6,7
672 7   G=G+1
673      NEW1=NEW
674      UNIF1=UNIF
675      GOTO 1
676      IF (UNIF1 .LE. 0) CALL UERR (NEW1,UNIF1,K)
677 6   Z=DSQRT (-2.0*DLOG(UNIF1))
678      SN1=Z*DCOS(6.28318*UNIF)
679      SN=Z*DSIN(6.28318*UNIF)
680      G=0
681      NEW1=NEW
682      RETURN
683      END

```

| Name | Type | Offset | P Class |
|------|------|--------|---------|
|------|------|--------|---------|

Page 18
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

| | | |
|-------|-----------|-----------|
| DCOS | | INTRINSIC |
| DLOG | | INTRINSIC |
| DSIN | | INTRINSIC |
| DSQRT | | INTRINSIC |
| G | INTEGER*2 | 44486 |
| K | INTEGER*4 | 44512 |
| M | INTEGER*4 | 44488 |
| MOD | | INTRINSIC |
| NEW | INTEGER*4 | 44492 |
| NEW1 | INTEGER*4 | 8 * |
| SN | REAL*8 | 0 * |
| SN1 | REAL*8 | 4 * |
| UNIF | REAL*8 | 44496 |
| UNIF1 | REAL*8 | 44504 |
| Z | REAL*8 | 44516 |

```

684 C
685 C
686 C*****
687 C
688 C      SUBROUTINE PRED1  (M,A,BS,SAL)
689 C
690 C      > PREDICT NEW SHARES FOR MNL MODEL
691 C
692 C*****
693 C
694 C
695 C      SUBROUTINE PRED1      (M,A,BS,SAL)
696 C
697 C      REAL*8 A(M),BS(M),SAL(M),DEN
698 C
699 C      DEN=0.0
700 C      DO 10 I=1,M
1 701 C      DEN=DEXP(A(I)+BS(I))
1 702 10 C      CONTINUE
703 C      DO 20 I=1,M
1 704 C      SAL(I)=DEXP(A(I)+BS(I))/DEN
1 705 20 C      CONTINUE
706 C
707 C      END

```

| Name | Type | Offset | P | Class |
|------|-----------|--------|---|-----------|
| A | REAL*8 | 4 * | | |
| BS | REAL*8 | 8 * | | |
| DEN | REAL*8 | 44524 | | |
| DEXP | | | | INTRINSIC |
| I | INTEGER*4 | 44532 | | |
| M | INTEGER*4 | 0 * | | |
| SAL | REAL*8 | 12 * | | |

```

708 C
709 C*****
710 C

```

Page 19
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 711 C SUBROUTINE PRED2 (M,A,N,B,E,SGN,X,BS2,SAL2)
 712 C
 713 C > PREDICT NEW SHARES FOR HDM MODEL
 714 C
 715 C CALL RANSET (ITER,K,NEW1,N)
 716 C CALL RANDCO (N,B,E,BLN,K,NEW1,SGN)
 717 C CALL ACCUM (M,N,BLN,X,DEN,A)
 718 C CALL BSUM1 (M,X,BLN,N,BS2)
 719 C
 720 C*****
 721 C
 722 C SUBROUTINE PRED2 (M,A,N,B,E,SGN,X,BS2,SAL2)
 723 C
 724 C REAL*8 A(M),B(N),DEN,BS2(M),SAL2(M),BLN(16),CONSUR,PSHR(200),
 725 C E(N),SGN(N),X(M,N)
 726 C INTEGER*4 ISEED,NEW1
 727 C INTEGER*2 K
 728 C
 729 C CALL RANSET (ITER,K,NEW1,N)
 730 C INITIALIZE PREDICTED SHARES
 731 DO 100 I=1,M
 1 732 SAL2(I)=0.0
 1 733 100 CONTINUE
 734 C BEGIN MONTE CARLO ITERATIONS
 735 DO 20 J=1,ITER
 1 736 CALL RANDCO (N,B,E,BLN,K,NEW1,SGN)
 1 737 CALL ACCUM (M,N,BLN,X,DEN,A)
 1 738 CALL BSUM1 (M,X,BLN,N,BS2)
 1 739 DO 10 I=1,M
 2 740 PSHR(I)=DEXP(A(I)+BS2(I))/DEN
 2 741 SAL2(I)=SAL2(I)+(PSHR(I)/ITER)
 2 742 10 CONTINUE
 1 743 20 CONTINUE
 744 C
 745 END

| Name | Type | Offset | P | Class |
|--------|-----------|--------|---|-----------|
| A | REAL*8 | 4 | * | |
| B | REAL*8 | 12 | * | |
| BLN | REAL*8 | 46144 | | |
| BS2 | REAL*8 | 28 | * | |
| CONSUR | REAL*8 | ***** | | |
| DEN | REAL*8 | 46298 | | |
| DEXP | | | | INTRINSIC |
| E | REAL*8 | 16 | * | |
| I | INTEGER*4 | 46282 | | |
| ISEED | INTEGER*4 | ***** | | |
| ITER | INTEGER*4 | 46272 | | |
| J | INTEGER*4 | 46290 | | |
| K | INTEGER*2 | 46276 | | |
| M | INTEGER*4 | 0 | * | |
| N | INTEGER*4 | 8 | * | |
| NEW1 | INTEGER*4 | 46278 | | |
| PSHR | REAL*8 | 44544 | | |
| SAL2 | REAL*8 | 32 | * | |

Page 20
 06-10-86
 14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985
 SGN REAL*8 20 *
 X REAL*8 24 *

```

746 C
747 ****
748 C
749 C      SUBROUTINE SURPRN (M1,M2,N,MODEL,CONSUR)
750 C
751 C      > PRINT RESULTS OF CONSUMER SURPLUS CALCULATION
752 C
753 ****
754 C
755 C
756 C
757      SUBROUTINE SURPRN (M1,M2,N,MODEL,CONSUR)
758 C  PRINT RESULTS OF CONSUMER SURPLUS CALCULATIONS
759      REAL*8 CONSUR
760 C
761      WRITE (*,100)
762 100  FORMAT(1HO,'      CALCULATIONS COMPLETED')
763      IF (MODEL .EQ. 1) WRITE (*,110)
764 110  FORMAT(1HO,'MULTINOMIAL LOGIT MODEL - CONSUMER SURPLUS')
765      IF (MODEL .EQ. 2) WRITE (*,120)
766 120  FORMAT(1HO,'HEDONIC DEMAND MODEL - CONSUMER SURPLUS')
767      WRITE (*,130) M1,M2
768 130  FORMAT(1HO,'BASE CHOICES = ',I3,' NEW CHOICES = ',I3)
769      WRITE (*,140) CONSUR
770 140  FORMAT(1HO,'SURPLUS CHANGE PER CONSUMER = $',E15.9)
771 C
772      END

```

| Name | Type | Offset | P | Class |
|--------|-----------|--------|---|-------|
| CONSUR | REAL*8 | 16 | * | |
| M1 | INTEGER*4 | 0 | * | |
| M2 | INTEGER*4 | 4 | * | |
| MODEL | INTEGER*4 | 12 | * | |
| N | INTEGER*4 | 8 | * | |

```

773 C
774 ****
775 C
776 C      SUBROUTINE PREPRN (MODEL,M1,SAL1,SAL2,M2)
777 C
778 C      > PRINT RESULTS OF SHARES PREDICTION
779 C
780 ****
781 C
782      SUBROUTINE PREPRN (MODEL,M1,SAL1,SAL2,M2)
783 C
784      REAL*8 SAL1(M1),SAL2(M2)
785 C
786      WRITE (*,100)
787 100  FORMAT(1HO,'BASE YEAR AND PREDICTED MARKET SHARES')

```

Page 21
06-10-86
14:58:29

Microsoft FORTRAN77 V3.31 August 1985

```
D Line# 1      7
 788 C
 789      WRITE (*,110)
 790 110  FORMAT(1HO,'          BASE YEAR      PREDICTED')
 791      DO 10 I=1,M1
 792      WRITE (*,200) I,SAL1(I),SAL2(I)
 1 793 10  CONTINUE
 1 794 200  FORMAT(4X,I3,3X,2E15.8)
 795      END
```

| Name | Type | Offset | P | Class |
|-------|-----------|--------|---|-------|
| I | INTEGER*4 | 46664 | | |
| M1 | INTEGER*4 | 4 | * | |
| M2 | INTEGER*4 | 16 | * | |
| MODEL | INTEGER*4 | 0 | * | |
| SAL1 | REAL*8 | 8 | * | |
| SAL2 | REAL*8 | 12 | * | |

```
796 C*****
797 C
798 C      SUBROUTINE UERR (NEW1,UNIF1,K)
799 C*****
800 C*****
801 C
802 C      ERROR CHECKING SUBROUTINES
803 C
804 C
805      SUBROUTINE UERR (NEW1,UNIF1,K)
806      INTEGER*4 NEW1,UNIF1
807      INTEGER*2 K
808      WRITE (*,100) NEW1,UNIF1,K
809 100  FORMAT(1HO,'ERROR IN RAN1.  NEW1=',E15.9,'UNIF1=',E15.9,'K=',I3)
810      END
```

| Name | Type | Offset | P | Class |
|-------|-----------|--------|---|-------|
| K | INTEGER*2 | 8 | * | |
| NEW1 | INTEGER*4 | 0 | * | |
| UNIF1 | INTEGER*4 | 4 | * | |

```
811 C*****
812 C*****
813 C
814 C      SUBROUTINE SERR (M,B,SAL,I)
815 C*****
816 C*****
817 C
818      SUBROUTINE SERR (M,B,SAL,I)
819      REAL*8 B(M),SAL(M)
820      WRITE (*,100) M,SAL(1),SAL(I),I
821 100  FORMAT(1HO,'ERROR IN SUM.  M=',I3,'SAL(1)=',E15.9,'SAL(I)=',E15.9
822 1,'I=',I3)
823      END
```

Page 22
 06-10-86
 14:58:29

D Line# 1 7

Microsoft FORTRAN77 V3.31 August 1985

Name Type Offset P Class

| | | |
|-----|-----------|------|
| B | REAL*8 | 4 * |
| I | INTEGER*4 | 12 * |
| M | INTEGER*4 | 0 * |
| SAL | REAL*8 | 8 * |

```

824 C
825 C
826 ****
827 C
828 C      SUBROUTINE AERR (ANEW,BASE,B,N)
829 C
830 ****
831      SUBROUTINE AERR (ANEW,BASE,B,N)
832      REAL*8 B(N),ANEW,BASE
833      WRITE (*,100) ANEW,BASE
834 100   FORMAT(1HO,'ERROR IN SURPLS. ANEW=',E15.9,'BASE=',E15.9)
835      DO 10 I=1,N
1 836      WRITE (*,200) I,B(I)
1 837 10   CONTINUE
838 200   FORMAT(1HO,'B',I3,' = ',E15.9)
839   END

```

Name Type Offset P Class

| | | |
|------|-----------|-------|
| ANEW | REAL*8 | 0 * |
| B | REAL*8 | 8 * |
| BASE | REAL*8 | 4 * |
| I | INTEGER*4 | 46874 |
| N | INTEGER*4 | 12 * |

840 C

Name Type Size Class

| | | | |
|--------|--|--|------------|
| ACCUM | | | SUBROUTINE |
| AERR | | | SUBROUTINE |
| BSUM1 | | | SUBROUTINE |
| BSUM2 | | | SUBROUTINE |
| CALIB | | | SUBROUTINE |
| CHOICE | | | SUBROUTINE |
| EQL | | | SUBROUTINE |
| HDMSUR | | | SUBROUTINE |
| INIT | | | SUBROUTINE |
| NORMAL | | | SUBROUTINE |
| PAR1 | | | SUBROUTINE |
| PAR2 | | | SUBROUTINE |
| PRED1 | | | SUBROUTINE |
| PRED2 | | | SUBROUTINE |
| PREPRN | | | SUBROUTINE |
| RAN1 | | | SUBROUTINE |
| RANDCO | | | SUBROUTINE |

Page 23
06-10-86
14:58:29

D Line# 1 7 Microsoft FORTRAN77 V3.31 August 1985

| | |
|--------|------------|
| RANSET | SUBROUTINE |
| RUMS | PROGRAM |
| SERR | SUBROUTINE |
| SETUP | SUBROUTINE |
| SHRS | SUBROUTINE |
| SUM | SUBROUTINE |
| SURPLS | SUBROUTINE |
| SURPRN | SUBROUTINE |
| UERR | SUBROUTINE |
| WEIGHT | SUBROUTINE |

Pass One No Errors Detected
840 Source Lines

Appendix B
Sample Model Runs

Appendix B

Sample Model Runs

System configuration. IBM PC with one floppy disk and one hard disk drive. Program RUMS.EXE resides on the hard disk and data are read from drive a::.

The first six runs illustrate the various options for estimating consumer's surplus using multinomial logit and hedonic demand models. The last two illustrate market shares predictions with the two models.

rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS

File name missing or blank - Please enter name

UNIT 11? a:pold.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS

UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

1

YOU CHOSE MODEL 1.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS

1

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING MNL MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.

(f9.6)

ENTER 1 TO PRINT PARAMETERS

1

-.286000000E-03
 -.339000000E+00
 .374000000E-01
 .137000000E+01
 .375000000E+00
 .462000000E+00

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.

(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

1

ENTER OUTPUT FORMAT, E.G. 1X, INPUT FORMAT
(1x,7f7.2)

| | | | | | | |
|---------|------|-------|------|------|------|-------|
| 3390.00 | 3.60 | 17.10 | 4.38 | 3.85 | 2.76 | 22.90 |
| 3930.00 | 5.25 | 11.20 | 5.00 | 3.92 | 3.43 | 18.80 |
| 4190.00 | 5.77 | 17.30 | 5.43 | 4.18 | 3.95 | 17.10 |
| 4630.00 | 5.96 | 17.50 | 5.34 | 4.35 | 4.54 | 20.50 |
| 8560.00 | 6.56 | 18.00 | 5.52 | 4.50 | 4.47 | 5.20 |
| 4700.00 | 5.72 | 13.80 | 5.45 | 4.27 | 3.78 | 15.60 |
| 3390.00 | 2.92 | 17.10 | 4.38 | 3.47 | 2.76 | 24.92 |
| 3930.00 | 3.45 | 11.20 | 4.75 | 3.53 | 3.43 | 21.15 |
| 4190.00 | 4.46 | 17.30 | 5.16 | 3.77 | 3.95 | 15.74 |
| 4630.00 | 4.81 | 17.50 | 5.07 | 3.91 | 4.54 | 17.67 |
| 9560.00 | 5.29 | 18.00 | 5.52 | 4.50 | 4.47 | 5.99 |
| 6700.00 | 4.23 | 13.80 | 5.45 | 4.27 | 3.78 | 14.54 |

WHAT TYPE OF WEIGHTING FOR LOGSUM TERMS? ENTER:

1 FOR SHARES

2 FOR NO WEIGHTS

2

CALCULATIONS COMPLETED

MULTINOMIAL LOGIT MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$-.116255301E+03

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:pold.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

1

YOU CHOSE MODEL 1.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS

1

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING MNL MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.

(f9.6)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

WHAT TYPE OF WEIGHTING FOR LOGSUM TERMS? ENTER:

1 FOR SHARES

2 FOR NO WEIGHTS

1

CALCULATIONS COMPLETED

MULTINOMIAL LOGIT MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$-.292400481E+03

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:pold.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

1

YOU CHOSE MODEL 1.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS

3

FOR OPTION 3 SETS NUMBER AND ORDER MUST AGREE

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING MNL MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.

(f9.6)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

CALCULATIONS COMPLETED

MULTINOMIAL LOGIT MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$.900960068E+01

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:params.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT
2 FOR HEDONIC DEMAND MODEL
2

YOU CHOSE MODEL 2.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE
2 FOR SHARES PREDICTION
3 FOR C S CHANGE, CORRESPONDING SET MEMBERS
1

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING HDM MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.

(3f6.3)

ENTER 1 TO PRINT PARAMETERS

1

-.794000000E+01 .118000000E+01 -.100000000E+01
-.128000000E+01 .100000000E-02 -.100000000E+01
-.410000000E+01 .999000000E+00 .100000000E+01
.569000000E+00 .622000000E+00 .100000000E+01
-.175000000E+01 .134000000E+01 .100000000E+01
-.263000000E+01 .234000000E+01 .100000000E+01

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.

(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

WHAT TYPE OF WEIGHTING FOR LOGSUM TERMS? ENTER:

1 FOR SHARES

2 FOR NO WEIGHTS

1

HOW MANY ITERATIONS FOR HDM MONTE CARLO?

1000

ENTER A NUMBER FROM 0 TO 46300

3265

CALCULATIONS COMPLETED

HEDONIC DEMAND MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$-.123954701E+04

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:params.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT
2 FOR HEDONIC DEMAND MODEL
2

YOU CHOSE MODEL 2.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE
2 FOR SHARES PREDICTION
3 FOR C S CHANGE, CORRESPONDING SET MEMBERS
3

FOR OPTION 3 SETS NUMBER AND ORDER MUST AGREE

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING HDM MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.

(3f6.3)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

HOW MANY ITERATIONS FOR HDM MONTE CARLO?
1000

ENTER A NUMBER FROM 0 TO 46300
3265

CALCULATIONS COMPLETED

HEDONIC DEMAND MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$-.564065774E+03

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:params.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

2

YOU CHOSE MODEL 2.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS

1

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING HDM MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.
(f9 3f6.3)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

WHAT TYPE OF WEIGHTING FOR LOGSUM TERMS? ENTER:

1 FOR SHARES
2 FOR NO WEIGHTS
0

HOW MANY ITERATIONS FOR HDM MONTE CARLO?
1000

ENTER A NUMBER FROM 0 TO 46300
3265

CALCULATIONS COMPLETED

HEDONIC DEMAND MODEL - CONSUMER SURPLUS

BASE CHOICES = 6 NEW CHOICES = 6

SURPLUS CHANGE PER CONSUMER = \$-.942366764E+03

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:polld.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? a:chars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

1

YOU CHOSE MODEL 1.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS

2

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING MNL MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.
(f9.6)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

BASE YEAR AND PREDICTED MARKET SHARES

| | BASE YEAR | PREDICTED |
|---|---------------|---------------|
| 1 | .22877123E+00 | .24917757E+00 |
| 2 | .18781219E+00 | .21151919E+00 |
| 3 | .17082917E+00 | .15735861E+00 |
| 4 | .20479520E+00 | .17668769E+00 |
| 5 | .51948052E-01 | .59871313E-01 |
| 6 | .15584416E+00 | .14538563E+00 |

C:\FORT>rums

PLEASE ENTER COMPLETE FILENAME FOR PARAMETERS
File name missing or blank - Please enter name

UNIT 11? a:params.dat

PLEASE ENTER FILENAME FOR CHARACTERISTICS
UNIT 12? archars.dat

ESTIMATION OF CONSUMER SURPLUS IN RUMS

WHAT TYPE OF MODEL? ENTER:

1 FOR MULTINOMIAL LOGIT

2 FOR HEDONIC DEMAND MODEL

2

YOU CHOSE MODEL 2.

WHAT TYPE OF ESTIMATION? ENTER:

1 FOR CONSUMER SURPLUS CHANGE

2 FOR SHARES PREDICTION

3 FOR C S CHANGE, CORRESPONDING SET MEMBERS
2

ENTER NUMBER OF ELEMENTS IN BASE CHOICE SET -
6

ENTER NUMBER OF ELEMENTS IN NEW CHOICE SET -
6

ENTER NUMBER OF CHARACTERISTICS -
6

THERE ARE 6 & 6 CHOICES & 6 CHARS.

READING HDM MODEL PARAMETERS . . .

ENTER RECORD FORMAT FOR PARAMS.DAT.
(3f6.3)

ENTER 1 TO PRINT PARAMETERS

READING CHARACTERISTICS & SALES DATA

ENTER RECORD FORMAT FOR CHARS.DAT.
(7f7.2)

ENTER 1 TO PRINT CHARACTERISTICS DATA

HOW MANY ITERATIONS FOR HDM MONTE CARLO?
1000

ENTER A NUMBER FROM 0 TO 46300
3265

BASE YEAR AND PREDICTED MARKET SHARES

| | BASE YEAR | PREDICTED |
|---|---------------|---------------|
| 1 | .22877123E+00 | .38661450E+00 |
| 2 | .18781219E+00 | .92754080E-01 |
| 3 | .17082917E+00 | .77710762E-01 |
| 4 | .20479520E+00 | .11016109E+00 |
| 5 | .51948052E-01 | .24268173E+00 |
| 6 | .15584416E+00 | .90077840E-01 |

INTERNAL DISTRIBUTION

- | | | | |
|-------|---|--------|----------------------------|
| 1-2. | Center for Energy and Environmental Information | 18. | R. Lee |
| 3. | J. Christian | 19. | F. C. Maienschein |
| 4. | G. A. Dailey | 20. | V. C. Mei |
| 5. | T. Dinan | 21. | C. G. Rizy |
| 6. | S. D. Floyd | 22. | R. B. Shelton |
| 7. | W. Fulkerson | 23. | R. A. Stevens |
| 8-12. | D. L. Greene | 24. | D. Vogt |
| 13. | V. J. Harley | 25. | T. J. Wilbanks |
| 14. | L. J. Hill | 26. | G. P. Zimmerman |
| 15. | E. L. Hillsman | 27-28. | Central Research Library |
| 16. | R. B. Honea | 29. | Document Reference Section |
| 17. | C. R. Kerley | 30. | Laboratory Records |
| | | 31-32. | Laboratory Records - RC |
| | | 33. | ORNL Patent Office |

EXTERNAL DISTRIBUTION

34. Office of Assistant Manager for Energy Research and Development, Department of Energy, Oak Ridge Operations Office, Oak Ridge, TN 37831.
35. Jaime G. Carbonell, Associate Professor of Computer Science, Carnegie-Mellon University, Pittsburgh, PA 15213.
36. S. Malcolm Gillis, Dean, Graduate School, Duke University, 4875 Duke Station, Durham, NC 27706.
37. Fritz R. Kalhammer, Vice President, Electric Power Research Institute, Post Office Box 10412, Palo Alto, CA 94303.
38. Roger E. Kasperson, Professor of Government and Geography, Graduate School of Geography, Clark University, Worcester, MA 01610.
39. Martin Lessen, Consulting Engineer, 12 Country Club Drive, Rochester, NY 14618.
- 40-63. Transportation Group Distribution, Energy Division.
- 64-90. Technical Information Center, P.O. Box 62, Oak Ridge, TN 37831.

